

Mark Scheme (Results) January 2010

GCE

Statistics S2 (6684)



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January 2010 6684 Statistics S2 Mark Scheme

Ques		Scheme		Mark	S
Q1	(a)	$X \sim B(20,0.05)$	B1		(2)
	(b)	$P(X = 0) = 0.95^{20} = 0.3584859$ or 0.3585 using tables.	M1	A1	(2)
	(c)	$P(X > 4) \qquad =1 - P(X \le 4)$	M1		
		=1-0.9974			
		=0.0026	A1		(2)
	(d)	$Mean = 20 \times 0.05 = 1$	B1		
		Variance = $20 \times 0.05 \times 0.95 = 0.95$	B1		(0)
			-	Γotal	(2) [8]
		<u>Notes</u>			
Q1	(a)	1 st B1 for binomial			
		2nd B1 for 20 and 0.05 o.e These must be in part (a)			
	(b)	M1 for finding $(p)^{20}$ $0 this working needs to be seen if answer incorrect to gain the M1 A1 awrt 0.358 or 0.359.$			
	(c)	M1 for writing 1 - $P(X \le 4)$			
		or $1 - [P(X = 0) + P(X = 1) + P(X = 2) + P(X = 3) + P(X = 4)]$ or $1 - 0.9974$ or $1 - 0.9568$			
		A1 awrt 0.0026 or 2.6×10^{-3} , do not accept a fraction e.g. 26/10000			
	(d)	1 st B1 for 1 2 nd B1 for 0.95			
		NB In parts b, c and d correct answers with no working gain full marks			

Ques Numi		Scheme	Marl	KS
Q2	(a)	P(X<0) = F(0)	M1	
		$=\frac{2}{6}=\frac{1}{3}$	A1	(2)
	(b)	$f(x) = \frac{dF(x)}{dx}$	M1	
		$f(x) = \frac{dF(x)}{dx}$ $f(x) = \begin{cases} \frac{1}{6} & -2 \le x \le 4\\ 0 & \text{otherwise} \end{cases}$	A1 B1	(3)
	(c)	Continuous Uniform (Rectangular) distribution	B1	(1)
	(d)	Mean = 1	B1	(1)
		Variance is $\frac{(42)^2}{12} = 3$	M1 A1	(3)
	(e)	P(X=1)=0	B1	(1)
		<u>Notes</u>	Total	[10]
Q2	(a)	M1 for attempting to find F(0) by a correct method eg subst 0 into F(x) or $\int_{-2}^{0} \frac{1}{6} dx$		
		Do NOT award M1 for $\int_{-2}^{0} \frac{x+2}{6} dx$ or $\frac{1}{2} \times \frac{1}{3} \times 2$ both of which give the correct		
		answer by using $F(x)$ as the pdf A1 1/3 o.e or awrt 0.333 Correct answer only with no incorrect working gets M1 A1		
	(b)	M1 for attempting to differentiate $F(x)$. (for attempt it must have no xs in) A1 for the first line. Condone $<$ signs B1 for the second line. – They must have $0 \ x < -2$ and $x > 4$ only.		
	(c)	B1 must have "continuous" and "uniform" or "Rectangular"		
	(d)	B1 for mean $= 1$		
		M1 for attempt to use $\frac{[\pm (b-a)]^2}{12}$, they must subst in values and not just quote the		
		formula, or using $\int_{-2}^{4} x^2 (their f(x)) - (their mean)^2$, including limits. Must get x^3		
		when they integrate. A1 cao .		
	(e)	B1 cao		

Ques		Scheme	Mark	S
Q3	(a)	$Y \sim \text{Po}(0.25)$	B1	
		$P(Y=0) = e^{-0.25} = 0.7788$	M1 A1	(2)
	(b)	$X \sim \text{Po}(0.4)$	B1	(3)
		P(Robot will break down) = $1 - P(X = 0)$		
		$=1-e^{-0.4}$	M1	
		=1-0.067032		
		= 0.3297	A1	(3)
	(c)	$P(X=2) = \frac{e^{-0.4}(0.4)^2}{2}$	M1	` '
		-		
		= 0.0536	A1	(2)
	(4)	0.2207	D1ft	` '
	(d)	0.3297 or answer to part (b) as Poisson events are <u>independent</u>	B1ft B1 dep	
				(2)
			Total	[10]
		Notes		
Q3	(a)	B1 for seeing or using Po(0.25)		
		M1 for finding P(Y =0) either by e^{-a} , where a is positive (a needn't equal their λ) or using tables if their value of λ is in them Beware common Binomial error using, $p = 0.05$ gives 0.7738 but scores B0 M0 A0 A1 awrt 0.779		
	(h)	D1 for the control of D2 (0.4) in most (b) and (c)		
	(b)	B1 for stating or a clear use of Po(0.4) in part (b) or (c) M1 for writing or finding 1 – P(X = 0) A1 awrt 0.33		
	(c)	M1 for finding P(X = 2) e.g $\frac{e^{-\lambda} \lambda^2}{2!}$ with their value of λ in		
		or if their λ is in the table for writing $P(X \le 2)$ - $P(X \le 1)$ A1 awrt 0.0536		
	(d)	1 st B1 their answer to part(b) correct to 2 sf or awrt 0.33 2 nd B1 need the word independent. This is dependent on them gaining the first B1 SC		
		Use of Binomial.		
		Mark parts a and b as scheme. They could get (a) B0,M0,A0 (b) B0 M1 A0 In part c allow M1 for ${}^{n}C_{2}(p)^{2}(1-p)^{n-2}$ with "their n" and "their p ". They could get (c) In a constant p and p and p and p and p are p and p and p are p are p and p are p and p are p and p are p are p are p and p are p are p and p are p are p and p are p are p are p and p are p are p and p are p are p and p are p and p are p are p are p are p are p and p are p are p and p are p are p and p are p and p are p ar	M1,A0	
		DO NOT GIVE for $p(x \le 2) - p(x \le 1)$ In (d) they can get the first B1 only. They could get (d) B1B0		
L		in (a) they can get the first by omy. They come get (a) by by		

Question Number	Scheme	Marks
Q4 (a)	$\int_0^3 k(x^2 - 2x + 2) dx + \int_3^4 3k dx = 1$	M1
	$k \left[\frac{1}{3}x^3 - x^2 + 2x \right]_0^3 + \left[3kx \right]_3^4 (=1) \text{or} k \left[\frac{1}{3}x^3 - x^2 + 2x \right]_0^3 + 3k (=1)$ $9k = 1$	A1 M1 dep
4.	$k = \frac{1}{9} **given** $ cso	A1 (4)
(b)	For $0 < x \le 3$, $F(x) = \int_0^x \frac{1}{9} (t^2 - 2t + 2) dt$	M1
	$= \frac{1}{9} \left(\frac{1}{3} x^3 - x^2 + 2x \right)$	A1
	For $3 < x \le 4$, $F(x) = \int_3^x 3k dt + \frac{2}{3}$	M1
	$=\frac{x}{3}-\frac{1}{3}$	A1
	$ \begin{pmatrix} 0 & x \le 0 \\ \frac{1}{x}(x^3 - 3x^2 + 6x) & 0 < x \le 3 \end{pmatrix} $	
	$F(x) = \begin{cases} 0 & x \le 0 \\ \frac{1}{27}(x^3 - 3x^2 + 6x) & 0 < x \le 3 \\ \frac{x}{3} - \frac{1}{3} & 3 < x \le 4 \end{cases}$	B1 ft
	$\begin{bmatrix} 3 & 3 \\ 1 & x > 4 \end{bmatrix}$	B1 (6)
(c)	$E(X) = \int_0^3 \frac{x}{9} (x^2 - 2x + 2) dt + \int_3^4 \frac{x}{3} dx$	M1
	$= \frac{1}{9} \left[\frac{1}{4} x^4 - \frac{2}{3} x^3 + x^2 \right]_0^3 + \left[\frac{1}{6} x^2 \right]_3^4$	A1
	$=\frac{29}{12}$ or 2.416 or awrt 2.42	A1
(d)	F(m) = 0.5	(3) M1
	$F(2.6) = \frac{1}{27}(2.6^3 - 3 \times 2.6^2 + 6 \times 2.6) = \text{awrt } 0.48$	M1
	$F(2.7) = \frac{1}{27}(2.7^3 - 3 \times 2.7^2 + 6 \times 2.7) = \text{awrt } 0.52$	A1
	Hence median lies between 2.6 and 2.7	A1 dA (4)
		Total [17]

Notes

Q4 (a)

(a) 1^{st} M1 attempting to integrate **at least one** part (at least one $x^n \to x^{n+1}$) (ignore limits)

1st A1 Correct integration. Limits not needed.

 2^{nd} M1 dependent on the previous M being awarded. Adding the two answers together, putting equal to 1 and have the correct limits.

2nd A1 cso

(b)

1st M1 Att to integrate $\frac{1}{9}(t^2 - 2t + 2)$ (at least one $x^n \to x^{n+1}$). Ignore limits for method mark

1st A1 $\frac{1}{9} \left(\frac{x^3}{3} - x^2 + 2x \right)$ allow use of t. Must have used/implied use of limit of 0.

This must be on its own without anything else added

 2^{nd} M1 attempting to find $\int_3^x 3k + \dots$ (must get 3kt or 3kx)

and they must use the correct limits and add $\int_0^3 \frac{1}{9} (t^2 - 2t + 2)$ or $\frac{2}{3}$

or use + C and use F(4) = 1

 $2^{\text{nd}} \text{ A} 1 \frac{x}{3} - \frac{1}{3}$ must be correct

 1^{st} B1 middle pair followed through from their answers. condone them using < or \le incorrectly they do not need to match up

2nd B1 end pairs, condone them using < or <. They do not need to match up

NB if they show no working and just write down the distribution. If it is correct they get full marks. If it is incorrect then they cannot get marks for any incorrect part. So if $0 < x \le 3$ is correct they can get M1 A1 otherwise M0 A0. If $3 < x \le 4$ is correct they can get M1 A1 otherwise M0 A0. you cannot award B1ft if they show no working unless the middle parts are correct.

(c) $\mathbf{1}^{st}$ M1 attempting to use integral of x f(x) on one part $\mathbf{1}^{st}$ A1 Correct Integration for both parts added together. Ignore limits. $\mathbf{2}^{nd}$ A1 cao or awrt 2.42

(d) $\mathbf{1}^{\text{st}} \mathbf{M1}$ for using F(X) = 0.5. This may be implied by subst into F(X) and comparing answers with 0.5.

 2^{nd} M1 for substituting both 2.6 and 2.7 into "their F(X)" – 0.5 or "their F(X)"

 1^{st} A1 awrt 0.48 and 0.52 if using "their F(X)" and awrt -0.02 and 0.02 or if using "their F(X)" 0.5

Other values possible. You may need to check their values for their correct equation NB these last two marks are B1 B1 on ePEN but mark as M1 A1

 2^{nd} A1 for conclusion but only award if it follows from their numbers. Dependent on previous A mark being awarded

SC using calculators

M1 for sign of a suitable equation

M1 A1 for awrt 2.66 provided equation is correct

A1 correct comment

Question Number	Scheme	Marks
Q5 (a)	$X \sim \text{Po}(10)$ $P(X < 9) = P(X \le 8)$ = 0.3328	B1 M1 A1 (3)
(b)	Y ~ Po(40) Y is approximately N(40,40) P(Y > 50) = 1 - P(Y \leq 50) = 1 - P\Bigg(Z < \frac{50.5 - 40}{\sqrt{40}}\Bigg) = 1 - P(Z < 1.660) = 1 - 0.9515 = 0.0485	M1 A1 M1 M1 A1 A1 (6) Total [9]
	N.B. Calculator gives 0.048437. Poisson gives 0.0526 (but scores nothing)	
Q5 (a)	Notes B1 for using Po(10) M1 for attempting to find P($X \le 8$): useful values P($X \le 9$) is 0.4579(M0), using Po(6) gives 0.8472, (M1). A1 awrt 0.333 but do not accept $\frac{1}{3}$	
(b)	1st M1 for identifying the normal approximation 1st A1 for [mean = 40] and [sd = $\sqrt{40}$ or var = 40] NB These two marks are B1 M1 on ePEN These first two marks may be given if the following are seen in the standardisation formula: 40 and $\sqrt{40}$ or awrt 6.32 2nd M1 for attempting a continuity correction (50 or 30 ± 0.5 is acceptable) 3rd M1 for standardising using their mean and their standard deviation and using either 49.5, 50 or 50.5. (29.5, 30, 30.5) accept ± 2nd A1 correct z value awrt ±1.66 or this may be awarded if see ± $\frac{50.5 - 40}{\sqrt{40}}$ or $\pm \frac{29.5 - 40}{\sqrt{40}}$ 3rd A1 awrt 3 sig fig in range 0.0484 – 0.0485	

Ques Num		Scheme	Marks
Q6	(a)	The set of values of the test statistic for which the null hypothesis is rejected in a hypothesis test.	B1 B1
	(b)	$X \sim B(30,0.3)$ $P(X \le 3) = 0.0093$	(2) M1
		$P(X \le 2) = 0.0021$ $P(X \ge 16) = 1 - 0.9936 = 0.0064$	A1
		$P(X \ge 17) = 1 - 0.9979 = 0.0021$ Critical region is $(0 \le)x \le 2$ or $16 \le x (\le 30)$	A1 A1A1
	(c)	Actual significance level 0.0021+0.0064=0.0085 or 0.85%	(5) B1 (1)
	(d)	15 (it) is not in the critical region not significant	Bft 2, 1, 0
		No significant evidence of a change in $p = 0.3$ accept H_0 , (reject H_1) $P(x \ge 15) = 0.0169$	(2) Total [10]
		<u>Notes</u>	
Q6	(a)	1 st B1 for "values/ numbers" 2 nd B1 for "reject the null hypothesis" o.e or the test is significant	
	(b)	M1 for using B(30,0.3) 1 st A1 $P(x \le 2) = 0.0021$ 2 nd A1 0.0064	
		3^{rd} A1 for $(X) \le 2$ or $(X) < 3$ They get A0 if they write $P(X \le 2/X < 3)$ 4^{th} A1 $(X) \ge 16$ or $(X) > 15$ They get A0 if they write $P(X \ge 16 X > 15)$ NB these are B1 B1 but mark as A1 A1	
	(c)	 16≤ X ≤ 2 etc is accepted To describe the critical regions they can use any letter or no letter at all. It does not have to be X. B1 correct answer only 	
	(d)	Follow through 15 and their critical region B1 for any one of the 5 correct statements up to a maximum of B2 - B1 for any incorrect statements	

Ques		Scheme	Marks
Q7	(a)	$ \begin{array}{c ccc} x & 1p & 2p \\ P(X = x) & \frac{1}{4} & \frac{3}{4} \end{array} $	
		$\mu = 1 \times \frac{1}{4} + 2 \times \frac{3}{4} = \frac{7}{4} \text{ or } 1\frac{3}{4} \text{ or } 1.75$	B1
		$\sigma^2 = 1^2 \times \frac{1}{4} + 2^2 \times \frac{3}{4} - \left(\frac{7}{4}\right)^2$	M1
		$=\frac{3}{16}$ or 0.1875	A1 (3)
	(b)	(1,1,1), (1,1,2) any order, (1,2,2) any order, (2,2,2)	B1
		(1,2,1) (2,1,1) (2,1,2) (2,2,1) all 8 cases considered. May be implied by $3*(1,1,2)$ and $3*(1,2,2)$	B1 (2)
	(c)	\overline{x} 1 $\frac{4}{3}$ $\frac{5}{3}$ 2	B1 M1 A1
		$P(\overline{X} = \overline{x}) \begin{vmatrix} \frac{1}{4} \times \frac{1}{4} \times \frac{1}{4} = \frac{1}{64} \\ 3 \times \frac{1}{4} \times \frac{1}{4} \times \frac{3}{4} = \frac{9}{64} \\ 3 \times \frac{1}{4} \times \frac{3}{4} \times \frac{3}{4} = \frac{27}{64} \end{vmatrix} \qquad \frac{3}{4} \times \frac{3}{4} \times \frac{3}{4} = \frac{27}{64}$	M1 A1A1
			(6)
			Total [11]
Q7	(a)	Notes B1 1.75 oe M1 for using $\sum (x^2 p) - \mu^2$ A1 0.1875 oe	
	(b)	ignore repeats	
	(c)	$1^{\rm st}$ B1 4 correct means (allow repeats) $1^{\rm st}$ M1 for p^3 for either of the ends 1st A1 for 1/64or awrt 0.016 and 27/64 or awrt 0.422 $2^{\rm nd}$ M1 $3\times p^2(1-p)$ for either of the middle two $0 May be awarded for finding the probability of the 3 samples with mean of either 4/3 or 5/3 . 2^{\rm nd} A1 for 9/64 (or 3/64 three times) and 27/64 (or 9/64 three times) accept awrt 3dp. 3^{\rm rd} A1 fully correct table, accept awrt 3dp.$	

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