| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
|  | Part (a) is a 'Show that..' so equations need to be given in full to earn A marks |  |  |
| 3(a) |  |  |  |
|  | Moments equation: (M1A0 for a moments inequality) | M1 | 3.3 |
|  | $\mathrm{M}(A), m g a \cos \theta=2 S a \sin \theta$ <br> $\mathrm{M}(B), m g a \cos \theta+2 F a \sin \theta=2 R a \cos \theta$ <br> $\mathrm{M}(C), F \times 2 a \sin \theta=m g a \cos \theta$ <br> $\mathrm{M}(D), 2 R a \cos \theta=m g a \cos \theta+2 S a \sin \theta$ <br> $\mathrm{M}(G), R a \cos \theta=F a \sin \theta+S a \sin \theta$. | A1 | 1.1b |
|  | ( $\downarrow$ ) $R=m g$ OR ( $\leftrightarrow$ ) $F=S$ | B1 | 3.4 |
|  | Use their equations (they must have enough) and $F \leq \mu R$ to give an inequality in $\mu$ and $\theta$ only (allow DM1 for use of $F=\mu R$ to give an equation in $\mu$ and $\theta$ only) | DM1 | 2.1 |
|  | $\mu \geq \frac{1}{2} \cot \theta^{*}$ | A1* | 2.2a |
|  |  | (5) |  |
| 3(b) |  |  |  |
|  | Moments equation: | M1 | 3.4 |
|  | $\begin{aligned} & \mathrm{M}(A), m g a \cos \theta=2 N a \sin \theta \\ & \mathrm{M}(B), m g a \cos \theta+2 k m g a \sin \theta=2 R a \cos \theta+\frac{1}{2} m g 2 a \sin \theta \\ & \mathrm{M}(D), 2 R a \cos \theta=m g a \cos \theta+N 2 a \sin \theta \\ & \mathrm{M}(G), k m g a \sin \theta+N a \sin \theta=\frac{1}{2} m g a \sin \theta+R a \cos \theta \end{aligned}$ | A1 | 1.1b |



| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 9(a) | Moments about $A$ (or any other complete method) | M1 | 3.3 |
|  | $T 2 a \sin a=M g a+3 M g x$ | A1 | 1.1b |
|  | $T=\frac{M g(a+3 x)}{2 a^{\prime} \frac{3}{5}}=\frac{5 M g(3 x+a)}{6 a} * \quad \text { GIVEN ANSWER }$ | A1* | 2.1 |
|  |  | (3) |  |
| (b) | $\frac{5 M g(3 x+a)}{6 a} \cos a=2 M g \quad$ OR $\quad 2 M g .2 a \tan \alpha=M g a+3 M g x$ | M1 | 3.1b |
|  | $x=\frac{2 a}{3}$ | A1 | 2.2a |
|  |  | (2) |  |
| (c) | Resolve vertically OR Moments about $B$ | M1 | 3.1b |
|  | $Y=3 M g+M g-\frac{5 M g\left(3 \cdot \frac{2 a}{3}+a\right)}{6 a} \sin a \quad 2 a Y=M g a+3 M g\left(2 a-\frac{2 a}{3}\right)$ Or: $Y=3 M g+M g-\left(\frac{2 M g}{\cos \alpha}\right) \sin \alpha$ | A1ft | 1.1b |
|  | $Y=\frac{5 M g}{2}$ <br> N.B. May use $R \sin \beta$ for $Y$ and/or $R \cos \beta$ for $X$ throughout | A1 | 1.1b |
|  | $\tan \beta=\frac{Y}{X} \quad$ or $\frac{R \sin \beta}{R \cos \beta}=\frac{\frac{5 M g}{2}}{2 M g}$ | M1 | 3.4 |
|  | $=\frac{5}{4}$ | A1 | 2.2a |
|  |  | (5) |  |
| (d) | $\frac{5 M g(3 x+a)}{6 a} \leq 5 M g$ and solve for $x$ | M1 | 2.4 |
|  | $x \leq \frac{5 a}{3}$ | A1 | 2.4 |
|  | For rope not to break, block can't be more than $\frac{5 a}{3}$ from $A$ oe Or just: $\quad x \leq \frac{5 a}{3}$, if no incorrect statement seen. <br> N.B. If the correct inequality is not found, their comment must mention 'distance from $A$ '. | B1 A1 | 2.4 |
|  |  | (3) |  |
| (13 marks) |  |  |  |


| Question | Scheme | Marks | AO |
| :---: | :---: | :---: | :---: |
| 4(a) | Drum smooth, or no friction, (therefore reaction is perpendicular to the ramp) | B1 | 2.4 |
|  |  | (1) |  |
| (b) | N.B. In (b), for a moments equation, if there is an extra $\sin \theta$ or $\cos \theta$ on a length, give M 0 for the equation <br> e.g. $\mathrm{M}(A): 20 g \times 4 \cos \theta=5 N \sin \theta$ would be given M0A0 |  |  |
|  |  |  |  |
|  | Possible equns$\begin{aligned} & (\nearrow): F \cos \theta+R \sin \theta=20 g \sin \theta \\ & (\nwarrow): N+R \cos \theta=20 g \cos \theta+F \sin \theta \\ & (\uparrow) R+N \cos \theta=20 g \\ & (\rightarrow): F=N \sin \theta \\ & \mathrm{M}(A): 20 g \times 4 \cos \theta=5 N \\ & \mathrm{M}(B): 3 N+R \times 8 \cos \theta=F \times 8 \sin \theta+20 g \times 4 \cos \theta \\ & \mathrm{M}(C): R \times 5 \cos \theta=F \times 5 \sin \theta+20 g \times \cos \theta \\ & \mathrm{M}(G): R \times 4 \cos \theta=F \times 4 \sin \theta+N \end{aligned}$ | M1 | 3.3 |
|  |  | A1 | 1.1b |
|  |  | M1 | 3.4 |
|  |  | A1 | 1.1b |
|  |  | M1 | 3.4 |
|  |  | A1 | 1.1b |
|  | (The values of the 3 unknowns are: $N=150.528 ; F=42.14784 ; R=51.49312$ ) |  |  |
|  | Alternative 1: using epts along ramp $(X)$ and perp to $\operatorname{ramp}(V)$ <br> Possible equations: $\begin{aligned} & (\nearrow): X=20 g \sin \theta \\ & (\nwarrow): Y+N=20 g \cos \theta \\ & (\uparrow): X \sin \theta+Y \cos \theta+N \cos \theta=20 g \\ & (\rightarrow): X \cos \theta=Y \sin \theta+N \sin \theta \\ & \mathrm{M}(A): 20 g \times 4 \cos \theta=5 N \\ & \mathrm{M}(B): 20 g \times 4 \cos \theta=8 Y+3 N \\ & \mathrm{M}(C): 20 g \times \cos \theta=5 Y \\ & \mathrm{M}(G): 4 Y=N \times 1 \end{aligned}$ | M1 | 3.3 |
|  |  | A1 | 1.1b |
|  |  | M1 | 3.4 |
|  |  | A1 | 1.1b |
|  |  | M1 | 3.4 |
|  |  | A1 | 1.1b |
|  | (The values of the 3 unknowns are: $N=150.528 ; X=54.88 ; Y=37.632$ ) |  |  |



| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 4(a) | Take moments about $A$ | M1 | 3.3 |
|  | $N \times \frac{4 a}{\sin \alpha}=M g \times 3 a \cos \alpha$ | A1 | 1.1b |
|  | $\frac{9 M g}{25} *$ | A1* | 1.1b |
|  |  | (3) |  |
| 4(b) | Resolve horizontally | M1 | 3.4 |
|  | $(\rightarrow) F=\frac{9 M g}{25} \sin \alpha$ | A1 | 1.1b |
|  | Resolve vertically | M1 | 3.4 |
|  | ( $\uparrow$ ) $R+\frac{9 M g}{25} \cos \alpha=M g$ | A1 | 1.1b |
|  | Other possible equations: $\begin{aligned} & (\nwarrow), R \cos \alpha+\frac{9 M g}{25}=M g \cos \alpha+F \sin \alpha \\ & (\nearrow), M g \sin \alpha=F \cos \alpha+R \sin \alpha \\ & \mathrm{M}(C), M g \cdot 2 a \cos \alpha+F .5 a \sin \alpha=R .5 a \cos \alpha \\ & \mathrm{M}(G), \frac{9 M g}{25} \cdot 2 a+F .3 a \sin \alpha=R .3 a \cos \alpha \\ & \mathrm{M}(B), M g .3 a \cos \alpha+F .6 a \sin \alpha=R .6 a \cos \alpha+\frac{9 M g}{25} a \\ & \left(F=\frac{36 M g}{125}, R=\frac{98 M g}{125}\right) \end{aligned}$ |  |  |
|  | $F=\mu R$ used | M1 | 3.4 |
|  | Eliminate $R$ and $F$ and solve for $\mu$ | M1 | 3.1b |
|  | Alternative equations if they have at $A$ : <br> $X$ horizontally and $Y$ perpendicular to the rod. $\begin{aligned} & \left(\mathbb{)}, Y+\frac{9 M g}{25}=M g \cos \alpha+X \sin \alpha\right. \\ & (\nearrow), M g \sin \alpha=X \cos \alpha \\ & (\uparrow), \frac{9 M g}{25} \cos \alpha+Y \cos \alpha=M g \\ & (\rightarrow), Y \sin \alpha+\frac{9 M g}{25} \sin \alpha=X \end{aligned}$ |  |  |


|  |  | $\mathrm{M}(C), M g .2 a \cos \alpha+X .5 a \sin \alpha=Y .5 a$ <br> $M(G), \frac{9 M g}{25} \cdot 2 a+X .3 a \sin \alpha=Y .3 a$ <br> $M(B), M g .3 a \cos \alpha+X .6 a \sin \alpha=Y .6 a+\frac{9 M g}{25} a$ <br> $\left(X=\frac{4 M g}{3}, Y=\frac{98 M g}{75}\right)$ <br> Then $F=\mu R \quad$ becomes: $X-Y \sin \alpha=\mu Y \cos \alpha$ <br> Eliminate $X$ and $Y$ and solve for $\mu$ |  |  |
| :--- | :--- | :--- | :--- | :--- |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 9(a) | Take moments about $A$ (or any other complete method to produce an equation in $S, \mathrm{~W}$ and $\alpha$ only) | M1 | 3.3 |
|  | $W a \cos \alpha+7 W 2 a \cos \alpha=S 2 a \sin \alpha$ | $\begin{aligned} & \text { A1 } \\ & \text { A1 } \end{aligned}$ | $\begin{aligned} & 1.1 \mathrm{~b} \\ & 1.1 \mathrm{~b} \end{aligned}$ |
|  | Use of $\tan \alpha=\frac{5}{2}$ to obtain $S$ | M1 | 2.1 |
|  | $S=3 W^{*}$ | A1* | 2.2a |
|  |  | (5) |  |
| (b) | $R=8 W$ | B1 | 3.4 |
|  | $F=\frac{1}{4} R(=2 W)$ | M1 | 3.4 |
|  | $P_{\mathrm{MAX}}=3 W+F$ or $P_{\mathrm{MIN}}=3 W-F$ | M1 | 3.4 |
|  | $P_{\mathrm{MAX}}=5 \mathrm{~W}$ or $P_{\mathrm{MIN}}=W$ | A1 | 1.1b |
|  | $W \leq P \leq 5 W$ | A1 | 2.5 |
|  |  | (5) |  |
| (c) | $\mathrm{M}(A)$ shows that the reaction on the ladder at $B$ is unchanged | M1 | 2.4 |
|  | also $R$ increases (resolving vertically) | M1 | 2.4 |
|  | which increases max $F$ available | M1 | 2.4 |
|  |  | (3) |  |
| (13 marks) |  |  |  |



| Q | Scheme | Marks | Notes |
| :---: | :---: | :---: | :---: |
| 5a |  |  |  |
|  | Take moments about $A$ : | M1 | Must be dimensionally correct. Condone $\sin /$ cos confusion |
|  | $5 N=4 \cos \theta W$ | A1 |  |
|  | $N=\frac{12}{25} W=0.48 W \quad * \text { Given Answer* }$ | A1 |  |
|  |  | (3) |  |
| 5b | $G=\frac{1}{4} N=0.12 \mathrm{~W}$ | B1 | Seen or implied |
|  | Resolve vertically | M1 | Needs all terms. Condone sin/cos confusion and sign errors |
|  | $\downarrow: R+N \cos \theta+G \sin \theta=W$ | A1 | $(R=0.616 \mathrm{~W})$ |
|  | Resolve horizontally | M1 | Needs all terms. Condone $\sin /$ cos confusion and sign errors |
|  | $\leftrightarrow: F+G \cos \theta=N \sin \theta$ | A1 | $(F=0.312 \mathrm{~W})$ |
|  | $\mu=\frac{N \sin \theta-G \cos \theta}{W-N \cos \theta-G \sin \theta}$ | DM1 | Use $F=\mu R$ to find $\mu$ <br> Dependent on 2 preceding M marks |
|  | $=\frac{0.48 W \times 0.8-0.12 W \times 0.6}{W-0.48 W \times 0.6-0.12 W \times 0.8}=\frac{0.312}{0.616}$ |  |  |
|  | $=0.51(0.50649 \ldots)\left(\frac{39}{77}\right)$ | A1 |  |
|  |  | (7) |  |
|  |  | [10] |  |
|  | NB, One of the two equations required for part (b) could be a moments equation: <br> $\mathrm{M}(P) \quad 1 \times W \cos \theta+5 F \sin \theta=5 R \cos \theta$ <br> $\mathrm{M}(B) \quad 3 N+8 R \cos \theta=4 W \cos \theta+8 F \sin \theta$ |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 4a | Moments about $A: 0.5 \times 2 g+2 \times 5 g(=11 g)=T \cos \theta \times 4=T \times \frac{3}{5} \times 4$ | M1A2 |
|  | $T=11 g \times \frac{5}{12}=\frac{55}{12} g=44.9(45)(\mathrm{N})$ | A1 (4) |
|  | Notes |  |
|  | N.B. If all $g$ 's are missing, mark as a MR. <br> M1 for $\mathrm{M}(A)$, with usual rules <br> First A1 and second A1 for a correct equation in $T$ only i.e. must be using a correct angle (but value of trig ratio not needed at this stage) Deduct 1 mark for each incorrect term. (A1A0 or A0A0) <br> Third A1 for 45 or 44.9 (N) (A0 for 45.0) |  |
| 4b | Resolving: $\leftrightarrow H=T \sin q$ OR $\mathrm{M}(D), H^{\prime} 3=2 g^{\prime} 0.5+5 g^{\prime} 2$ | M1 |
|  | $\downarrow T \cos q+V=7 \mathrm{~g} \quad$ OR $\quad \mathrm{M}(B), V^{\prime} 4=2 g^{\prime} 3.5+5 g^{\prime} 2$ | M1A1 |
|  | Pythagoras: $\|R\|=\sqrt{41.65^{2}+35.93^{2}}=55.0$ (55) (N) | M1A1 (5) |
|  | Notes |  |
|  | First M1 for resolving horizontally or $\mathrm{M}(D)$ with usual rules to give equation in $T$ only. ( $T$ does not need to be substituted) <br> Second M1 for resolving vertically or $\mathrm{M}(B)$ with usual rules <br> First A1 for a correct equation in $T$ only. ( $T$ does not need to be substituted) <br> Third M1 (independent but must have found 2 components) for squaring, adding and rooting their 2 components <br> Second A1 for 55 or 55.0 |  |
| 4c | Use of $F \leq F_{\max }=\mu R: V \leq \mu H \quad$ (Must have found $H$ and $V$ ) | M1 |
|  | $m^{3} \frac{V}{H}=\frac{41.65}{35.93 . .}=\frac{51}{44}, 1.2$ or better | A1 (2) |
|  | Notes |  |
|  | M1 for use of $V \leq \mu H$ <br> M0 for use of $V=H$ or $V<H$ <br> $m^{3} \frac{V}{H}=\frac{51}{44}$ <br> Allow fraction (since g cancels) or 1.2 or better |  |


| Question <br> Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5a | Moments about $A$ : $6 \mathrm{~g}(\times 1) \times \sin 70=T \sin 30 \times 2$ | M1A2 |
|  | $T=55.3(\mathrm{~N})$ or $55(\mathrm{~N})$ | A1 (4) |
| 5b | Resolve horizontally: $\quad T \cos 50=R(=35.5)$ | B1 ft |
|  | Resolve vertically: $\quad T \sin 50=6 \mathrm{~g} \pm F$ | M1A1 ft |
|  | $\|F\|=16.5 \quad(16.473 \ldots)$ |  |
|  | Use $F=\mu R: \quad \mu=\frac{6 g-T \sin 50}{T \cos 50} \quad$ (with their values) | M1 |
|  | $=0.464$ or 0.46 | A1 (5) |
| 5c | Use of $\tan$ and their components: $\tan ^{-1}\left(\frac{35.5}{16.5}\right)$ | M1 |
|  | $=65.1^{\circ}$ or $65^{\circ}$ to the upward vertical | A1 (2) |
|  | or equivalent ( $24.9^{\circ}$ or $25^{\circ}$ above the | [11] |
|  | horizontal) |  |
|  | Notes |  |
| 5a | First M1 for a complete method to find $T$, with usual rules, correct no. of terms, allow sin/cos confusion, dim correct (missing g is an A error) and allow incorrect angles. <br> First A2 for a correct equation (A1A0 for one error) <br> Third A1 for $55(\mathrm{~N})$ or 55.3 (N) |  |
| 5b | First B1 ft for resolving horizontally ( $T$ does not need to be substituted) First M1 for resolving vertically with usual rules, must be using $40^{\circ}$ or $50^{0}$ <br> First A1 ft for a correct equation ( $T$ does not need to be substituted) Second M1, independent, for use of $F=\mu R$, must have found an $F$ and an $R$ <br> Second A1 for 0.46 or 0.464 <br> N.B. They may resolve in other directions e.g. along the rod or perpendicular to the rod or take moments e.g. about $B$ or $C$ <br> First B1 for a correct equation seen <br> M1A1 for the better equation seen, usual rules etc. |  |
| 5c | First M1 for a complete method to find the angle (must have found the two components) with either the horizontal or vertical |  |
|  | First A1 for $65^{0}$ or $65.1^{0}$ to the upward vertical oe (A0 for just an angle) |  |
|  | Or the angle marked on a clear diagram with an arrow. |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |




