

Please check the examination details below before entering your candidate information	
Candidate surname	Other names
Centre Number	Candidate Number
Pearson Edexcel Level 3 GCE	
Monday 13 May 2024	
Afternoon (Time: 1 hour 40 minutes)	Paper reference 8FM0/01
Further Mathematics Advanced Subsidiary PAPER 1: Core Pure Mathematics	
You must have: Mathematical Formulae and Statistical Tables (Green), calculator	Total Marks

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 80.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1. The cubic equation

$$2x^3 - 3x^2 + 5x + 7 = 0$$

has roots α , β and γ .

Without solving the equation, determine the exact value of

(i) $\alpha^2 + \beta^2 + \gamma^2$ (3)

(ii) $\frac{3}{\alpha} + \frac{3}{\beta} + \frac{3}{\gamma}$ (3)

(iii) $(5 - \alpha)(5 - \beta)(5 - \gamma)$ (3)

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Question 1 continued

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Question 1 continued

Lined area for writing answers.

(Total for Question 1 is 9 marks)



2. With respect to the **right-hand rule**, a rotation through θ° anticlockwise about the z -axis is represented by the matrix
- $$\begin{pmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Given that the matrix $\mathbf{M}$, where

$$\mathbf{M} = \begin{pmatrix} -\frac{\sqrt{3}}{2} & \frac{1}{2} & 0 \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

represents a rotation through α° anticlockwise about the z -axis with respect to the **right-hand rule**,

- (a) determine the value of α . (1)

- (b) Hence determine the smallest possible positive integer value of k for which $\mathbf{M}^k = \mathbf{I}$ (2)

The 3×3 matrix $\mathbf{N}$ represents a reflection in the plane with equation $y = 0$

- (c) Write down the matrix $\mathbf{N}$. (1)

The point A has coordinates $(-2, 4, 3)$

The point B is the image of the point A under the transformation represented by matrix $\mathbf{M}$ followed by the transformation represented by matrix $\mathbf{N}$.

- (d) Show that the coordinates of B are $(2 + \sqrt{3}, 2\sqrt{3} - 1, 3)$ (2)

Given that O is the origin,

- (e) show that, to 3 significant figures, the size of angle AOB is 66.9° (2)

- (f) Hence determine the area of triangle AOB , giving your answer to 3 significant figures. (2)



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Question 2 continued

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Question 2 continued

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(Total for Question 2 is 10 marks)



3. (a) Use the standard results for summations to show that, for all positive integers n ,

$$\sum_{r=1}^n r^2(r+1) = \frac{1}{12}n(n+1)(n+2)(an+b)$$

where a and b are integers to be determined.

(4)

- (b) Hence show that, for all positive integers k ,

$$\sum_{r=k+1}^{3k} r^2(r+1) = \frac{1}{3}k(3k+1)(Ak^2+Bk+C)$$

where A , B and C are integers to be determined.

(3)

- (c) Hence, using algebra and making your method clear, determine the value of k for which

$$25 \sum_{r=k+1}^{3k} r^2(r+1) = 192k^3(3k+1)$$

(3)

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Question 3 continued

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Question 3 continued

Lined area for writing the answer to Question 3.

(Total for Question 3 is 10 marks)



4.

$$\mathbf{A} = \begin{pmatrix} -1 & -2 & -7 \\ 3 & k & 2 \\ 1 & 1 & 4 \end{pmatrix} \quad \mathbf{B} = \begin{pmatrix} 4k-2 & 1 & 7k-4 \\ -10 & 3 & -19 \\ 3-k & -1 & 6-k \end{pmatrix}$$

where k is a constant.

(a) Determine the value of the constant c for which

$$\mathbf{AB} = (3k + c)\mathbf{I} \quad (2)$$

(b) Hence determine the value of k for which $\mathbf{A}^{-1}$ does not exist.

(2)

Given that $\mathbf{A}^{-1}$ does exist,

(c) write down $\mathbf{A}^{-1}$ in terms of k .

(1)

(d) Use the answer to part (c) to solve the simultaneous equations

$$-x - 2y - 7z = 10$$

$$3x + ky + 2z = 3$$

$$x + y + 4z = 1$$

giving the values of x , y and z in simplest form in terms of k .

(3)

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Question 4 continued

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Question 4 continued

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Question 4 continued

Handwriting practice area with horizontal lines.

(Total for Question 4 is 8 marks)





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Question 5 continued

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Question 5 continued

Lined area for writing the answer to Question 5.

(Total for Question 5 is 10 marks)



- (d) the shortest distance between pipes P_1 and P_2 (5)

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Question 6 continued

Lined area for writing the answer to Question 6.



Question 6 continued

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Question 6 continued

Lined area for writing answers.

(Total for Question 6 is 12 marks)



7. (i) Prove by induction that, for all positive integers n ,

$$\sum_{r=1}^n \frac{1}{r(r+1)} = \frac{n}{n+1} \quad (5)$$

- (ii) Prove by induction that, for all positive integers n ,

$$f(n) = 3^{2n+4} - 2^{2n}$$

is divisible by 5

(5)

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 10 marks)



8.

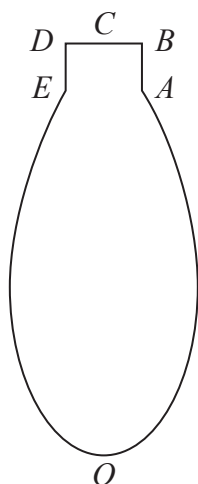


Figure 1

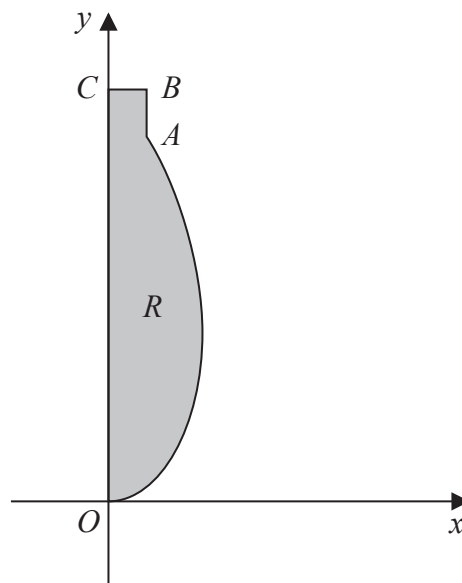


Figure 2

Figure 1 shows the central vertical cross-section, $OABCDEO$, of the design for a solid glass ornament.

Figure 2 shows the finite region, R , which is bounded by the y -axis, the horizontal line CB , the vertical line BA , and the curve AO .

The ornament is formed by rotating the region R through 360° about the y -axis.

The curve AO is modelled by the equation

$$x = ky^2 + \sqrt{y} \quad 0 \leq y \leq 4$$

where k is a constant.

The point A has coordinates $(0.4, 4)$ and the point B has coordinates $(0.4, 4.5)$

The units are centimetres.

- (a) Determine the value of k according to this model. (2)
- (b) Use algebraic integration to determine the exact volume of glass that would be required to make the ornament, according to the model. (7)
- (c) State a limitation of the model. (1)

When the ornament was manufactured, 9 cm^3 of glass was required.

- (d) Use this information and your answer to part (b) to evaluate the model, explaining your reasoning. (1)



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Question 8 continued

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