

# Mark Scheme (Results)

# Summer 2012

GCE Core Mathematics C4 (6666) Paper 1



#### Edexcel and BTEC Qualifications

Edexcel and BTEC qualifications come from Pearson, the world's leading learning company. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. For further information, please visit our website at <u>www.edexcel.com</u>.

Our website subject pages hold useful resources, support material and live feeds from our subject advisors giving you access to a portal of information. If you have any subject specific questions about this specification that require the help of a subject specialist, you may find our Ask The Expert email service helpful.

www.edexcel.com/contactus

#### Pearson: helping people progress, everywhere

Our aim is to help everyone progress in their lives through education. We believe in every kind of learning, for all kinds of people, wherever they are in the world. We've been involved in education for over 150 years, and by working across 70 countries, in 100 languages, we have built an international reputation for our commitment to high standards and raising achievement through innovation in education. Find out more about how we can help you and your students at: www.pearson.com/uk

Summer 2012 Publications Code UA031959 All the material in this publication is copyright © Pearson Education Ltd 2012

### General Marking Guidance

- •All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- •Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- •All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- •Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- •When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol  $\ensuremath{\bigwedge}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

### **General Principles for Core Mathematics Marking**

(But note that specific mark schemes may sometimes override these general principles).

### Method mark for solving 3 term quadratic:

1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q)$$
, where  $|pq| = |c|$ , leading to  $x = \dots$   
 $(ax^2 + bx + c) = (mx + p)(nx + q)$ , where  $|pq| = |c|$  and  $|mn| = |a|$ , leading to  $x = \dots$ 

### 2. <u>Formula</u>

Attempt to use <u>correct</u> formula (with values for a, b and c), leading to  $x = \dots$ 

3. Completing the square

Solving  $x^2 + bx + c = 0$ :  $(x \pm \frac{b}{2})^2 \pm q \pm c$ ,  $q \neq 0$ , leading to  $x = \dots$ 

#### Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ( $x^n \rightarrow x^{n-1}$ )

#### 2. Integration

Power of at least one term increased by 1. ( $x^n \rightarrow x^{n+1}$ )

#### Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

#### Exact answers

Examiners' reports have emphasised that where, for example, an <u>exact</u> answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

#### Answers without working

The rubric says that these <u>may</u> not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

## June 2012 6666 Core Mathematics C4 Mark Scheme

Question Number	Scheme	Marks
Question Number	Scheme (a) $1 = A(3x-1)^2 + Bx(3x-1) + Cx$ $x \to 0$ $(1=A)$ $x \to \frac{1}{3}$ $1 = \frac{1}{3}C \Rightarrow C = 3$ any two constants correct Coefficients of $x^2$ $0 = 9A + 3B \Rightarrow B = -3$ all three constants correct (b)(i) $\int \left(\frac{1}{x} - \frac{3}{3x-1} + \frac{3}{(3x-1)^2}\right) dx$ $= \ln x - \frac{3}{3}\ln(3x-1) + \frac{3}{(-1)3}(3x-1)^{-1}$ (+C) $\left(= \ln x - \ln(3x-1) - \frac{1}{3x-1} + (+C)\right)$ (ii) $\int_1^2 f(x) dx = \left[\ln x - \ln(3x-1) - \frac{1}{3x-1}\right]_1^2$ $= \left(\ln 2 - \ln 5 - \frac{1}{5}\right) - \left(\ln 1 - \ln 2 - \frac{1}{2}\right)$ $= \ln \frac{2 \times 2}{5} + \dots$ $= \frac{3}{10} + \ln\left(\frac{4}{5}\right)$	Marks B1 M1 A1 A1 A1 (4) M1 A1ft A1ft M1 A1 A1 (6) [10]
		[10]

Question Number	Scheme	N	larks
2.	(a) $V = x^3 \Rightarrow \frac{dV}{dx} = 3x^2 $ <b>*</b> cso	B1	(1)
	(b) $\frac{\mathrm{d}x}{\mathrm{d}t} = \frac{\mathrm{d}x}{\mathrm{d}V} \times \frac{\mathrm{d}V}{\mathrm{d}t} = \frac{0.048}{3x^2}$	M1	
	At $x = 8$ $\frac{dx}{dt} = \frac{0.048}{3(8^2)} = 0.00025 \text{ (cm s}^{-1}\text{)}$ $2.5 \times 10^{-4}$	A1	(2)
	(c) $S = 6x^2 \implies \frac{dS}{dx} = 12x$	B1	
	$\frac{\mathrm{d}S}{\mathrm{d}t} = \frac{\mathrm{d}S}{\mathrm{d}x} \times \frac{\mathrm{d}x}{\mathrm{d}t} = 12x \left(\frac{0.048}{3x^2}\right)$	M1	
	At $x=8$ $\frac{dS}{dt} = 0.024  (cm^2 s^{-1})$	A1	(3) [6]

Question Number	Scheme	Marks
3.	(a) $f(x) = ( x)^{-\frac{1}{2}}$ = $6 \times 9^{-\frac{1}{2}} ()$ $\frac{6}{9^{\frac{1}{2}}}, \frac{6}{3}, 2 \text{ or equivalent}$	M1 B1
	$= \dots \left( 1 + \left( -\frac{1}{2} \right) \left( kx \right); + \frac{\left( -\frac{1}{2} \right) \left( -\frac{3}{2} \right)}{2} \left( kx \right)^2 + \frac{\left( -\frac{1}{2} \right) \left( -\frac{3}{2} \right) \left( -\frac{5}{2} \right)}{3!} \left( kx \right)^3 + \dots \right)$	M1; A1ft
	$= 2\left(1 + \frac{2}{9}x +\right) \qquad \text{or } 2 + \frac{4}{9}x$	A1
	$=2+\frac{4}{9}x+\frac{4}{27}x^2+\frac{40}{729}x^3+\ldots$	A1 (6)
	(b) $g(x) = 2 - \frac{4}{9}x + \frac{4}{27}x^2 - \frac{40}{729}x^3 + \dots$	B1ft (1)
	(c) $h(x) = 2 + \frac{4}{9}(2x) + \frac{4}{27}(2x)^2 + \frac{40}{729}(2x)^3 + \dots$	M1 A1 (2)
	$\left(=2+\frac{8}{9}x+\frac{16}{27}x^2+\frac{320}{729}x^3+\ldots\right)$	[9]

Question Number	Scheme	Marks
4.	$\int y  dy = \int \frac{3}{\cos^2 x}  dx$ Can be implied. Ignore integral signs $= \int 3 \sec^2 x  dx$	B1
	$\frac{1}{2}y^2 = 3\tan x  (+C)$	M1 A1
	$y = 2, x = \frac{\pi}{4}$ $\frac{1}{2}2^2 = 3\tan\frac{\pi}{4} + C$ Leading to	M1
	C = -1 $\frac{1}{2}y^{2} = 3\tan x - 1$ or equivalent	A1 (5) [5]

Question Number	Scheme	Marks
5.	(a) Differentiating implicitly to obtain $\pm ay^2 \frac{dy}{dx}$ and/or $\pm bx^2 \frac{dy}{dx}$	M1
	$48y^2\frac{\mathrm{d}y}{\mathrm{d}x}+\ldots-54\ldots$	A1
	$9x^2y \rightarrow 9x^2\frac{dy}{dx} + 18xy$ or equivalent	B1
	$\left(48y^2 + 9x^2\right)\frac{dy}{dx} + 18xy - 54 = 0$	M1
	$\frac{dy}{dx} = \frac{54 - 18xy}{48y^2 + 9x^2}  \left( = \frac{18 - 6xy}{16y^2 + 3x^2} \right)$	A1 (5)
	(b) $18-6xy = 0$ Using $x = \frac{3}{y}$ or $y = \frac{3}{x}$	M1
	$16y^{3} + 9\left(\frac{3}{y}\right)^{2}y - 54\left(\frac{3}{y}\right) = 0 \text{ or } 16\left(\frac{3}{x}\right)^{3} + 9x^{2}\left(\frac{3}{x}\right) - 54x = 0$ Leading to	M1
	$16y^{4} + 81 - 162 = 0 \qquad \text{or} \qquad 16 + x^{4} - 2x^{4} = 0$ $y^{4} = \frac{81}{16} \qquad \text{or} \qquad x^{4} = 16$	M1
	$y = \frac{3}{2}, -\frac{3}{2}$ or $x = 2, -2$	A1 A1
	Substituting either of their values into $xy = 3$ to obtain a value of the other variable.	M1
	$\left(2,\frac{3}{2}\right),\left(-2,-\frac{3}{2}\right)$ both	A1 (7)
		[12]

Question Number	Scheme	Marks
6.	(a) $\frac{\mathrm{d}x}{\mathrm{d}t} = 2\sqrt{3}\cos 2t$	B1
	$\frac{\mathrm{d}y}{\mathrm{d}t} = -8\cos t\sin t$	M1 A1
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{-8\cos t\sin t}{2\sqrt{3}\cos 2t}$ $4\sin 2t$	M1
	$= -\frac{4\sin 2t}{2\sqrt{3}\cos 2t}$	
	$\frac{\mathrm{d}y}{\mathrm{d}x} = -\frac{2}{3}\sqrt{3}\tan 2t \qquad \left(k = -\frac{2}{3}\right)$	A1 (5)
	(b) When $t = \frac{\pi}{3}$ $x = \frac{3}{2}$ , $y = 1$ can be implied	B1
	$m = -\frac{2}{3}\sqrt{3}\tan\left(\frac{2\pi}{3}\right)  (=2)$	M1
	$y - 1 = 2\left(x - \frac{3}{2}\right)$	M1
	y = 2x - 2	A1 (4)
	(c) $x = \sqrt{3} \sin 2t = \sqrt{3} \times 2 \sin t \cos t$ $x^2 = 12 \sin^2 t \cos^2 t = 12(1 - \cos^2 t) \cos^2 t$	M1
	$x^{2} = 12\left(1 - \frac{y}{4}\right)\frac{y}{4}$ or equivalent	M1 A1 (3)
	( 4)4	[12]
	Alternative to (c) $y = 2\cos 2t + 2$	M1
	$\frac{x^{2}}{3} + \frac{(y-2)^{2}}{4} = 1$	M1 A1 (3)

Question Number	Scheme	Marks
7.	(a) $\begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1
	Area = $\frac{1}{2} \times 1()$ $\approx (0.6931 + 2(1.9605 + 3.1034) + 4.1589)$ $\approx \frac{1}{2} \times 14.97989 \approx 7.49$ 7.49 cao	B1 M1 A1 (4)
	(b) $\int x^{\frac{1}{2}} \ln 2x  dx = \frac{2}{3} x^{\frac{3}{2}} \ln 2x - \int \frac{2}{3} x^{\frac{3}{2}} \times \frac{1}{x}  dx$ $= \frac{2}{3} x^{\frac{3}{2}} \ln 2x - \int \frac{2}{3} x^{\frac{1}{2}}  dx$ $= \frac{2}{3} x^{\frac{3}{2}} \ln 2x - \frac{4}{9} x^{\frac{3}{2}}  (+C)$	M1 A1 M1 A1 (4)
	(c) $\left[\frac{2}{3}x^{\frac{3}{2}}\ln 2x - \frac{4}{9}x^{\frac{3}{2}}\right]_{1}^{4} = \left(\frac{2}{3}4^{\frac{3}{2}}\ln 8 - \frac{4}{9}4^{\frac{3}{2}}\right) - \left(\frac{2}{3}\ln 2 - \frac{4}{9}\right)$ = $(16\ln 2)$ Using or implying $\ln 2^{n} = n\ln 2$ = $\frac{46}{3}\ln 2 - \frac{28}{9}$	M1 M1 A1 (3) [11]

Question Number	Scheme	Marks
8.	(a) $AB = \begin{pmatrix} 8\\3\\4 \end{pmatrix} - \begin{pmatrix} 10\\2\\3 \end{pmatrix} = \begin{pmatrix} -2\\1\\1 \end{pmatrix}$	M1 A1 (2)
	(b) $\mathbf{r} = \begin{pmatrix} 10\\2\\3 \end{pmatrix} + t \begin{pmatrix} -2\\1\\1 \end{pmatrix}$ $\mathbf{r} = \begin{pmatrix} 8\\3\\4 \end{pmatrix} + t \begin{pmatrix} -2\\1\\1 \end{pmatrix}$	M1 A1ft (2)
	(c) $UP = \begin{pmatrix} 10-2t \\ 2+t \\ 3+t \end{pmatrix} - \begin{pmatrix} 3 \\ 12 \\ 3 \end{pmatrix} = \begin{pmatrix} 7-2t \\ t-10 \\ t \end{pmatrix}$	- M1 A1
	$\begin{pmatrix} 7-2t \\ t-10 \\ t \end{pmatrix} \begin{pmatrix} -2 \\ 1 \\ 1 \end{pmatrix} = -14 + 4t + t - 10 + t = 0$ Leading to $t = 4$ $\begin{pmatrix} 10-8 \end{pmatrix} \begin{pmatrix} 2 \end{pmatrix}$	- M1 A1
	Position vector of P is $\begin{vmatrix} 2+4\\3+4 \end{vmatrix} = \begin{vmatrix} 6\\7 \end{vmatrix}$	M1 A1 (6) [10]
	Alternative working for (c)	
	$\operatorname{uur}_{CP} = \begin{pmatrix} 8-2t\\ 3+t\\ 4+t \end{pmatrix} - \begin{pmatrix} 3\\ 12\\ 3 \end{pmatrix} = \begin{pmatrix} 5-2t\\ t-9\\ t+1 \end{pmatrix}$ $(5-2t) \begin{pmatrix} 2 \end{pmatrix}$	- M1 A1
	$ \begin{pmatrix} 3-2t \\ t-9 \\ t+1 \end{pmatrix}, \begin{pmatrix} -2 \\ 1 \\ 1 \end{pmatrix} = -10 + 4t + t - 9 + t + 1 = 0 $	- M1
	Leading to $t=3$	A1
	Position vector of P is $\begin{pmatrix} 8-6\\3+3\\4+3 \end{pmatrix} = \begin{pmatrix} 2\\6\\7 \end{pmatrix}$	- M1 A1 (6)

Further copies of this publication are available from Edexcel Publications, Adamsway, Mansfield, Notts, NG18 4FN

Telephone 01623 467467 Fax 01623 450481 Email <u>publication.orders@edexcel.com</u> Order Code UA031959 Summer 2012

For more information on Edexcel qualifications, please visit our website <u>www.edexcel.com</u>

Pearson Education Limited. Registered company number 872828 with its registered office at Edinburgh Gate, Harlow, Essex CM20 2JE





Llywodraeth Cynulliad Cymru Welsh Assembly Government

