1. A particle P moves with constant acceleration $(2\mathbf{i} - 3\mathbf{j})\,\text{m s}^{-2}$

At time $t = 0$, P is moving with velocity $4\mathbf{i}\,\text{m s}^{-1}$

(a) Find the velocity of P at time $t = 2$ seconds.

(2)

At time $t = 0$, the position vector of P relative to a fixed origin O is $(\mathbf{i} + \mathbf{j})\,\text{m}$.

(b) Find the position vector of P relative to O at time $t = 3$ seconds.

(2)

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8. [*In this question* **i** *and* **j** *are horizontal unit vectors due east and due north respectively and position vectors are given relative to the fixed point O.*]

A particle P moves with constant acceleration.
At time $t = 0$, the particle is at O and is moving with velocity $(2\mathbf{i} - 3\mathbf{j})\,\text{m s}^{-1}$
At time $t = 2$ seconds, P is at the point A with position vector $(7\mathbf{i} - 10\mathbf{j})\,\text{m}$.

(a) Show that the magnitude of the acceleration of P is $2.5\,\text{m s}^{-2}$

(4)

At the instant when P leaves the point A, the acceleration of P changes so that P now moves with constant acceleration $(4\mathbf{i} + 8.8\mathbf{j})\,\text{m s}^{-2}$

At the instant when P reaches the point B, the direction of motion of P is north east.

(b) Find the time it takes for P to travel from A to B.

(4)

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2. A particle, P, moves with constant acceleration $(2\mathbf{i} - 3\mathbf{j})\,\text{m s}^{-2}$

At time $t = 0$, the particle is at the point A and is moving with velocity $(-\mathbf{i} + 4\mathbf{j})\,\text{m s}^{-1}$

At time $t = T$ seconds, P is moving in the direction of vector $(3\mathbf{i} - 4\mathbf{j})$

(a) Find the value of T.

(4)

At time $t = 4$ seconds, P is at the point B.

(b) Find the distance AB.

(4)

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2. A particle P moves with acceleration $(4\mathbf{i} - 5\mathbf{j})\,\text{m s}^{-2}$

At time $t = 0$, P is moving with velocity $(-2\mathbf{i} + 2\mathbf{j})\,\text{m s}^{-1}$

(a) Find the velocity of P at time $t = 2$ seconds.

(2)

At time $t = 0$, P passes through the origin O.

At time $t = T$ seconds, where $T > 0$, the particle P passes through the point A.

The position vector of A is $(\lambda\mathbf{i} - 4.5\mathbf{j})$m relative to O, where λ is a constant.

(b) Find the value of T.

(4)

(c) Hence find the value of λ

(2)

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8. [*In this question* **i** *and* **j** *are horizontal unit vectors due east and due north respectively*]

A radio controlled model boat is placed on the surface of a large pond.

The boat is modelled as a particle.

At time $t = 0$, the boat is at the fixed point O and is moving due north with speed 0.6 m s^{-1}.

Relative to O, the position vector of the boat at time t seconds is **r** metres.

At time $t = 15$, the velocity of the boat is $(10.5\mathbf{i} - 0.9\mathbf{j})$ m s^{-1}.

The acceleration of the boat is constant.

(a) Show that the acceleration of the boat is $(0.7\mathbf{i} - 0.1\mathbf{j})$ m s^{-2}.

(2)

(b) Find **r** in terms of t.

(2)

(c) Find the value of t when the boat is north-east of O.

(3)

(d) Find the value of t when the boat is moving in a north-east direction.

(3)

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6. [*In this question,* **i** *is a horizontal unit vector and* **j** *is an upward vertical unit vector*.]

A particle P is projected from a fixed origin O with velocity $(3\mathbf{i} + 4\mathbf{j})$ m s^{-1}. The particle moves freely under gravity and passes through the point A with position vector $\lambda(\mathbf{i} - \mathbf{j})$m, where λ is a positive constant.

(a) Find the value of λ.

(6)

(b) Find

(i) the speed of P at the instant when it passes through A,

(ii) the direction of motion of P at the instant when it passes through A.

(7)

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2. [*In this question* **i** *and* **j** *are perpendicular unit vectors in a horizontal plane.*]

Three forces, $(-10\mathbf{i} + a\mathbf{j})$ N, $(b\mathbf{i} - 5\mathbf{j})$ N and $(2a\mathbf{i} + 7\mathbf{j})$ N, where a and b are constants, act on a particle P of mass 3 kg. The acceleration of P is $(3\mathbf{i} + 4\mathbf{j})$ m s^{-2}

(a) Find the value of a and the value of b.

(5)

At time $t = 0$ seconds the speed of P is u m s^{-1} and at time $t = 4$ seconds the velocity of P is $(20\mathbf{i} + 20\mathbf{j})$ m s^{-1}

(b) Find the value of u.

(4)

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4. [*In this question* **i** *and* **j** *are horizontal unit vectors due east and due north respectively and position vectors are given relative to a fixed origin O*]

A particle P is moving with velocity $(\mathbf{i} - 2\mathbf{j})$ km h^{-1}. At time $t = 0$ hours, the position vector of P is $(-5\mathbf{i} + 9\mathbf{j})$ km. At time t hours, the position vector of P is $\mathbf{p}$ km.

(a) Find an expression for $\mathbf{p}$ in terms of t.

(2)

The point A has position vector $(3\mathbf{i} + 2\mathbf{j})$ km.

(b) Find the position vector of P when P is due west of A.

(4)

Another particle Q is moving with velocity $\left[(2b - 1)\mathbf{i} + (5 - 2b)\mathbf{j}\right]$ km h^{-1} where b is a constant.

Given that the particles are moving along parallel lines,

(c) find the value of b.

(4)

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6. [*In this question* **i** *and* **j** *are horizontal unit vectors due east and due north respectively.*]

A particle P moves with constant acceleration $(-2\mathbf{i} + 3\mathbf{j})\,\text{m s}^{-2}$. At time t seconds, the velocity of P is $\mathbf{v}\,\text{m s}^{-1}$. When $t = 0$, $\mathbf{v} = 10\mathbf{i} + 4\mathbf{j}$.

(a) Find the direction of motion of P when $t = 6$, giving your answer as a bearing to the nearest degree.

(5)

(b) Find the value of t when P is moving north east.

(4)

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5. Two forces, $\mathbf{F}_1$ and $\mathbf{F}_2$, act on a particle A.

$\mathbf{F}_1 = (2\mathbf{i} - 3\mathbf{j})$ N and $\mathbf{F}_2 = (p\mathbf{i} + q\mathbf{j})$ N, where p and q are constants.

Given that the resultant of $\mathbf{F}_1$ and $\mathbf{F}_2$ is parallel to $(\mathbf{i} + 2\mathbf{j})$,

(a) show that $2p - q + 7 = 0$

(5)

Given that $q = 11$ and that the mass of A is 2 kg, and that $\mathbf{F}_1$ and $\mathbf{F}_2$ are the only forces acting on A,

(b) find the magnitude of the acceleration of A.

(5)

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7. A particle P moves from point A to point B with constant acceleration $(c\mathbf{i} + d\mathbf{j})$ m s^{-2}, where c and d are positive constants. The velocity of P at A is $(-3\mathbf{i} - 3\mathbf{j})$ m s^{-1} and the velocity of P at B is $(2\mathbf{i} + 9\mathbf{j})$ m s^{-1}. The magnitude of the acceleration of P is 2.6 m s^{-2}.

Find the value of c and the value of d.

(5)

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5. [*In this question* **i** *and* **j** *are horizontal unit vectors due east and due north respectively. Position vectors are given relative to a fixed origin O.*]

A boy B is running in a field with constant velocity $(3\mathbf{i} - 2\mathbf{j})$ m s^{-1}. At time $t = 0$, B is at the point with position vector $10\mathbf{j}$ m.

Find

(a) the speed of B,

(2)

(b) the direction in which B is running, giving your answer as a bearing.

(3)

At time $t = 0$, a girl G is at the point with position vector $(4\mathbf{i} - 2\mathbf{j})$ m. The girl is running with constant velocity $\left(\frac{5}{3}\mathbf{i} + 2\mathbf{j}\right)$ m s^{-1} and meets B at the point P.

(c) Find

(i) the value of t when they meet,

(ii) the position vector of P.

(6)

Leave blank

6. [*In this question* **i** *and* **j** *are perpendicular horizontal unit vectors.*]

A particle P of mass 2 kg moves under the action of two forces, $(2\mathbf{i} + 3\mathbf{j})$ N and $(4\mathbf{i} - 5\mathbf{j})$ N.

(a) Find the magnitude of the acceleration of P.

(4)

At time $t = 0$, P has velocity $(-u\mathbf{i} + u\mathbf{j})$ m s^{-1}, where u is a positive constant.

At time $t = T$ seconds, P has velocity $(10\mathbf{i} + 2\mathbf{j})$ m s^{-1}.

(b) Find

(i) the value of T,

(ii) the value of u.

(5)

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2. A particle P of mass 0.5 kg moves under the action of a single constant force $(2\mathbf{i} + 3\mathbf{j})$N.

(a) Find the acceleration of P.

(2)

At time t seconds, P has velocity $\mathbf{v}$ m s^{-1}. When $t = 0$, $\mathbf{v} = 4\mathbf{i}$

(b) Find the speed of P when $t = 3$

(4)

Given that P is moving parallel to the vector $2\mathbf{i} + \mathbf{j}$ at time $t = T$

(c) find the value of T.

(3)

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