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Edexcel

Mark Scheme

Summer 2023

Pearson Edexcel GCE

In Mathematics (9MA0)

Paper 31 Statistics

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## EDEXCEL GCE MATHEMATICS

### General Instructions for Marking

1. The total number of marks for the paper is 50.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.

### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod – benefit of doubt
- ft – follow through
- the symbol  $\checkmark$  will be used for correct ft
- cao – correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw – ignore subsequent working
- awrt – answers which round to
- SC: special case
- oe – or equivalent (and appropriate)
- dep – dependent
- indep – independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- $\square$  The second mark is dependent on gaining the first mark

4. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.

5. Where a candidate has made multiple responses and indicates which response they wish to submit, examiners should mark this response.

If there are several attempts at a question which have not been crossed out, examiners should mark the final answer which is the answer that is the most complete.

6. Ignore wrong working or incorrect statements following a correct answer.

7. Mark schemes will firstly show the solution judged to be the most common response expected from candidates. Where appropriate, alternatives answers are provided in the notes. If examiners are not sure if an answer is acceptable, they will check the mark scheme to see if an alternative answer is given for the method used.

## General Principles for Mechanics Marking

*(But note that specific mark schemes may sometimes override these general principles)*

- Rules for M marks: correct no. of terms; dimensionally correct; all terms that need resolving (i.e. multiplied by cos or sin) are resolved.
- Omission or extra  $g$  in a resolution is an accuracy error not method error.
- Omission of mass from a resolution is a method error.
- Omission of a length from a moments equation is a method error.
- Omission of units or incorrect units is not (usually) counted as an accuracy error.
- DM indicates a dependent method mark i.e. one that can only be awarded if a previous specified method mark has been awarded.
- Any numerical answer which comes from use of  $g = 9.8$  should be given to 2 or 3 SF.
- Use of  $g = 9.81$  should be penalised once per (complete) question.  
N.B. Over-accuracy or under-accuracy of correct answers should only be penalised *once* per complete question. However, premature approximation should be penalised every time it occurs.
- Marks must be entered in the same order as they appear on the mark scheme.
- In all cases, if the candidate clearly labels their working under a particular part of a question i.e. (a) or (b) or (c),.....then that working can only score marks for that part of the question.
- Accept column vectors in all cases.
- Misreads – if a misread does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, bearing in mind that after a misread, the subsequent A marks affected are treated as A ft
- Mechanics Abbreviations

M(A) Taking moments about A.

N2L Newton's Second Law (Equation of Motion)

NEL Newton's Experimental Law (Newton's Law of Impact)

HL Hooke's Law

SHM Simple harmonic motion

PCLM Principle of conservation of linear momentum

RHS, LHS Right hand side, left hand side

Qu 1	Scheme	Marks	AO
(a)	$[0.13 + 0.25 = ]$ <b><u>0.38</u></b>	B1 (1)	1.1b
(b)	Independence implies: e.g. $[P(B \cap C) = P(B) \times P(C) \Rightarrow] 0.3 = (0.3 + 0.05 + 0.25) \times (0.3 + p)$ So $p = \underline{0.2}$ [Sum of probabilities = 1 gives] $q = \underline{0.07}$	M1 A1 B1ft (3)	1.1b 1.1b 1.1b
(c)	$[P(A B') = ] \frac{P(A \cap B')}{P(B')} \text{ or } \frac{0.13}{(1-0.6) \text{ or } (0.13 + "0.2" + "0.07")}$  $= \frac{13}{40} \text{ or } \underline{0.325}$	M1  A1 (2)	1.1b  1.1b
<b>Notes</b>			
(a)	B1 for 0.38 (or exact equivalent)		
<b>If answers are given on Venn Diagram <u>and</u> in the script then the script takes precedence.</b>			
(b)	M1 for a correct equation in $p$ or $P(C)$ only. May be implied by an answer of $p = 0.2$ <b>provided</b> this does not come from incorrect working. Condone missing brackets if they get 0.2 Other rules for independence will give simple rearrangements of this equation.		
<b>Beware</b>	If $p = 0.2$ comes from incorrect working, we've seen $p = \frac{0.6}{0.3} = 0.2$ , score M0A0		
	A1 for $p = 0.2$ (or exact equivalent) B1ft for $q = 0.07$ (or exact equivalent) ft their $p$ i.e. $q = 0.27 - "0.2"$ where $0 \leq p \leq 0.27$		
(c)	M1 for a correct ratio of probability expressions <u>or</u> a correct ratio of probabilities ft their values of $p$ and $q$ (provided both probabilities) <u>or</u> letters $p$ and $q$ A1 for 0.325 or exact equivalent. Correct answer only will score 2/2 <b>NB on open this is labelled M1 but treat it as A1</b>		

Qu 2	Scheme	Marks	AO
(a)	Comment in context about either <b>independence</b> or <b>random</b> packing e.g. “ <u>prizes must be placed in packets at random/independently</u> of each other” <b>or</b> about <b>constant probability</b> e.g. “the <u>probability</u> of a <u>packet</u> containing a <u>prize</u> is <u>constant/ the same/fixed</u> ”	B1 (1)	3.5b
(b)(i)	$[P(T = 6) = ]$ 0.17273... awrt <b>0.173</b>	B1	1.1b
(ii)	$[P(T < 3) = P(T \leq 2) = ]$ 0.061587... awrt <b>0.0616</b>	B1 (2)	1.1b
(c)	$[K = \text{no. of boxes with fewer than 3 packets containing a prize}]$ $K \sim B(5, \text{“0.0616”})$ $P(K = 2) = 0.031344...$ in the range <b>[0.0313~0.0314]</b>	M1 A1 (2)	1.1b 1.1b
(d)	$H_0 : p = \frac{1}{7}$ $H_1 : p < \frac{1}{7}$ $[X = \text{no of packets containing a prize}] X \sim B(110, \frac{1}{7})$ $[P(X \leq 9)] = 0.038292...$ $[\text{Significant result or reject } H_0]$ E.g. there <u>is</u> evidence to <u>support</u> Kamil’s <u>claim</u>	B1 M1 A1 A1 (4)	2.5 3.3 3.4 2.2b
		<b>( 9 marks)</b>	
<b>Notes</b>			
(a)	B1 <b>May use idea of independent events:</b> a suitable reason, <b>in context</b> , covering idea of <u>random</u> packing or packets filled <u>independently</u> . Should mention key words/ideas of: <u>prizes in packets</u> <b>or</b> <u>packets in boxes</u> <b>May use idea of constant probability.</b> Must see key words underlined in scheme. Idea of probability with “independence” or “not affected by other packets” is B0 B0 for: <b>Idea of only 2 cases.</b> E.g. <u>Packet</u> contains a <u>prize</u> or not <b>or</b> <b>Idea of a fixed number of trials.</b> E.g. Need a <u>fixed</u> number of <u>packets</u> in each <u>box</u>		
(b)(i)	B1 for awrt 0.173		
(ii)	B1 for awrt 0.0616		
(c)	M1 for sight of $B(5, \text{“0.0616”})$ <b>or</b> ${}^5C_2 (\text{“0.0616”})^2 (1 - \text{“0.0616”})^3$ ft their answer to (b)(ii). A1 for an answer in the range [0.0313 to 0.0314] Use of 0.0616 gives 0.031356..ans only 2/2		
(d)	B1 for both hypotheses correct in terms of $p$ or $\pi$ M1 for selecting an appropriate model, may be implied by 1 <sup>st</sup> A1 or $P(X = 9) = 0.0199(2...)$ 1 <sup>st</sup> A1 for 0.038 or better <b>or</b> allow 0.04 with sight of $P(X \leq 9)$		
<b>ALT</b>	<b>Critical Region.</b> Allow CR of $X \leq 9$ (or $X < 10$ ) provided a supporting probability is seen e.g. A1 for correct CR plus $P(X \leq 10) = 0.0718...$ (accept 2sf or 1sf if prob statement seen) 2 <sup>nd</sup> A1 (dep on 1 <sup>st</sup> A1 but indep of hyp’s) for a suitable conclusion in context that suggests <u>support</u> for (Kamil’s) <u>claim</u> <b>or</b> states that there is evidence that <u>proportion</u> / <u>probability/chance</u> of packets containing a <u>prize</u> is less than $\frac{1}{7}$		
<b>Normal</b>	Do not award 2 <sup>nd</sup> A1 for contradictory statements e.g. “not significant” so “supports claim” Sight of $N\left(\frac{110}{7}, \frac{660}{49}\right)$ <b>or</b> awrt 13.5 <b>or</b> probability of 0.045(20.) <b>or</b> 0.033(66..) scores M1		



Qu 3	Scheme	Marks	AO
(a)	Need to replace tr with a numerical value Value of tr is between 0 and 0.05 suggest using e.g 0.025 , 0 <u>or</u> value ,, 0.05	M1 A1 (2)	1.2 1.1b
(b)(i)	$\left[ \bar{x} = \frac{389.3 \sim 390.8}{184} \right] = 2.119\dots$ awrt <b>2.12</b> allow $\frac{195}{92}$ or $2\frac{11}{92}$	B1	1.1b
(ii)	$[\sigma =] \sqrt{\frac{(\text{awrt})4336}{184} - \bar{x}^2}$ <u>or</u> allow $[\sigma^2 =] \frac{(\text{awrt})4336}{184} - \bar{x}^2$ <u>or</u> awrt 19.1 = 4.367... awrt <b>4.37</b>	M1 A1 (3)	1.1b 1.1b
(c)(i)	Only covers May~Oct (so not a suitable sample)	B1	1.1b
(ii)	e.g. Winter months are <u>missing</u> when we'd expect <u>more rain</u> so expect estimate in (b)(i) to be an <u>underestimate</u> (oe)	B1 (2)	2.4
		<b>( 7 marks)</b>	
<b>Notes</b>			
(a)	M1 for recognising that tr must be replaced (oe) with a numerical value The following examples would score M0: The tr values are worth 0 so ignore (not replacing) <u>or</u> must remove outliers <u>or</u> fill gaps in table <u>or</u> make widths the same <u>or</u> need to find mid-points A1 for using a suitable value: e.g. 0.025 (or allow 0) i.e. any value in [0, 0.05] (these give $\sum x = 390$ (3sf), use of 0.05 gives 390.8, use of 0 gives 389.3 allow in (b)(i))		
(b)(i)	B1 for awrt 2.12 <u>or</u> allow simplified fraction or mixed number. B0 for $\frac{390}{184}$		
(ii)	M1 for a correct expression for standard deviation <b>or</b> variance. Allow $\sum x^2 = \text{awrt } 4336$ Ignore their label $\sigma$ or $\sigma^2$ Can fit their mean A1 for awrt 4.37 [Use of $s$ gives 4.3791... so for correct use seen allow awrt 4.38]		
SC	Using $n = 155$ Allow M1 for expression $[\sigma =] \sqrt{\frac{(\text{awrt})4336}{155} - \bar{x}^2} = \sqrt{21.64\dots}$ or 4.65...		
<b>Part (c) can effectively be marked together.</b>			
(c)(i)	B1 for a comment mentioning that data is just from May~Oct (so not representative of the whole year). Just saying "only 184 days so not representative" is B0, <b>must mention May ~ Oct</b>		
(ii)	B1 for comment that <u>missing/winter</u> months expected to have more rain (oe) <b>and</b> "underestimate"(oe) We are looking for all 3 of these ideas here: 1. A statement or implication that missing data is from winter or different months. 2. A suggestion about the rainfall in these months (probably more rain). 3. A statement about the impact on the estimate in (b)(i) <u>equivalent</u> to saying it would be an underestimate or the (actual) mean will be higher.		
SC	If you see "Leeming or N or NE has <u>less</u> rain in winter months" – please send to review		

Qu 4	Scheme	Marks	AO
(a)	[Let $N =$ height from region A; $P(N > 180) = ] 0.24937... \text{ awrt } \underline{0.249}$	B1	1.1b
(b)	$H_0 : \mu = 175.4 \quad H_1 : \mu \neq 175.4$ [ $S =$ height from region B] $\bar{S} \sim N\left(175.4, \frac{6.8^2}{52}\right)$ Allow $\sigma^2 =$ awrt 0.889 [ $P(\bar{S} > 177.2)] = 0.02814... \dots$ [0.028... $> 0.025$ , Not sig, do not reject $H_0$ ] <u>Insufficient</u> evidence to <u>support</u> student's <u>claim</u>	B1 M1 A1 A1	1.1b 2.5 3.3 3.4 2.2b
(c)	[ $p$ -value = $2 \times 0.02814... = ] 0.05628... \dots$ in range <u>0.056~0.06</u> or <u>5.6(%)~6(%)</u>	B1ft	1.2
		(1)	
<b>( 6 marks)</b>			
<b>Notes</b>			
(a)	B1 for awrt 0.249		
(b)	B1 for both hypotheses correct in terms of $\mu$ ( <b>See below for one-tail test</b> ) M1 for selecting the correct model, may be implied by standardisation using correct values <u>or</u> may be implied by a correct <u>value</u> in 1 <sup>st</sup> A1 e.g.(Prob =) 0.028 or awrt 0.972, ( $Z =$ ) 1.9(08..) (CV=) 177.25 Condone use of $S$ (or any other letter) instead of $\bar{S}$ Condone use of $\bar{S} \sim N\left(177.2, \frac{6.8^2}{52}\right)$ but <b>this will lose 2<sup>nd</sup> A mark</b>		
ALT	1 <sup>st</sup> A1 for probability of awrt 0.028 (allow 0.03 if $P(\bar{S} > 177.2)$ is seen) Condone $1 - 0.02814 \dots = 0.9718...(\text{awrt } 0.972)$ <b>only if clearly compared with 0.975</b> Allow $Z = 1.9(088...)$ <u>and</u> comparison with 1.96 (or better: calc gives 1.95996...) <u>or</u> CR of $[\bar{S}] \dots 177.248...(\text{awrt } 177.25)$ Allow $[\bar{S}] > 177.248...(\text{awrt } 177.25)$ Implied by diagram or correct interpretation of inequality with their CV (Ignore any attempt at a lower CR for $\bar{S}$ )		
	2 <sup>nd</sup> A1 (dep on 1 <sup>st</sup> A1 and use of correct model. Use of $N(177.2, \dots)$ scores A0) for a conclusion using context: e.g. does <u>not support</u> student's <u>claim</u> <u>or</u> e.g. <u>insufficient</u> evidence of a <u>difference in heights</u> Do not allow 2 <sup>nd</sup> A mark for contradictory statements e.g. "significant" so "no support for claim"		
(c)	B1ft for answer in range 0.056~0.06 or 5.6%~6% (Ranges are inclusive, condone missing %) (can ft their probability, provided $< 0.5$ , from part (b) but not 0.025 leading to 5%)		
NB	<b>One-tail test [Max of 3/5 for (b) and (c)]</b> In (b) B0 (hypotheses) M1(model as above) 1 <sup>st</sup> A1[for probability <u>or</u> $Z$ compared with 1.6449 <u>or</u> CR $[\bar{S}] \dots$ or $> 176.95... (\text{awrt } 177)]$ 2 <sup>nd</sup> A1 for conclusion in context that <u>supports claim</u> <b>or</b> " <u>heights</u> of men from $B$ is <u>different from/greater than</u> from $A$ " In (c) B0		

Qu 5	Scheme	Marks	AO
(a)	$P(S \cap \{X = 50\}) = P(S \cap \{X = 80\}) [= a \text{ constant, } V] \Rightarrow b \times \frac{k}{50} = c \times \frac{k}{80}$	M1	3.1a
	May see: $\frac{k}{50} = \frac{V}{b}$ <u>and</u> $\frac{k}{80} = \frac{V}{c}$ (condone any <u>letter</u> for $V$ even $S$ )		
	So $c = \frac{8}{5}b$ *	A1cso*	1.1b
		(2)	
(b)	$d = 2b$ <b>or</b> $a = \frac{2}{5}b$ <b>or</b> $c = 4a$ <b>or</b> $d = 5a$ <b>or</b> $d = \frac{5}{4}c$	M1 A1	2.1 3.3
	$\frac{2}{5}b + b + \frac{8}{5}b + 2b = 1$	M1	2.1
	$\Rightarrow 5b = 1$ so $b = \frac{1}{5}$ (o.e.)	A1	1.1b
	$\underline{\underline{a = \frac{2}{25} \quad b = \frac{1}{5} \quad c = \frac{8}{25} \quad d = \frac{2}{5}}}$	A1	3.2a
	(5)		
(c)	[Experiment suggests for Nav] $P(S   \{X = 100\}) = 0.3 \Rightarrow k = 30$		
	<b>or</b> $0.3 = \frac{V}{0.4} \Rightarrow V = 0.12$		
	So model won't work since	B1	2.4
	$P(S   X = 20) = \frac{30}{20}$ <u>or</u> $\frac{0.12}{0.08}$ and so would be greater than 1		
	(1)		
	(8 marks)		
<b>Notes</b>			
(a)	M1 for use of $P(S   X = x) \times P(X = x)$ for $x = 50$ <u>and</u> $x = 80$ (Must see $k$ or their $V$ ) Any expression or equation <b>MUST</b> be based on the probability statements in qu.		
* NB	A1cso for rearranging to required result, no incorrect work seen, condone poor notation Use of values e.g. $b = \frac{50}{20 + 50 + 80 + 100}$ to prove (a) is M0A0 but scores 2 <sup>nd</sup> M1A1 in (b)		
	<b>Marks for (b) may be awarded for work seen in (a)</b>		
(b)	1 <sup>st</sup> M1 for at least one other relationship (either probability the subject) from the list. 1 <sup>st</sup> A1 for a second different relationship (either probability the subject) from the list. <u>or</u> Allow for: $\frac{ak}{20} = \frac{bk}{50} = \frac{ck}{80} = \frac{dk}{100}$ for 1 <sup>st</sup> M1 1 <sup>st</sup> A1		
	2 <sup>nd</sup> M1 for using or stating sum of prob's = 1 May be implied by one correct probability. 2 <sup>nd</sup> A1 for one correct probability e.g. $b = \frac{1}{5}$ or exact equivalent such as 0.2 3 <sup>rd</sup> A1 for all correct probabilities. Allow exact equivalents e.g. $c = 0.32$		
	<b>Sight of correct distribution or list of probs with no obvious incorrect working is 5/5</b>		
(c)	B1 for deducing $k = 30$ <b>and</b> giving a suitable example to show model breaks down		

Qu 6	Scheme	Marks	AO
(a)	$2 \times 4.2, 4 \times 4, 4 \times 3.5, 10 \times 1$ ( $= 8.4 + 16 + 14 + 10 = 48.4$ ) [So $P(10 < T < 30) = ] \left[ \frac{48.4}{90} \right] = \frac{121}{225} = 0.53777\dots$ <b>0.53~0.54</b> (2sf OK)	M1 A1	1.1b 1.1b
(b)	(Not suitable as) data is not symmetric <u>or</u> is skew (normal is symmetric) ("Even" distribution or a diagram <u>on its own</u> is not enough so B0)	(2) B1 (1)	2.4
(c)	$\int xe^{-x} (dx) = \int xd(-e^{-x})$ $= [-xe^{-x}] - \int(-e^{-x}) (dx) (+c)$ $\int_0^n xe^{-x} (dx) = [-xe^{-x} - e^{-x}]_0^n = (-ne^{-n} - e^{-n}) - [-(0) - 1]$ $= 1 - (n+1)e^{-n} (*)$	M1 A1 dM1 A1cso*	2.1 1.1b 1.1b 1.1b
(d)	Require area = 90 i.e. $k \int_{(0)}^{(n)} xe^{-x} dx = 90$ (ignore limits) Using the result in part (c) with $n = 4$ gives $k[1 - 5e^{-4}] = 90$ ( $k =$ ) <b>99(.0729\dots)</b> (*)	M1 M1 A1cso*	3.1a 2.1 1.1b
(e)(i)	[ $P(10 < T < 30) = ]$ 0.64863... awrt <b>0.649</b>	B1	1.1b
(ii)	[No. of patients =] $(99) \left[ (1 - 4e^{-3}) - (1 - 2e^{-1}) \right]$ ( $= 53.1\dots$ ) Prob = $\frac{0.5366\dots \times 99}{90} = 0.59027\dots$ [or 0.5907...] = awrt <b>0.590 or 0.591</b>	M1 A1	3.4 3.2a
(f)	eg Patients might stay longer than 40 hours (Can ignore other comments unless clearly contradictory.)	B1	3.5b
		<b>( 14 marks)</b>	
<b>Notes</b>			
(a)	M1 for an attempt to find the number between 10 and 30 ( 2 correct products or 48 or 48.4 seen) A1 for 2sf answer in [0.53 ~ 0.54] NB use of 48 gives 0.5333... [Correct ans implies 2/2]		
(b)	B1 for a comment suggesting not suitable based on (lack of) symmetry <u>or</u> "not bell shaped"		
(c)	1 <sup>st</sup> M1 for attempting integration by parts in right direction. Must have $u = x$ and $v = \pm e^{-x}$ 1 <sup>st</sup> A1 for a correct first step, correct first integration and expression for second integral 2 <sup>nd</sup> dM1 (dep on 1 <sup>st</sup> M1) for all integration attempted and some use of at least one limit * 2 <sup>nd</sup> A1 for cso with no incorrect working seen. Minimum is correct int and use of limits seen.		
(d)	1 <sup>st</sup> M1 for realising need area under the curve (implied by the integral) = 90 2 <sup>nd</sup> M1 for use of (c) with $n = 4$ and set = 90 May be implied by sight of 99.07... or better * A1cso for $k = 99$ or awrt 99.1 <b>NB</b> Allow use of $k = 99$ and show area = awrt 89.9 with a conclusion to score 3/3		
(e)(i)	B1 for awrt 0.649		
(ii)	M1 for use of (c) with $n = 1$ and $n = 3$ Don't need the 99. Implied by sight of awrt 0.54 A1 for awrt 0.590 or awrt 0.591 Allow 0.59 from correct working seen.		
(f)	B1 eg for comment, in context, about the upper limit for <u>time</u> ( $t$ or $x$ )(time/hour may be implied)		

**Notes on Question 5**

The question essentially uses the definition of  $P(A | B)$  given in the formula booklet.

$$\text{In particular } P(S | \{X = x\}) = \frac{P(S \cap \{X = x\})}{P(X = x)} \quad \boxed{1}$$

The first "blob" tells us that  $P(S | \{X = x\}) = \frac{k}{x}$  where  $k$  is a constant.

The second "blob" tells us that  $P(S \cap \{X = x\})$  is the same for all  $x$  so  $P(S \cap \{X = x\}) = V$  where  $V$  is a constant.

$$\text{Using these results in } \boxed{1} \text{ gives } \frac{k}{x} = \frac{V}{P(X = x)} \quad \boxed{2}$$

Line 1 of MS for part (a) uses  $V = P(X = x) \times \frac{k}{x}$  for  $x = 50$  and  $x = 80$

Line 2 of MS for part (a) uses  $\boxed{2}$  with  $x = 50$  and  $x = 80$

**Other implications**

$$\text{Equation } \boxed{1} \text{ can be rearranged to give } P(X = x) = x \times \frac{V}{k} \quad \boxed{3}$$

$$\text{So when } a + b + c + d = 1 \text{ is used this gives } 1 = \frac{V}{k}(20 + 50 + 80 + 100) \text{ or } \frac{V}{k} = \frac{1}{250} \quad \boxed{4}$$

In particular if we use this relationship in  $\boxed{3}$  the probabilities  $a, b, c$  and  $d$  can simply be written down for example  $b = \frac{50}{250}$  as given in the **NB** in the notes on the MS.

The point is that  $k$  and  $V$  will vary according to equation  $\boxed{4}$  but as part (c) shows there are some restrictions on the values  $k$ , and therefore  $V$ , can take.

Since  $\frac{k}{x}$  is a probability then, ignoring the trivial cases\*,  $0 < \frac{k}{x} < 1$  and the "restricting" value of  $x$  is

$$\text{clearly } x = 20 \text{ so } 0 < k < 20 \text{ and from } \boxed{4} \text{ we get } 0 < V < \frac{20}{250} = \frac{2}{25} = a$$

So the restrictions on  $k$  and on  $V$  are given by the shortest distance and its associated probability.

\*  $k = 0$  would say Tisam can never get the ball in the cup no matter what the distance.

$k = 20$  says she always gets the ball in the cup for any distance.





**Pearson**  
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Mark Scheme

Summer 2023

Pearson Edexcel GCE

In Mathematics (9MA0)

Paper 32 Mechanics

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## EDEXCEL GCE MATHEMATICS

### General Instructions for Marking

1. The total number of marks for the paper is 50.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.

### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod – benefit of doubt
  - ft – follow through
  - the symbol  $\checkmark$  will be used for correct ft
  - cao – correct answer only
  - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
  - isw – ignore subsequent working
  - awrt – answers which round to
  - SC: special case
  - oe – or equivalent (and appropriate)
  - dep – dependent
  - indep – independent
  - dp decimal places
  - sf significant figures
  - \* The answer is printed on the paper
  - The second mark is dependent on gaining the first mark
4. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
  5. Where a candidate has made multiple responses and indicates which response they wish to submit, examiners should mark this response.  
If there are several attempts at a question which have not been crossed out, examiners should mark the final answer which is the answer that is the most complete.
  6. Ignore wrong working or incorrect statements following a correct answer.

7. Mark schemes will firstly show the solution judged to be the most common response expected from candidates. Where appropriate, alternative answers are provided in the notes. If examiners are not sure if an answer is acceptable, they will check the mark scheme to see if an alternative answer is given for the method used.

### General Principles for Mechanics Marking

*(But note that specific mark schemes may sometimes override these general principles)*

- Rules for M marks: correct no. of terms; dimensionally correct; all terms that need resolving (i.e. multiplied by cos or sin) are resolved.
- Omission or extra  $g$  in a resolution is an accuracy error not method error.
- Omission of mass from a resolution is a method error.
- Omission of a length from a moments equation is a method error.
- Omission of units or incorrect units is not (usually) counted as an accuracy error.
- DM indicates a dependent method mark i.e. one that can only be awarded if a previous specified method mark has been awarded.
- Any numerical answer which comes from use of  $g = 9.8$  should be given to 2 or 3 SF.
- Use of  $g = 9.81$  should be penalised once per (complete) question.

N.B. Over-accuracy or under-accuracy of correct answers should only be penalised *once* per complete question. However, premature approximation should be penalised every time it occurs.

- Marks must be entered in the same order as they appear on the mark scheme.
- In all cases, if the candidate clearly labels their working under a particular part of a question i.e. (a) or (b) or (c),.....then that working can only score marks for that part of the question.
- Accept column vectors in all cases.
- Misreads – if a misread does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, bearing in mind that after a misread, the subsequent A marks affected are treated as A ft
- Mechanics Abbreviations

M(A) Taking moments about A.

N2L Newton's Second Law (Equation of Motion)

NEL Newton's Experimental Law (Newton's Law of Impact)

HL Hooke's Law

SHM Simple harmonic motion

PCLM Principle of conservation of linear momentum

RHS, LHS Right hand side, left hand side

Question	Scheme		Marks	AOs
1(a)	16 ( m s <sup>-1</sup> ) seen as the answer		B1	1.1b
			(1)	
1(b)	$s = \frac{1}{2} \times 3.2 \times 5^2$ OR $s = \frac{(0+16)}{2} \times 5$ OR $s = (16 \times 5) - \frac{1}{2} \times 3.2 \times 5^2$ OR $16^2 = 2 \times 3.2 \times s$ OR from a v-t graph, $s = \frac{1}{2} \times 5 \times 16$		M1	3.1b
	s = 40 (m)		A1	1.1b
			(2)	
<b>(3 marks)</b>				
<b>Notes:</b>				
1a	B1	cao. Must be positive. Ignore any working.		
1b	M1	Complete method to find an equation in s only, possibly using their '16' Allow 'reversed motion': use of $s = vt - \frac{1}{2}at^2$ with $v = 0$ i.e. $s = -\frac{1}{2} \times 3.2 \times 5^2$ can score M1 and $s = -40$ so distance is 40 (m) can score the A1		
	A1	cao. Must be positive.		
		<b>N.B.</b> correct answer only, in (b), can score both marks.		

Question	Scheme		Marks	AOs
2(a)	Resolve vertically, $R = 5g = 49$ (N)		B1	1.1b
			(1)	
2(b)	Equation of motion: $28 - F = 5 \times 1.4$		M1	3.1a
	$F = 21$		A1	1.1b
			(2)	
2(c)	$\mu = 0.43$ (2sf required)		B1 ft	3.4
			(1)	
<b>(4 marks)</b>				
<b>Notes:</b>				
2a	B1	Allow either $5g$ or $49$ . No penalty for using $g = 9.81$ or $10$ . Ignore any working. Must be a positive number. B0 if $m$ is involved. <b>N.B.</b> Could be seen on a diagram, provided it's clearly the reaction.		
2b	M1	Equation with correct terms, dimensionally correct, condone sign errors.		
	A1	cao but allow $\frac{15g}{7}$ . Ignore units.		
2c	B1ft	$\mu = \frac{\text{their (b)}}{\text{their (a)}}$ . <b>Answer must be a positive number given to 2sf.</b> <b>N.B.</b> B0 if they use $g = 9.81$ or $10$ in this part of the question. Do not allow restarts. Allow $\mu > 1$ .		

Question	Scheme		Marks	AOs
3(a)	7i – 3j seen or implied by Pythagoras		B1	1.1b
	Use Pythagoras: $\sqrt{7^2 + (-3)^2}$		M1	3.1a
	$\sqrt{58}$ , 7.6 or better ( m s <sup>-1</sup> )		A1	1.1b
			(3)	
3(b)	$t^2 - 3t + 7 = 2t^2 - 3$ OR $\frac{t^2 - 3t + 7}{2t^2 - 3} = \frac{1}{1} = 1$		M1	2.1
	t = 2 only		A1	1.1b
			(2)	
3(c)	Differentiate <b>v</b> wrt <i>t</i> to give a vector.		M1	3.1a
	$(2t - 3)\mathbf{i} + 4t\mathbf{j}$		A1	1.1b
			(2)	
3(d)	2t – 3 = 0		M1	3.1a
	t = 1.5		A1	1.1b
			(2)	
<b>(9 marks)</b>				
<b>Notes: Allow column vectors throughout.</b>				
3a	B1	cao		
	M1	Use of Pythagoras, including the square root, on a <b>velocity</b> vector at <i>t</i> = 0		
	A1	cao. Must come from a <u>correct</u> <b>v</b> .		
3b	M1	Equating <b>i</b> and <b>j</b> components of <b>v</b> or a ratio of 1:1 to obtain a quadratic in <i>t</i> only. If they use a constant, e.g. $t^2 - 3t + 7 = k$ and $2t^2 - 3 = k$ , <i>k</i> must be eliminated to earn this mark. <b>N.B.</b> M0 (since wrong working seen) if they write down $\mathbf{i} + \mathbf{j} = (t^2 - 3t + 7)\mathbf{i} + (2t^2 - 3)\mathbf{j}$  <b>OR</b> $\begin{pmatrix} 1 \\ 1 \end{pmatrix} = \begin{pmatrix} t^2 - 3t + 7 \\ 2t^2 - 3 \end{pmatrix}$  <b>OR</b> $t^2 - 3t + 7 = 1$ and $2t^2 - 3 = 1$		

		and then $t^2 - 3t + 7 = 2t^2 - 3$
	A1	$t = 2$
		<b>N.B.</b> Allow M1A1 for a <b>correct</b> trial and error method where they obtain $\mathbf{v} = 5\mathbf{i} + 5\mathbf{j}$ when $t = 2$ but M0 if they don't get $t = 2$
<b>3c</b>	M1	At least one power decreasing by 1 in <b>each</b> component in their $\mathbf{v}$ (M0 if clearly dividing by $t$ ) <b>Both i and j</b> needed in their answer or a column vector Allow recovery if the <b>i</b> and <b>j</b> disappear and then reappear.
	A1	cao (must be a vector) isw e.g. if they find the magnitude or put $t = 0$ or differentiate again <b>i</b> 's and <b>j</b> 's do not need to be collected. <b>N.B.</b> Allow M1A0 for $2t - 3\mathbf{i} + 4t\mathbf{j}$
<b>3d</b>	M1	$2t - 3 = 0$ or (their <b>derivative</b> of the <b>i</b> -component of $\mathbf{v}$ ) = 0 <b>N.B.</b> M0 if they equate the derivative of both components of $\mathbf{v}$ to zero.
	A1	cao <b>N.B.</b> Correct answer, with no working, can score both marks.



Question	Scheme	Marks	AOs
4(a)	$\mathbf{v}_B = (-16\mathbf{i} - 3\mathbf{j}) + 5(2.4\mathbf{i} + \mathbf{j})$	M1	3.4
	$\mathbf{v}_B = (-4\mathbf{i} + 2\mathbf{j})$	A1	1.1b
	$\sqrt{(-4)^2 + 2^2}$	M1	3.1a
	$\sqrt{20} = 2\sqrt{5}, 4.5 \text{ or better (m s}^{-1}\text{)}$	A1	1.1b
		(4)	
4(b)	<p><u>Using A as the initial position:</u></p> $\mathbf{r}_C = \mathbf{v}_A t + \frac{1}{2} \mathbf{a} t^2 + \mathbf{r}_A \quad \text{where } t = T$ $(4\mathbf{i} + c\mathbf{j}) = (-16\mathbf{i} - 3\mathbf{j})T + \frac{1}{2}(2.4\mathbf{i} + \mathbf{j})T^2 + (44\mathbf{i} - 10\mathbf{j})$ <p>OR</p> $\begin{pmatrix} 4 \\ c \end{pmatrix} = \begin{pmatrix} -16 \\ -3 \end{pmatrix} T + \frac{1}{2} \begin{pmatrix} 2.4 \\ 1 \end{pmatrix} T^2 + \begin{pmatrix} 44 \\ -10 \end{pmatrix}$ <p>Equating i-components, to give a <b>quadratic</b> equation in <math>T</math> only. Allow <math>t</math> instead of <math>T</math>.</p> <p><b>N.B.</b> Allow omission of 44 for this M mark. Also allow <math>\pm 4</math> but M0 if 4 is not used at all i.e. <math>4 = -16T + \frac{1}{2} \times 2.4T^2</math> scores M1A0A0</p>	M1	3.1a
	$4 = -16T + \frac{1}{2} \times 2.4T^2 + 44$	A1	1.1b
	$(T =) 10$	A1	1.1b
	<p><b>ALTERNATIVE</b> <u>using B as the initial position:</u></p> <p>(The position vector of B, <math>\mathbf{r}_B</math>, should be <math>-6\mathbf{i} - 12.5\mathbf{j}</math> but no credit for finding this)</p> $\mathbf{r}_C = \mathbf{v}_B t + \frac{1}{2} \mathbf{a} t^2 + \mathbf{r}_B \quad \text{using their } \mathbf{v}_B \text{ from (a) and their } \mathbf{r}_B$ $(4\mathbf{i} + c\mathbf{j}) = (-4\mathbf{i} + 2\mathbf{j})t + \frac{1}{2}(2.4\mathbf{i} + \mathbf{j})t^2 + (-6\mathbf{i} - 12.5\mathbf{j})$ $\begin{pmatrix} 4 \\ c \end{pmatrix} = \begin{pmatrix} -4 \\ 2 \end{pmatrix} t + \frac{1}{2} \begin{pmatrix} 2.4 \\ 1 \end{pmatrix} t^2 + \begin{pmatrix} -6 \\ -12.5 \end{pmatrix}$ <p>Equating i-components, to give a <b>quadratic</b> equation in <math>t</math> only. Allow if they have <math>T</math> instead of <math>t</math>.</p>	M1	3.1a

		<b>N.B.</b> Allow omission of their $-6$ or if they use 44 for this M mark. Also allow $\pm 4$ but M0 if 4 is not used at all. e.g. $4 = -4t + \frac{1}{2} \times 2.4t^2$ scores M1A0A0		
		$4 = -4t + \frac{1}{2} \times 2.4t^2 - 6$	A1	1.1b
		$t = 5$ so ( $T =$ ) 10	A1	1.1b
			<b>(3)</b>	
<b>4(c)</b>		Equating <b>j</b> -components, with <u>their value of <math>T</math> or <math>t</math> substituted</u> , to give an equation, which must have a square term, in $c$ only. <b>N.B.</b> Allow $\pm c$ in their equation.  <b>(N.B.</b> Allow omission of $-10$ or their $-12.5$ for this M mark  i.e. if using $A$ as initial position $c = (-3 \times 10) + \frac{1}{2} \times 1 \times 10^2$ scores M1M0A0 <b>OR</b> if using $B$ as initial position $c = (2 \times 5) + \frac{1}{2} \times 1 \times 5^2$ scores M1M0A0)	M1	2.1
		if using $A$ as initial position $c = (-3 \times 10) + \frac{1}{2} \times 1 \times 10^2 + (-10)$ <b>N.B.</b> Allow $\pm c$ and/or $\pm(-10)$ in their equation  <b>OR</b> if using $B$ as initial position $c = (2 \times 5) + \frac{1}{2} \times 1 \times 5^2 + (-12.5)$ <b>N.B.</b> Allow $\pm c$ and/or $\pm(-12.5)$ in their equation	M1	1.1b
		$c = 10$	A1	1.1b
			<b>(3)</b>	
<b>(10 marks)</b>				
<b>Notes: Accept column vectors throughout</b>				
<b>4a</b>	M1	Use of $\mathbf{v} = \mathbf{u} + \mathbf{at}$ with $t = 5$ to give an unsimplified $\mathbf{v}_B$		

		<p>M0 if <math>\mathbf{u} = \mathbf{0}</math></p> <p><b>N.B.</b> If using integration, they must get to the same stage i.e. have found the constant and put <math>t = 5</math></p> <p>M0 if they omit the constant altogether</p>
	A1	Correct $\mathbf{v}_B$ with $\mathbf{i}$ 's and $\mathbf{j}$ 's collected
	M1	Use of Pythagoras on <i>their</i> $\mathbf{v}_B$ to give a magnitude (need the root)
	A1	Must be positive
<b>4b</b>	M1	<p>Equating components of <math>\mathbf{i}</math> to give an equation in <math>T</math> or <math>t</math> only.</p> <p><b>N.B.</b> (they could use integration to get to the same stage) for this M mark, they <b>only</b> need to be equating the <math>\mathbf{i}</math>-components, and receive no credit until they do so.</p> <p>M0 if <math>\mathbf{u} = \mathbf{0}</math></p>
	A1	A correct equation in $T$ or $t$ only (could be in $(T - 5)$ if using $B$ as initial position)
	A1	$T = 10$
<b>4c</b>	M1	Equating components of $\mathbf{j}$ to give an equation in $c$ only but allow omission of their initial position
	M1	With their value of $T$ or $t$ and <b>must include <math>t = 0</math> position</b> (should be $-10$ if using $A$ <b>OR</b> their $-12.5$ if using $B$ )
	A1	cao

Question	Scheme	Marks	AOs
	<b>N.B.</b> In this question, allow misread of $\alpha$ for $a$ .		
<b>5(a)</b>	Use horizontal motion to give an equation in $T$ and $\alpha$ only: $28\cos\alpha \times T = 40$	M1	3.4
	$T = \frac{10}{7\cos\alpha} *$	A1*	1.1b
		<b>(2)</b>	
<b>5(b)</b>	Use vertical motion to give an equation in $T$ and $\alpha$ only	M1	3.3
	$20 = (28\sin\alpha)T - \frac{1}{2}gT^2$	A1	1.1b
	Eliminate $T$ to give an unsimplified equation in $\alpha$ only: $20 = (28\sin\alpha) \times \frac{10}{7\cos\alpha} - \frac{1}{2}g\left(\frac{10}{7\cos\alpha}\right)^2$	M1	1.1b
	Use $\sec^2\alpha = 1 + \tan^2\alpha$ oe to give an unsimplified equation in <b>tan <math>\alpha</math> only</b> : $20 = 40\tan\alpha - \frac{1}{2}g \times \frac{100}{49}(1 + \tan^2\alpha)$	M1	3.1b
	$\tan^2\alpha - 4\tan\alpha + 3 = 0 *$ (allow $0 = \tan^2\alpha - 4\tan\alpha + 3$ )	A1*	2.2a
		<b>(5)</b>	
<b>5(c)</b>	Solve and use of $\tan\alpha = 3$ or $\sin\alpha = \frac{3}{\sqrt{10}}$ or $\alpha = 71.565..^\circ$ to find an equation in $H$ only.	M1	3.1b
	$0 = (28\sin\alpha)^2 - 2gH$ <b>where</b> $\tan\alpha = 3$ ( $\alpha = 71.565..^\circ$ )	M1	3.4
	$H = 36$ or $36.0$ (m)	A1	1.1b
		<b>(3)</b>	
<b>5(d)</b>	e.g. spin of the ball, the wind, the dimensions or shape of the ball, ball is modelled as a particle, uses an inaccurate value of $g$ , motion takes place in 3D not in 2D, $g$ could be variable. B0 if mass or weight are mentioned. B0 for ground may not be horizontal.	B1	3.5b
		<b>(1)</b>	

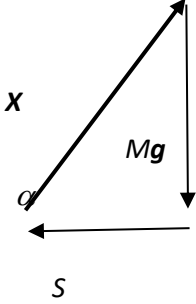
(11 marks)

**Notes:**

<b>5a</b>	M1	Correct no. of terms, dim correct, condone sin/cos confusion and sign errors
	A1*	Correct printed answer correctly obtained. Allow $\frac{10}{7 \cos \alpha} = T$ OR $T = \frac{40}{28 \cos \alpha} = \frac{10}{7 \cos \alpha}$ OR $\frac{40}{28 \cos \alpha} = \frac{10}{7 \cos \alpha} = T$ OR $t$ instead of $T$
<b>5b</b>	M1	Correct no. of terms, dim correct, condone sin/cos confusion and sign errors
	A1	Correct equation
	M1	Eliminate $T$ , using either the given answer in (a) or their own $T$ expression, from their equation to give an unsimplified equation in $\alpha$ only
	M1	Use $\sec^2 \alpha = 1 + \tan^2 \alpha$ to produce an equation in $\tan \alpha$ only
	A1*	Given answer correctly obtained. <b>N.B.</b> Must be $\alpha$ (or $a$ ) in the final answer but allow a different angle in the working.
<b>5c</b>	M1	Solve given equation and select larger value of $\tan \alpha$ and use it to try to obtain an equation in $H$ only.
	M1	Complete method to give an equation in <b><math>H</math> only</b> , using <b>larger</b> value of $\alpha$ , correct no. of terms, dim correct, condone sin/cos confusion and sign errors.
	A1	cao. Must be positive, (allow a negative value, changed to a positive answer). <b>N.B.</b> This answer comes from use of $g = 9.8$ , so must be rounded to 2 or 3 sf.
<b>5d</b>	B1	B0 if any incorrect extras

Question	Scheme	Marks	AOs
6(a)	The normal reaction at $B$ is acting to the left so it must act to the right, right as it needs to balance (oppose, counter) the force at $B$ , right as it prevents the rod from sliding (slipping, falling), right as the weight (mass) of the rod will mean the rod tends to slip left, mass or weight will be pushing the rod to the left so friction will oppose that. <b>N.B.</b> You may see an arrow on the diagram at $A$ , instead of 'right'. B0 if they say the rod is moving oe Accept towards the wall instead of to the right.	B1	2.4
		(1)	
6(b)	Take moments about $A$	M1	3.4
	$S \times 2a \sin \theta = Mga \cos \theta$	A1	1.1b
	$S = \frac{1}{2} Mg \cot \theta^*$	A1*	2.2a
		(3)	
6(c)	Resolve vertically, $R = Mg$	B1	3.3
	Resolve horizontally, $F = S$	B1	3.3
	Other possible equations: Resolve along the rod, $F \cos \theta + R \sin \theta = S \cos \theta + Mg \sin \theta$ Resolve perp to the rod, $R \cos \theta + S \sin \theta = F \sin \theta + Mg \cos \theta$ $M(B)$ , $R \times 2a \cos \theta = F \times 2a \sin \theta + Mga \cos \theta$ $M(G)$ , $Ra \cos \theta = Fa \sin \theta + Sa \sin \theta$ <b>N.B.</b> When entering these two B marks on ePEN, <b>First</b> B1 is for a <b>vertical</b> resolution, <b>second</b> B1 is for a <b>horizontal</b> resolution, and if either is replaced by a different equation, enter appropriately. If both are replaced by other equations, enter in the order in which they appear in their working.		
	$F = \mu R$	B1	1.2
	$\frac{1}{2} Mg \times \frac{4}{3} = \mu Mg$	dM1	2.1
	$\mu = \frac{2}{3}$ oe Accept 0.67 or better	A1	2.2a
	<b>S.C. For <math>F</math> ,, <math>\mu R</math>,</b>	B0	
	$\frac{1}{2} Mg \times \frac{4}{3}$ ,, $\mu Mg$	M1	

		$\frac{2}{3} \mu$	A0		
		<b>N.B.</b> If $\mu = \frac{2}{3}$ follows this, they could score all the marks.			
				<b>(5)</b>	
<b>6(d)</b>		$\sqrt{F^2 + R^2}$		M1	3.1a
		$\sqrt{\left(\frac{2}{3}Mg\right)^2 + (Mg)^2}$		M1	1.1b
		$\frac{1}{3}Mg\sqrt{13}$ or 1.2Mg or better		A1	2.2a
				<b>(3)</b>	
<b>6(e)</b>		New value of S would be <b>larger</b> as the <b>moment</b> of the <b>weight</b> about <b>A</b> would be larger		B1	3.5a
				<b>(1)</b>	
<b>(13 marks)</b>					
<b>Notes:</b>					
<b>6a</b>	B1	Any equivalent appropriate statement.			
<b>6b</b>	M1	Correct no. of terms, dimensionally correct, condone sin/cos confusion and sign errors. <b>N.B.</b> If $a$ 's never appear, M0			
	A1	Correct equation			
	A1*	Correct given answer correctly obtained, <b>with no wrong working seen.</b> Allow $\frac{1}{2}Mg \cot \theta = S$ or $S = \frac{Mg \cot \theta}{2}$ or $\frac{Mg \cot \theta}{2} = S$ or $S = \frac{Mg}{2} \cot \theta$ or similar but NOT $S = \frac{1}{2} \cot \theta Mg$ or similar <b>N.B.</b> Allow $m$ instead of $M$ Must be $\theta$ in final answer but allow a different angle in the working.			
<b>6c</b>	B1	cao			
	B1	cao			
	B1	Seen anywhere, e.g. on the diagram			
	<b>dM1</b>	Using $F = \mu R$ , their two equations and substitute for trig (not necessarily correctly) to produce an equation in $\mu$ only. This mark is <b>dependent</b> on the 3 previous B marks.			
	A1	Accept 0.67 or better			

<b>6d</b>	M1	Use of Pythagoras with square root to find the required magnitude, but $F$ and $R$ do not need to be substituted
	M1	Substitute for their $F$ and their $R$ in terms of $Mg$ and take square root to obtain magnitude in terms of $M$ and $g$ only. <b>N.B.</b> Must be using Pythagoras
		<p><b>ALTERNATIVE:</b> Using trig on triangle of forces</p>  <p>M1: <math>X = \frac{Mg}{\sin \alpha}</math> or <math>\frac{S}{\cos \alpha}</math></p> <p>M1: substitute for <math>\sin \alpha</math> or <math>\cos \alpha</math> and <math>S</math>, where <math>\tan \alpha = \frac{Mg}{S} (= \frac{3}{2})</math>, to obtain <math>X</math> in terms of <math>M</math> and <math>g</math> only.</p>
	A1	Any equivalent surd form or $1.2Mg$ or better Must be in terms of $M$ and $g$
<b>6e</b>	B1	Correct answer and any equivalent appropriate statement.



