



**GCE**

**Mathematics B (MEI)**

**H640/02: Pure Mathematics and Statistics**

Advanced GCE

**Mark Scheme for June 2019**

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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## Text Instructions

### Annotations and abbreviations

Annotation in scoris	Meaning
✓ and ✕	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction <b>In this question you must show detailed reasoning</b> appears in the question.

**Subject-specific Marking Instructions for A Level Mathematics B (MEI)**

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

**M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

**E**

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.
- When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.
  - When a value is not given in the paper accept any answer that agrees with the correct value to **2 s.f.**

Follow through should be used so that only one mark is lost for each distinct accuracy error.

- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- i If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question		Answer	Marks	AOs		Guidance
1	(a)	$0.2 + 0.1 + k + 2k + 4k [= 1]$ soi [ $k =$ ] 0.1	M1 A1 [2]	1.1a 1.1		
1	(b)	$1 - 2 \times$ their $k$ $0.8$ or $\frac{4}{5}$ cao	M1 A1 [2]	1.1 1.1	$1 -$ their $P(X = 4)$ oe	
2	(a)	$k(x^2 + 5)^{11}$ seen $24x(x^2 + 5)^{11}$	M1 A1 [2]	1.1a 1.1		
2	(b)	$a(x^2 + 5)^{12}$ $2(x^2 + 5)^{12} (+c)$	M1 A1 [2]	1.1 1.1	condone omission of $+c$	A1 FT their $kx(x^2 + 5)^{11}$ from part (a)
3	(a)	2.8 to 2.81 BC	B1 [1]	1.1		NB 2.8063583815029..

Question		Answer	Marks	AOs		Guidance
3	(b)	eg the data is already grouped oe eg we do not have the original raw data oe eg we are using the mid-point of the intervals eg we are assuming the data are uniformly distributed across each interval oe	<b>B1</b>  <b>[1]</b>	<b>2.4</b>		
3	(c)	eg using upper class limit in each case gives mean is 3.4...so it is possible that mean is more than 3	<b>B1</b> <b>[1]</b>	<b>2.3</b>	or eg need 520 or more and using the upper limits gives 590	simply stating eg the mean could be 3.4 is insufficient
4	(a)	$\frac{0.5}{2} [\sqrt{1+(-1)^3} + 2\sqrt{1+(-0.5)^3} + \sqrt{1+0^3}]$ oe  $\sqrt{1+(-0.5)^3}$ soi  0.717707 cao	<b>M1</b>  <b>B1</b>  <b>A1</b> <b>[3]</b>	<b>1.1</b>  <b>1.1</b>  <b>1.1</b>	condone omission of brackets  NB $\frac{\sqrt{14}}{4} = 0.9(35414346693)$  NB $\frac{2+\sqrt{14}}{8}$ unsupported implies <b>M1B1</b>	must be three terms in the bracket  if unsupported allow <b>SC3</b> for 0.717707 and <b>SC2</b> for 0.717707173347 unsupported to 7 or more dp
4	(b)	under-estimate since curve is concave down /convex up oe	<b>B1</b> <b>[1]</b>	<b>2.4</b>	or eg the slant lines of both trapezia are entirely below the curve allow annotated diagram with at least one trapezium	condone eg trapezium below curve allow integral is 0.841309 BC so my answer is an underestimate

Question		Answer	Marks	AOs	Guidance
5	(a)	2.5	<b>B1</b> [1]	<b>1.1</b>	
5	(b)	positive skew cao	<b>B1</b> [1]	<b>1.1</b>	
5	(c)	1	<b>B1</b> [1]	<b>1.1</b>	
6		$k \frac{x^{-4}}{-4} \ln x - \int k \frac{x^{-4}}{-4} \times \frac{1}{x} dx$ oe $[32] \frac{x^{-4}}{-4} \ln x - \int [32] \frac{x^{-4}}{-4} \times \frac{1}{x} dx$ oe $-8x^{-4} \ln x - 2x^{-4} + c$ oe isw	<b>M1</b>  <b>A1</b>  <b>A1</b> <b>A1</b> <b>[4]</b>	<b>3.1a</b>  <b>1.1</b>  <b>1.1</b> <b>1.1</b>	allow sign errors only  all correct  two of three elements correct all three elements correct
7	(a)	$\theta = \frac{72.576}{r^2}$ or $72.576 r^{-2}$ isw	<b>B1</b> [1]	<b>1.1</b>	eg $\frac{9072}{125r^2}$ or $\frac{9072r^{-2}}{125}$
7	(b)	$r\theta + 2r$ or $r(\theta + 2) = 24.48$ seen <b>and</b> $\theta = \frac{24.48 - 2r}{r}$ or equivalent constructive step to give $\frac{24.48}{r} - 2$ <b>AG</b>	<b>B1</b> [1]	<b>1.1</b>	or $2\pi r \frac{\theta}{2\pi} + 2r = 24.48$



Question		Answer	Marks	AOs		Guidance
7	(c)	<p><i>their</i> <math>\frac{2 \times 36.288}{r^2} = \frac{24.48}{r} - 2</math> oe</p> <p><math>r^2 - 12.24r + 36.288 [= 0]</math></p> <p><math>[r =] 5.04</math> or <math>7.2</math> oe</p>	<p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>[3]</b></p>	<p><b>3.1a</b></p> <p><b>2.1</b></p> <p><b>1.1</b></p>	<p>NB 72.576</p> <p>quadratic obtained in form <math>f(r) [= 0]</math></p>	<p>allow <b>B3</b> for 5.04 <b>and</b> 7.2 unsupported</p> <p><b>or</b> allow <b>SC3</b> for obtaining and solving an equation for <math>\theta</math> and then finding both values of <math>r</math></p>
8	(a)	<p>0.4×0.4 or 0.6×0.2 seen</p> <p>0.4×0.4 + 0.6×0.2</p> <p>0.28</p>	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>A1</b></p> <p><b>[3]</b></p>	<p><b>3.1a</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p>	<p>or tree diagram with correct outcomes and probabilities shown</p>	<p>allow 0.4×0.4×0.4 or 0.4×0.6×0.2</p> <p>mark the final answer</p>
8	(b)	<p><math>\frac{1}{120}</math> or <math>\frac{5}{120}</math> seen</p> <p><math>\frac{1}{24}</math> or 0.0416666... to 2 or more sf</p>	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>[2]</b></p>	<p><b>3.1a</b></p> <p><b>1.1</b></p>	<p><b>B2</b> for 0.0416666... unsupported</p> <p><b>B0</b> for 0.042 unsupported</p>	<p>mark the final answer</p>

Question		Answer	Marks	AOs		Guidance
8	(c)	1 – their $\frac{1}{24}$ evaluated	<b>M1</b>	<b>3.1a</b>		
		$1 - \left(\frac{23}{24}\right)^n > 0.95$ FT	<b>M1</b>	<b>2.1</b>	allow use of =, $\geq$ or $\leq$	
		$\left(\frac{23}{24}\right)^n < 0.05$ FT	<b>M1</b>	<b>1.1</b>	allow use of = or $\leq$	
		$n = 71$ cao	<b>A1</b> <b>[4]</b>	<b>2.2a</b>	70.3890...unsupported but rounded to 1 or more dp implies <b>M1M1M1</b>	award full marks for 71 unsupported or from trial and improvement
9	(a)	$(2x + 3 - 1)^2$ or $(2x + 3)^2 - 2(2x + 3) + 1$ seen	<b>M1</b>	<b>1.1</b>	substitution	
		simplified to eg $4(x + 1)^2$ or $4x^2 + 8x + 4$ or $(2x + 2)^2$	<b>A1</b>	<b>1.1</b>	mark the final answer	ignore superfluous work on eg finding roots
		domain is $-1 < x < 0$	<b>B1</b> <b>[3]</b>	<b>1.1</b>	from $2x + 3 > 1$	
9	(b)	$0 < \text{gf}(x) < 4$	<b>B1</b> <b>[1]</b>	<b>1.1</b>		

Question		Answer	Marks	AOs		Guidance
9	(c)	factorise their gf(x) to obtain perfect square or complete the square	<b>M1</b>	<b>3.1a</b>	allow eg $2(x + 1)(2x + 2)$ ; may follow slip eg dividing by 4	or $g^{-1}(x) = \sqrt{x} + 1$ or $f^{-1}(x) = \frac{1}{2}(x - 3)$ for <b>M1</b>
		$y = 4(x + 1)^2$ or $(2x + 2)^2$ oe	<b>A1</b>	<b>2.1</b>	FT	<b>A1</b> for both correct
		$(x + 1) = (\pm)\sqrt{\frac{y}{4}}$ oe	<b>M1</b>	<b>1.1</b>		<b>M1</b> for their $f^{-1}$ (their $\sqrt{x} + 1$ )
		$[(gf)^{-1}(x) =] \sqrt{\frac{x}{4}} - 1$ or $\frac{\sqrt{x}}{2} - 1$ oe	<b>A1</b>	<b>1.1</b>		<b>A1</b> for $(gf)^{-1}(x) = \sqrt{\frac{x}{4}} - 1$ or $\frac{\sqrt{x}}{2} - 1$ oe
		domain is $0 < x < 4$	<b>B1</b> <b>[5]</b>	<b>1.1</b>	FT their (b)	$x$ and $y$ may be interchanged for the first 3 marks but not for the final <b>A1</b>
10	(a)	[=]153	<b>B1</b> <b>[1]</b>	<b>1.1</b>		
10	(b)	$z = \pm 1.645$ used	<b>B1</b>	<b>1.1</b>	or $\pm 1.644(85\dots)$	<b>M0</b> if continuity correction used
		their positive $1.645 = \frac{183 - \text{their } 153}{\sigma}$ oe (= 18.237...to 18.248...)	<b>M1</b>	<b>2.1</b>		
		$\sigma = 18.2$ cao	<b>A1</b>	<b>1.1</b>		
			<b>[3]</b>			

Question		Answer	Marks	AOs		Guidance
10	(c)	$\left[\frac{16}{452} = \right] 0.035(398 \dots)$ their $P(X < 120)$ from $N(\text{their } 153, \text{their } 18.2^2)$ probability of 0.0349 to 0.0352 which agrees to 2 sf	<b>B1</b>  <b>M1</b>  <b>A1</b>  <b>[3]</b>	<b>3.1b</b>  <b>1.1</b>  <b>2.2b</b>	allow percentage  <b>M0</b> if continuity correction used  allow percentage  ..... <b>or B1</b> for their $P(X < 120)$ then <b>M1</b> for $452 \times \text{their } 0.03490..$ then <b>A1</b> for 15.77 to 15.91 which is close to 16 oe ..... <b>or B1</b> as main scheme then <b>M1</b> for $\sigma = \frac{120 - 153}{\text{their } -1.809}$ and $18.3 \approx 18.2$ for <b>A1</b>	or <b>B1</b> as main scheme then Invnorm(0.0353, their 153, their 18.2) for <b>M1</b> <b>NB</b> 119.95 to 120.15 which is close to 120 oe for <b>A1</b>  <b>or B1</b> as main scheme then $z = \frac{120 - \text{their } 153}{\text{their } 18.2}$ for <b>M1</b> <b>NB</b> -1.809 to -1.813 and Invnorm(0.0353, 0, 1) to obtain -1.806 to - 1.812 which is close to -1.809 to -1.813) for <b>A1</b>

Question		Answer	Marks	AOs	Guidance	
10	(d)	$H_0: \mu = \text{their } 153$	<b>B1</b>	<b>1.1</b>	for both hypotheses; may be stated in words, but need to see 153 for <b>B1</b> and <b>population</b> mean for 2 <sup>nd</sup> <b>B1</b>	<b>B0</b> if other parameter used unless clearly defined as population mean  or $z = \frac{143.6 - \text{their } 153}{\frac{\text{their } 18.2}{\sqrt{24}}}$  $z = -2.5248..$ to $-2.5302... \text{ to } 2$ or more dp  their $z$ compared with $-2.326$ or $-2.33$  do not allow eg conclude / prove / indicate or other assertive statement instead of suggest
		$H_1: \mu < \text{their } 153$				
		$\mu$ is the <b>population mean</b> flight time from <b>Magaluf to Liverpool</b>	<b>B1</b>	<b>2.5</b>		
		use of $N(\text{their } 153, \frac{\text{their } 18.2^2}{24})$ to find $P(\bar{X} < 143.6)$	<b>M1*</b>	<b>3.3</b>	or inv Norm(0.01, their 153, $\frac{\text{their } 18.2^2}{24}$ )	
		awrt 0.0057 to 0.0058... to 2 or more sf oe <b>isw</b>	<b>A1</b>	<b>1.1</b>	$\bar{X} < 144$ to 144.4 is critical region	
		their 0.0057 correctly compared with 0.01 oe	<b>M1dep*</b>	<b>3.4</b>	143.6 correctly compared with their 144.36 FT their comparison	
		result is significant or reject $H_0$ or accept $H_1$	<b>A1</b>	<b>1.1</b>	FT their comparison	
there is sufficient evidence to <b>suggest</b> at the 1% level that the <b>mean</b> flight time from <b>Magaluf</b> <b>to Liverpool</b> is less than <b>153</b> / mean flight time from Liverpool to Magaluf	<b>A1</b>	<b>2.2b</b>				
		<b>[7]</b>				

Question		Answer	Marks	AOs		Guidance
<b>10</b>	<b>(e)</b>	<p><b>reduce</b> the value of <math>\mu</math></p> <p><b>increase</b> the value of <math>\sigma</math> or <math>\sigma^2</math></p>	<p><b>B1</b></p> <p><b>B1</b></p> <p><b>[2]</b></p>	<p><b>3.5c</b></p> <p><b>3.5c</b></p>	<p>allow <b>B1</b> for eg use new sample data to calculate new estimate for <math>\sigma</math> or <math>\sigma^2</math></p>	<p>eg take a bigger sample is insufficient</p>
<b>11</b>	<b>(a)</b>	<p>differentiate to obtain <math>2x - 4</math></p> <p><math>+ 1 \times \ln x + x \times \frac{1}{x}</math> oe</p> <p>derivative = 0 oe seen and terms combined</p> <p><math>2x - 3 + \ln x = 0</math> www <b>isw AG</b></p>	<p><b>B1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>A1</b></p> <p><b>[4]</b></p>	<p><b>3.1a</b></p> <p><b>2.1</b></p> <p><b>1.1</b></p> <p><b>2.4</b></p>	<p>use of Product Rule</p> <p>all correct</p>	<p>allow one error</p>

Question		Answer	Marks	AOs		Guidance
11	(b)	any rearrangement to obtain $x = g(x)$ from given derivative = 0	<b>M1*</b>	<b>2.1</b>	allow sign error	eg $x = e^{2x-3}$  need not see subscripts in iterative formula    <b>0</b> for 1.3500 unsupported  trial and improvement does not score  need not see subscripts in iterative formula
		$x = \frac{3 - \ln x}{2}$	<b>A1</b>	<b>1.1</b>	any correct rearrangement	
		use of their $g(x_n) = \frac{3 - \ln x_n}{2}$ to obtain at least two iterates eg 2, 1.1534, 1.4286...	<b>M1dep*</b>	<b>1.1</b>	must see iterates	
		1.3500 cao	<b>A1</b>	<b>2.2a</b>		
		..... <i>Alternatively,</i>				
		$x_{n+1} = x_n - \frac{2x_n - 3 + \ln x_n}{\text{their } \left(2 + \frac{1}{x_n}\right)}$	<b>M1*</b>	<b>2.1</b>	Newton-Rapshon iterative formula seen (not for solving $f(x) = 0$ )	
		use of their N-R formula to obtain $x_1, x_2, \dots$ eg 1.5, 1.34795, 1.34996, .....1.349962	<b>A1</b> <b>M1dep*</b>	<b>1.1</b> <b>1.1</b>	formula all correct must see iterates	
		1.3500 cao	<b>A1</b> <b>[4]</b>	<b>2.2a</b>		

Question		Answer	Marks	AOs		Guidance
12	(a)	$0.94^n < k$ or $0.06^n < k$ seen $k = 0.025$ used in inequality as above 60	<b>M1</b> <b>B1</b> <b>A1</b> <b>[3]</b>	<b>3.4</b> <b>1.1</b> <b>2.2a</b>	NB 59.617.. or 1.311...to 1 or more dp if unsupported implies <b>M1B1</b>	allow = instead of <  60 unsupported or from trial and improvement scores 3



Question		Answer	Marks	AOs	Guidance	
12	(b)	<p><math>H_0 : p = 0.06</math> allow equivalent in words  <math>H_1 : p \neq 0.06</math>  <math>p</math> is the probability that a <b>jaguar</b> chosen at random is a <b>black</b> panther / has <b>black</b> coat</p> <p>use of <math>B(83, 0.06)</math> to obtain <math>P(X \leq K)</math> oe</p> <p><math>\text{cdfBinomial}(83, 0.06, 9) = 0.973</math> to <math>0.97321\dots</math>  or <math>1 - \text{cdfBinomial}(83, 0.06, 9) = 0.02679</math> to <math>0.027</math></p> <p><math>1 -</math> their <math>P(X \leq K)</math> compared with <math>0.025</math> or their <math>P(X \leq K)</math> compared with <math>0.975</math> oe</p> <p>result is not significant or do not reject <math>H_0</math> or reject <math>H_1</math></p> <p>there is insufficient evidence at the 5% level to <b>suggest</b> that the probability that a <b>jaguar</b> selected at random from this population is a <b>black panther</b> is not <math>0.06</math></p>	<p><b>B1</b></p> <p><b>B1</b></p> <p><b>M1*</b></p> <p><b>A1</b></p> <p><b>M1dep*</b></p> <p><b>A1</b></p> <p><b>A1</b></p> <p>[7]</p>	<p><b>1.1</b></p> <p><b>2.5</b></p> <p><b>3.3</b></p> <p><b>1.1</b></p> <p><b>3.4</b></p> <p><b>1.1</b></p> <p><b>2.2b</b></p>	<p><b>or</b> <math>p</math> is the proportion of <b>jaguars</b> that are <b>black</b> panthers / have a <b>black</b> coat</p> <p>not <math>P(X = K)</math></p> <p>or critical region is <math>X \geq 11</math> (ignore lower tail)</p> <p>eg 10 compared with their critical region oe</p> <p>must have the correct probability or correct critical region for the last two <b>A</b> marks</p>	<p>NB <math>P(X \leq 10) = .98927\dots</math></p> <p>for comparison of their <math>P(X &gt; K)</math> with <math>0.025</math> or their <math>P(X \leq K)</math> with <math>0.975</math> or stating whether 10 is in their critical region</p> <p>allow accept <math>H_0</math></p> <p>do not allow eg conclude / prove / indicate or other assertive statement instead of suggest</p>
13	(a)	3	<p><b>B1</b></p> <p>[1]</p>	<b>3.3</b>		

Question		Answer	Marks	AOs		Guidance
13	(b)	$[8 \times 3^4 =] 648$	<b>B1</b> <b>[1]</b>	<b>1.1</b>		
13	(c)	$\frac{8(3^n - 1)}{3 - 1}$ $= 4(3^n - 1)$ or $-4(1 - 3^n)$	<b>B1</b> <b>[1]</b>	<b>3.4</b>	use of formula for sum of gp  mark the final answer	or $4 \times 3^n - 4$
13	(d)	their $4(3^n - 1) = 185\,207$ or $3^n = 46303(.75)$ awrt 9.8 cao  [=] 9	<b>M1</b> <b>A1</b>  <b>A1</b> <b>[3]</b>	<b>3.1a</b> <b>1.1</b>  <b>3.2a</b>	<b>M0</b> for eg $8 \times 3^{n-1}$ no FT available here  not from wrong working	allow use of $<$ or $\leq$ for up to 3 marks allow <b>M1</b> only for use of $>$ or $\geq$ or $3^9 = 19683$ <b>and</b> $3^{10} = 59049$ seen for <b>M1</b> then <b>A1</b> (comparison with 46 303)
13	(e)	unlikely because  eg some of the population will be immune to the virus  eg some of the population will not be exposed to the virus  eg medical intervention  eg extrapolation  eg movement of people in and out of town	<b>B1</b>      <b>[1]</b>	<b>3.5b</b>	any sensible reason	it's unlikely that everyone will be affected oe is insufficient

Question		Answer	Marks	AOs		Guidance
14	(a)	the data was not available for all countries oe	<b>B1</b> <b>[1]</b>	<b>2.4</b>		
14	(b)	use of $Q_1 - 1.5 \times (Q_3 - Q_1)$ and $Q_3 + 1.5 \times (Q_3 - Q_1)$ seen for either set  4.135 < 6.28 and 15.775 > 14.46  0.38 < 3.58 and 18.86 > 14.89	<b>M1</b>  <b>A1</b>  <b>A1</b> <b>[3]</b>	<b>3.1b</b>  <b>1.1</b>  <b>1.1</b>	if <b>A0A0</b> allow <b>SC1</b> for 4.135, 15.775, 0.38 and 18.86 all seen	
14	(c)	22 954 isw	<b>B1</b>  <b>[1]</b>	<b>3.1b</b>	allow 22 955, 22 950 or 23 000	<b>NB</b> $6411776 \times \frac{3.58}{1000}$
14	(d)	there are almost certainly more “old” people in the population oe	<b>B1</b> <b>[1]</b>	<b>2.4</b>		

Question		Answer	Marks	AOs		Guidance
<b>14</b>	<b>(e)</b>	<p>in African countries there is a negative association / relationship between (or negative correlation between the ranks of) median age and crude death rate, but in Europe there seems to be a positive association / relationship between (or positive correlation between the ranks of) median age and crude death rate</p> <p>the “association” / “relationship between” or “correlation between the ranks of” median age and crude death rate (appears to be) stronger in Europe</p>	<p><b>B1</b></p> <p><b>B1</b></p> <p><b>[2]</b></p>	<p><b>2.4</b></p> <p><b>2.4</b></p>	<p>do not allow “negative correlation” and / or “positive correlation”</p> <p>allow <b>B1</b> both relationships are weak oe</p>	<p>comment comparing and contrasting type of relationship in both continents for <b>B1</b>, <b>and</b> one comment comparing and contrasting strength of relationship in both continents for <b>B1</b></p> <p>allow equivalent explanations in words eg as median age increases crude death rates decrease in Africa and similar for Europe</p>

Question		Answer	Marks	AOs		Guidance
15		$\mu = 35$ <b>soi</b>	<b>B1</b>	<b>1.2</b>	by symmetry	may be embedded in $N(35,4^2)$ or $N(35,16)$ <b>M0</b> if continuity corrections used  their 0.7887 must be from use of $N(35, 4^2)$
		$\sigma = 4$ seen	<b>B1</b>	<b>3.1b</b>	$35 - 31 = 4$	
		use of $N(35, 4^2)$ to obtain a value for $P(30 < X < 40)$	<b>M1</b>	<b>2.1</b>		
		[cdfNormal(30, 40, 35, 4) =] 0.788700... BC to 2 or more dp	<b>A1</b>	<b>1.1</b>		
		use of $Y \sim B(50, \text{their } 0.7887)$ to find $P(Y \leq K)$ or $P(Y \geq K)$	<b>M1</b>	<b>3.1b</b>	eg cdfBinomial(50,0.7887,45,50)	
	$[1 - P(Y \leq 44)] = 0.032$ to $0.034$ BC	<b>A1</b>	<b>1.1</b>			
			<b>[6]</b>			

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