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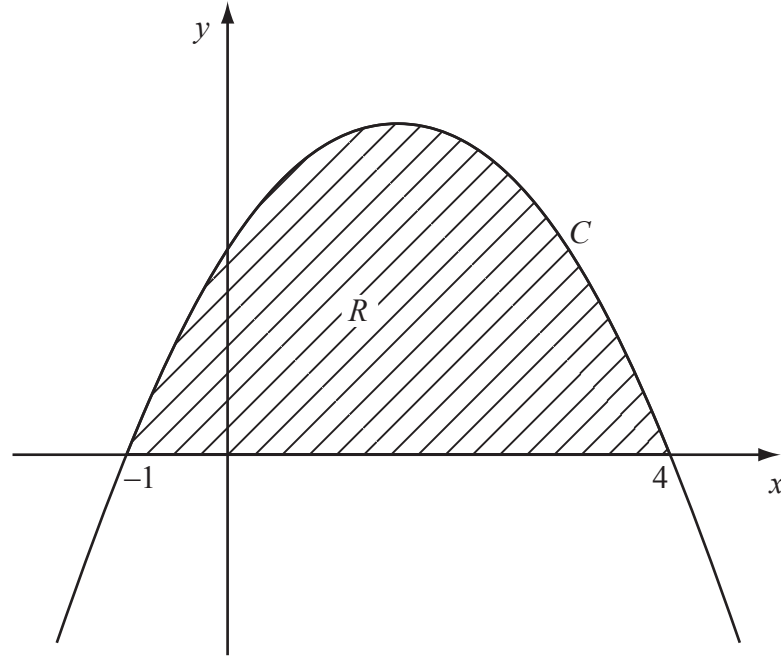


Figure 1

Figure 1 shows part of the curve C with equation $y = (1+x)(4-x)$.

The curve intersects the x -axis at $x = -1$ and $x = 4$. The region R , shown shaded in Figure 1, is bounded by C and the x -axis.

Use calculus to find the exact area of R .

(5)



Question 2 continued

Lined area for writing the answer to Question 2 continued.

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Q2

(Total 5 marks)



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3.

$$y = \sqrt{10x - x^2}$$

(a) Complete the table below, giving the values of y to 2 decimal places.

x	1	1.4	1.8	2.2	2.6	3
y	3	3.47			4.39	

(2)

(b) Use the trapezium rule, with all the values of y from your table, to find an approximation

for the value of $\int_1^3 \sqrt{10x - x^2} \, dx$.

(4)



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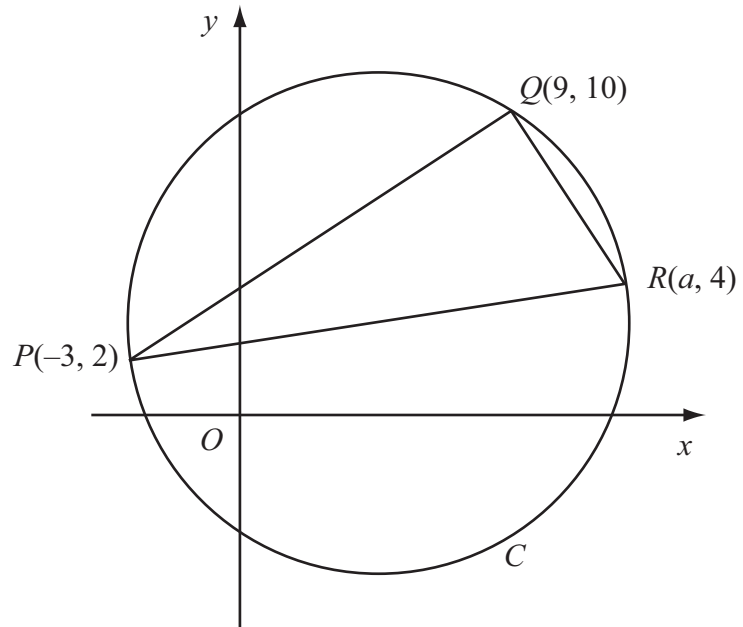


Figure 2

The points $P(-3, 2)$, $Q(9, 10)$ and $R(a, 4)$ lie on the circle C , as shown in Figure 2. Given that PR is a diameter of C ,

(a) show that $a = 13$, (3)

(b) find an equation for C . (5)



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6. $f(x) = x^4 + 5x^3 + ax + b,$

where a and b are constants.

The remainder when $f(x)$ is divided by $(x - 2)$ is equal to the remainder when $f(x)$ is divided by $(x + 1)$.

(a) Find the value of a . **(5)**

Given that $(x + 3)$ is a factor of $f(x)$,

(b) find the value of b . **(3)**



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7.

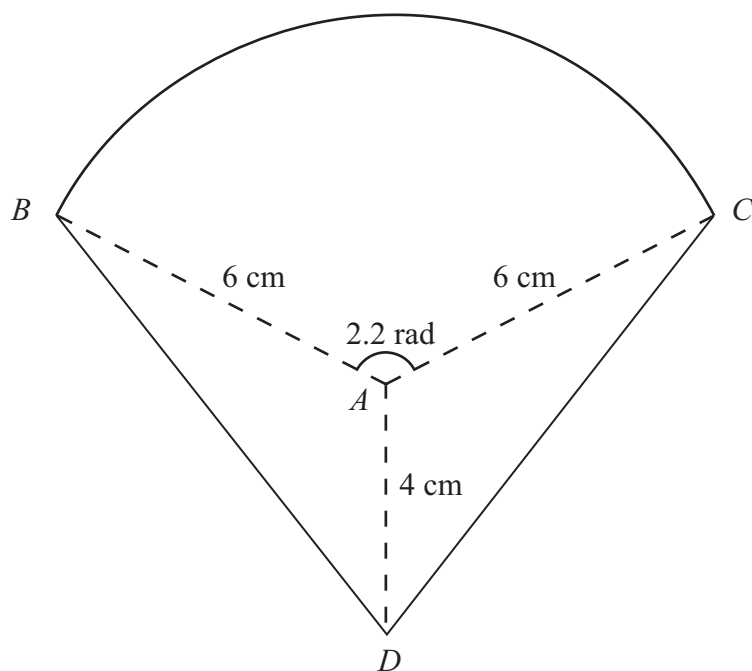


Figure 3

The shape BCD shown in Figure 3 is a design for a logo.

The straight lines DB and DC are equal in length. The curve BC is an arc of a circle with centre A and radius 6 cm. The size of $\angle BAC$ is 2.2 radians and $AD = 4$ cm.

Find

- (a) the area of the sector BAC , in cm^2 , (2)
- (b) the size of $\angle DAC$, in radians to 3 significant figures, (2)
- (c) the complete area of the logo design, to the nearest cm^2 . (4)



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10. A solid right circular cylinder has radius r cm and height h cm.

The total surface area of the cylinder is 800 cm^2 .

(a) Show that the volume, $V \text{ cm}^3$, of the cylinder is given by

$$V = 400r - \pi r^3. \qquad \qquad \qquad \mathbf{(4)}$$

Given that r varies,

(b) use calculus to find the maximum value of V , to the nearest cm^3 . **(6)**

(c) Justify that the value of V you have found is a maximum. **(2)**



