

Question	Scheme	Marks	AOs
8 (a)	$(2+ax)^8$ Attempts the term in $x^5 = {}^8C_5 2^3 (ax)^5 = 448a^5 x^5$	M1 A1	1.1a 1.1b
	Sets $448a^5 = 3402 \Rightarrow a^5 = \frac{243}{32}$	M1	1.1b
	$\Rightarrow a = \frac{3}{2}$	A1	1.1b
		(4)	
(b)	Attempts either term. So allow for 2^8 or ${}^8C_4 2^4 a^4$	M1	1.1b
	Attempts the sum of both terms $2^8 + {}^8C_4 2^4 a^4$	dM1	2.1
	$= 256 + 5670 = 5926$	A1	1.1b
		(3)	

(7 marks)**Notes****(a)**

M1: An attempt at selecting the correct term of the binomial expansion. If all terms are given then the correct term must be used. Allow with a missing bracket ${}^8C_5 2^3 ax^5$ and left without the binomial coefficient expanded

A1: $448a^5 x^5$ Allow unsimplified but 8C_5 must be "numerical"

M1: Sets their $448a^5 = 3402$ and proceeds to $\Rightarrow a^k = \dots$ where $k \in \mathbb{N}$ $k \neq 1$

A1: Correct work leading to $a = \frac{3}{2}$

(b)

M1: Finds either term required. So allow for 2^8 or ${}^8C_4 2^4 a^4$ (even allowing with a)

dM1: Attempts the sum of both terms $2^8 + {}^8C_4 2^4 a^4$

A1: cso 5926

Question	Scheme	Marks	AOs
11(a)	$\left(2 - \frac{x}{16}\right)^9 = 2^9 + \binom{9}{1}2^8 \cdot \left(-\frac{x}{16}\right) + \binom{9}{2}2^7 \cdot \left(-\frac{x}{16}\right)^2 + \dots$	M1	1.1b
	$\left(2 - \frac{x}{16}\right)^9 = 512 + \dots$	B1	1.1b
	$\left(2 - \frac{x}{16}\right)^9 = \dots - 144x + \dots$	A1	1.1b
	$\left(2 - \frac{x}{16}\right)^9 = \dots + \dots + 18x^2 (+ \dots)$	A1	1.1b
		(4)	
(b)	Sets '512' $a = 128 \Rightarrow a = \dots$	M1	1.1b
	$(a =) \frac{1}{4}$ oe	A1 ft	1.1b
		(2)	
(c)	Sets '512' $b + '-144' a = 36 \Rightarrow b = \dots$	M1	2.2a
	$(b =) \frac{9}{64}$ oe	A1	1.1b
		(2)	
(8 marks)			
11(a) alt	$\left(2 - \frac{x}{16}\right)^9 = 2^9 \left(1 - \frac{x}{32}\right)^9 = 2^9 \left(1 + \binom{9}{1} \left(-\frac{x}{32}\right) + \binom{9}{2} \left(-\frac{x}{32}\right)^2 + \dots\right)$	M1	1.1b
	$= 512 + \dots$	B1	1.1b
	$= \dots - 144x + \dots$	A1	1.1b
	$= \dots + \dots + 18x^2 (+ \dots)$	A1	1.1b
Notes			
<p>(a) M1: Attempts the binomial expansion. May be awarded on either term two and/or term three Scored for a correct binomial coefficient combined with a correct power of 2 and a correct power of $\left(\pm \frac{x}{16}\right)$ Condone $\binom{9}{2}2^7 \cdot \left(-\frac{x^2}{16}\right)$ for term three.</p> <p>Allow any form of the binomial coefficient. Eg $\binom{9}{2} = {}^9C_2 = \frac{9!}{7!2!} = 36$</p> <p>In the alternative it is for attempting to take out a factor of 2 (may allow 2^n outside bracket) and having a correct binomial coefficient combined with a correct power of $\left(\pm \frac{x}{32}\right)$</p>			

Question	Scheme	Marks	AOs
8(a)	2^6 or 64 as the constant term	B1	1.1b
	$\left(2 + \frac{3x}{4}\right)^6 = \dots + {}^6C_1 2^5 \left(\frac{3x}{4}\right)^1 + {}^6C_2 2^4 \left(\frac{3x}{4}\right)^2 + \dots$	M1	1.1b
	$= \dots + 6 \times 2^5 \left(\frac{3x}{4}\right)^1 + \frac{6 \times 5}{2} \times 2^4 \left(\frac{3x}{4}\right)^2 + \dots$	A1	1.1b
	$= 64 + 144x + 135x^2 + \dots$	A1	1.1b
		(4)	
(b)	$\frac{3x}{4} = -0.075 \Rightarrow x = -0.1$	B1ft	2.4
	So find the value of $64 + 144x + 135x^2$ with $x = -0.1$		
		(1)	

(5 marks)**Notes****(a)****B1:** Sight of either 2^6 or 64 as the constant term**M1:** An attempt at the binomial expansion. This may be awarded for a correct attempt at either the second **OR** third term. Score for the correct binomial coefficient with the correct power of 2 and the correct power of $\frac{3x}{4}$ condoning slips. Correct bracketing is not essential for this M mark.Condone ${}^6C_2 2^4 \frac{3x^2}{4}$ for this mark**A1:** Correct (unsimplified) second **AND** third terms.The binomial coefficients must be processed to numbers /numerical expression e.g $\frac{6!}{4!2!}$ or $\frac{6 \times 5}{2}$ They cannot be left in the form 6C_1 and/or $\binom{6}{2}$ **A1:** $64 + 144x + 135x^2 + \dots$ Ignore any terms after this. Allow to be written 64, 144x, $135x^2$ **(b)****B1ft:** $x = -0.1$ or $-\frac{1}{10}$ **with** a comment about substituting this into their $64 + 144x + 135x^2$ If they have written (a) as 64, 144x, $135x^2$ candidate would need to say substitute $x = -0.1$ into the sum of the first three terms.

As they do not have to perform the calculation allow

Set $2 + \frac{3x}{4} = 1.925$, solve for x and then substitute this value into the expression from (a)If a value of x is found then it must be correct

Alternative to part (a)

$$\left(2 + \frac{3x}{4}\right)^6 = 2^6 \left(1 + \frac{3x}{8}\right)^6 = 2^6 \left(1 + {}^6C_1 \left(\frac{3x}{8}\right)^1 + {}^6C_2 \left(\frac{3x}{8}\right)^2 + \dots\right)$$

B1: Sight of either 2^6 or 64

Question	Scheme	Marks	AOs
6 (a)	$(1+kx)^{10} = 1 + \binom{10}{1}(kx)^1 + \binom{10}{2}(kx)^2 + \binom{10}{3}(kx)^3 \dots$	M1 A1	1.1b 1.1b
	$= 1 + 10kx + 45k^2x^2 + 120k^3x^3 \dots$	A1	1.1b
		(3)	
(b)	Sets $120k^3 = 3 \times 10k$	B1	1.2
	$4k^2 = 1 \Rightarrow k = \dots$	M1	1.1b
	$k = \pm \frac{1}{2}$	A1	1.1b
		(3)	
(6 marks)			

(a)

M1: An attempt at the binomial expansion. This may be awarded for either the second or third term or fourth term. The coefficients may be of the form ${}^{10}C_1$, $\binom{10}{2}$ etc or eg $\frac{10 \times 9 \times 8}{3!}$

A1: A correct unsimplified binomial expansion. The coefficients must be numerical so cannot be of the form ${}^{10}C_1$, $\binom{10}{2}$. Coefficients of the form $\frac{10 \times 9 \times 8}{3!}$ are acceptable for this mark.

The bracketing must be correct on $(kx)^2$ but allow recovery

A1: $1 + 10kx + 45k^2x^2 + 120k^3x^3 \dots$ or $1 + 10(kx) + 45(kx)^2 + 120(kx)^3 \dots$
Allow if written as a list.

(b)

B1: Sets their $120k^3 = 3 \times$ their $10k$ (Seen or implied)

For candidates who haven't cubed allow $120k = 3 \times$ their $10k$

If they write $120k^3 x^3 = 3 \times$ their $10kx$ only allow recovery of this mark if x disappears afterwards.

M1: Solves a cubic of the form $Ak^3 = Bk$ by factorising out/cancelling the k and proceeding correctly to at least one value for k . Usually $k = \sqrt{\frac{B}{A}}$

A1: $k = \pm \frac{1}{2}$ o.e ignoring any reference to 0

Question	Scheme	Marks	AOs
7(a)	$\left(2 - \frac{x}{2}\right)^7 = 2^7 + \binom{7}{1}2^6 \cdot \left(-\frac{x}{2}\right) + \binom{7}{2}2^5 \cdot \left(-\frac{x}{2}\right)^2 + \dots$	M1	1.1b
	$\left(2 - \frac{x}{2}\right)^7 = 128 + \dots$	B1	1.1b
	$\left(2 - \frac{x}{2}\right)^7 = \dots - 224x + \dots$	A1	1.1b
	$\left(2 - \frac{x}{2}\right)^7 = \dots + \dots + 168x^2 (+ \dots)$	A1	1.1b
		(4)	
(b)	Solve $\left(2 - \frac{x}{2}\right) = 1.995$ so $x = 0.01$ and state that 0.01 would be substituted for x into the expansion	B1	2.4
		(1)	
(5 marks)			
Notes:			
(a)			
M1: Need correct binomial coefficient with correct power of 2 and correct power of x . Coefficients may be given in any correct form; e.g. 1, 7, 21 or 7C_0 , 7C_1 , 7C_2 or equivalent			
B1: Correct answer, simplified as given in the scheme			
A1: Correct answer, simplified as given in the scheme			
A1: Correct answer, simplified as given in the scheme			
(b)			
B1: Needs a full explanation i.e. to state $x = 0.01$ and that this would be substituted and that it is a solution of $\left(2 - \frac{x}{2}\right) = 1.995$			

Question Number	Scheme	Marks
1.	$\left(3 - \frac{1}{3}x\right)^5 -$ $3^5 + {}^5C_1 3^4 \left(-\frac{1}{3}x\right) + {}^5C_2 3^3 \left(-\frac{1}{3}x\right)^2 + {}^5C_3 3^2 \left(-\frac{1}{3}x\right)^3 \dots$ First term of 243 $\left({}^5C_1 \times \dots \times x\right) + \left({}^5C_2 \times \dots \times x^2\right) + \left({}^5C_3 \times \dots \times x^3\right) \dots$ $= (243 \dots) - \frac{405}{3}x + \frac{270}{9}x^2 - \frac{90}{27}x^3 \dots$ $= (243 \dots) - 135x + 30x^2 - \frac{10}{3}x^3 \dots$	B1 M1 A1 A1 (4) [4]
Alternative method	$\left(3 - \frac{1}{3}x\right)^5 = 3^5 \left(1 - \frac{x}{9}\right)^5$ $3^5 \left(1 + {}^5C_1 \left(-\frac{1}{9}x\right) + {}^5C_2 \left(-\frac{1}{9}x\right)^2 + {}^5C_3 \left(-\frac{1}{9}x\right)^3 \dots\right)$ Scheme is applied exactly as before	
Notes B1: The constant term should be 243 in their expansion M1: Two of the three binomial coefficients must be correct and must be with the correct power of x. Accept 5C_1 or $\binom{5}{1}$ or 5 as a coefficient, and 5C_2 or $\binom{5}{2}$ or 10 as another and 5C_3 or $\binom{5}{3}$ or 10 as another..... Pascal's triangle may be used to establish coefficients. NB: If they only include the first two of these terms then the M1 may be awarded. A1: Two of the final three terms correct – may be unsimplified i.e. two of $-135x + 30x^2 - \frac{10}{3}x^3$ correct, or two of $-\frac{405}{3}x + \frac{270}{9}x^2 - \frac{90}{27}x^3$ (may be just two terms) A1: All three final terms correct and simplified. (Can be listed with commas or appear on separate lines. Accept in reverse order.) Accept correct alternatives to $-\frac{10}{3}$ e.g. $-3\frac{1}{3}$ or $-3.\bar{3}$ the recurring must be clear. 3.3 is not acceptable. Allow e.g. $+ -135x$		
e.g. The common error $3^5 + {}^5C_1 3^4 \left(-\frac{1}{3}x\right) + {}^5C_2 3^3 \left(-\frac{1}{3}x\right)^2 + {}^5C_3 3^2 \left(-\frac{1}{3}x\right)^3 = (243) - 135x - 90x^2 - 30x^3$ would earn B1, M1, A0, A0, so 2/4 If extra terms are given then isw No negative signs in answer also earns B1, M1, A0, A0 If the series is divided through by 3 at the final stage after an error or omission resulting in all multiple of three coefficients then apply scheme to series before this division and ignore subsequent work (isw) Special Case: Only gives first three terms $=(243 \dots) - 135x + 30x^2 \dots$ or $243 - \frac{405}{3}x + \frac{270}{9}x^2$ Follow the scheme to give B1 M1 A1 A0 special case. (Do not treat as misread.) Answers such as $243 + 405 - \frac{1}{3}x + 270 - \frac{1}{9}x^2 + 90 - \frac{1}{27}x^3 \dots$ gain no credit as the binomial coefficients are not linked to the x terms.		

Question Number	Scheme	Marks
5.	(a) $(2-9x)^4 = 2^4 + {}^4C_1 2^3(-9x) + {}^4C_2 2^2(-9x)^2$, (b) $f(x) = (1+kx)(2-9x)^4 = A - 232x + Bx^2$	
(a)	First term of 16 in their final series	B1
Way 1	At least one of $({}^4C_1 \times \dots \times x)$ or $({}^4C_2 \times \dots \times x^2)$	M1
	$= (16) - 288x + 1944x^2$	At least one of $-288x$ or $+1944x^2$ A1
		Both $-288x$ and $+1944x^2$ A1
		[4]
(a)	$(2-9x)^4 = (4-36x+81x^2)(4-36x+81x^2)$	First term of 16 in their final series B1
Way 2	$= 16 - 144x + 324x^2 - 144x + 1296x^2 + 324x^2$	Attempts to multiply a 3 term quadratic by the same 3 term quadratic to achieve either 2 terms in x or at least 2 terms in x^2 . M1
	$= (16) - 288x + 1944x^2$	At least one of $-288x$ or $+1944x^2$ A1
		Both $-288x$ and $+1944x^2$ A1
		[4]
(a)	$\{(2-9x)^4\} = 2^4 \left(1 - \frac{9}{2}x\right)^4$	First term of 16 in final series B1
Way 3	$= 2^4 \left(1 + 4\left(\frac{-9}{2}x\right) + \frac{4(3)}{2}\left(\frac{-9}{2}x\right)^2 + \dots\right)$	At least one of $(4 \times \dots \times x)$ or $\left(\frac{4(3)}{2} \times \dots \times x^2\right)$ M1
	$= (16) - 288x + 1944x^2$	At least one of $-288x$ or $+1944x^2$ A1
		Both $-288x$ and $+1944x^2$ A1
		[4]
	Parts (b), (c) and (d) may be marked together	
(b)	$A = "16"$	Follow through their value from (a) B1ft
		[1]
(c)	$\{(1+kx)(2-9x)^4\} = (1+kx)(16 - 288x + \{1944x^2 + \dots\})$	May be seen in part (b) or (d) and can be implied by work in parts (c) or (d). M1
	x terms: $-288x + 16kx = -232x$	
	giving, $16k = 56 \Rightarrow k = \frac{7}{2}$	$k = \frac{7}{2}$ A1
		[2]
(d)	x^2 terms: $1944x^2 - 288kx^2$	
	So, $B = 1944 - 288\left(\frac{7}{2}\right); = 1944 - 1008 = 936$	See notes 936 M1 A1
		[2]
		9

Question Number	Scheme	Marks
11.(a)	$(3+ax)^5 = 3^5 + \binom{5}{1}3^4(ax) + \binom{5}{2}3^3(ax)^2 + \dots$ $= 243 + 405ax + 270a^2x^2 + \dots$	M1 B1, A1, A1 [4]
(b)	$f(x) = (a-x)(3+ax)^5 = (a-x)(243 + 405ax + 270a^2x^2 + \dots)$ $-243 + 405a^2 = 0 \Rightarrow a^2 = \frac{243}{405} \Rightarrow a = \sqrt{\frac{3}{5}} \text{ or equivalent}$	M1,dM1A1 [3] (7 marks)

(a)

M1 This method mark is awarded for an attempt at a Binomial expansion to get the second and/or third term – it requires a correct binomial coefficient combined with correct power of 3 and the correct power of x . Ignore bracketing errors. Accept any notation for 5C_1 , 5C_2 , e.g. as on scheme or 5, and 10 from Pascal's triangle. This mark may be given if no working is shown, if either or both of the terms including x is correct.

An alternative is $(3+ax)^5 = 3^5 \left\{ 1 + \frac{ax}{3} \right\}^5 = 3^5 \left\{ 1 + 5 \times \frac{ax}{3} + \frac{5 \times 4}{2(!)} \times \left(\frac{ax}{3} \right)^2 \right.$

In this method it is scored for the correct attempt at a binomial expansion to get the second and/or third term in the bracket of $3^n \left\{ 1 + 5 \times \frac{ax}{3} + \frac{5 \times 4}{2(!)} \times \left(\frac{ax}{3} \right)^2 \dots \dots \right\}$

Score for binomial coefficient with the correct power of $\left(\frac{x}{3} \right)$ Eg. $5 \times \frac{..x}{3}$ or $10 \times \left(\frac{..x}{3} \right)^2$

B1 Must be simplified to 243 (writing just 3^5 is B0).

A1 cao and is for one correct from $405ax$, and $270a^2x^2$ Also allow $270(ax)^2$ with the bracket

A1 cao and is for both of $405ax$, and $270a^2x^2$.

Allow $270(ax)^2$ with the bracket correct (ignore extra terms). Allow listing for all marks

It is possible to score 1011 in (a)

There are a minority of students who attempt this in (a)

$f(x) = (a-x)(3+ax)^5 = (a-x)(243 + 405ax + 270a^2x^2 + \dots)$ and go on to expand this.

They can have all the marks in part (a)

(b)

M1 Attempt to set the coefficient of x in the expansion of $(a-x)(3+ax)^5$ equal to 0

$$(a-x)(3+ax)^5 = (a-x)(P + Qax + Ra^2x^2 + \dots) = aP + (a^2Q - P)x + \dots$$

For this to be scored you must see an equation of the form $\pm P \pm Qa^2 = 0$ You are condoning slips/ sign errors

dM1 For $\pm P \pm Qa^2 = 0 \Rightarrow a = \dots$ using a correct method. This cannot be scored for an attempt at sq rooting a negative number

A1 $a = \sqrt{\frac{3}{5}}$ or exact equivalent such as $a = \frac{\sqrt{15}}{5}$ You may ignore any reference to $a = -\sqrt{\frac{3}{5}}$

Question Number	Scheme	Marks
10 (a)	2^{10} OR 1024 seen as the constant term $\left(2 - \frac{x}{8}\right)^{10} = 2^{10} + {}^{10}C_1 2^9 \left(-\frac{x}{8}\right)^1 + {}^{10}C_2 2^8 \left(-\frac{x}{8}\right)^2 + \dots$ $= 1024 - 640x + 180x^2 + \dots$	B1 M1A1 A1 (4)
(b)	$\left(2 - \frac{x}{8}\right)^{10} (a + bx) = (1024 - 640x + 180x^2)(a + bx)$ $1024a = 256 \Rightarrow a = \frac{1}{4}$ oe	M1A1 (2)
(c)	$1024b - 640a = 352 \Rightarrow b = \frac{1}{2}$	M1A1 (2)
		(8 marks)

(a)

B1 2^{10} OR 1024 seen as the constant termM1 For a correct attempt at the binomial expansion for $(a + b)^n$ with $a = 2$, $b = \pm \frac{x}{8}$ and $n = 10$ Condone missing brackets. Accept any unsimplified term in x as evidenceAccept a power series expansion on $(1 \pm kx)^{10} = 1 + 10(\pm kx) + \frac{10 \times 9}{2}(\pm kx)^2 + \dots$ condoning missing brackets. Again accept any unsimplified term in x as evidence

A1 A completely correct unsimplified solution.

Accept $= 2^{10} + {}^{10}C_1 2^9 \left(-\frac{x}{8}\right)^1 + {}^{10}C_2 2^8 \left(-\frac{x}{8}\right)^2 + \dots$

Accept $= 2^{10} \left(1 + 10 \times \left(-\frac{x}{16}\right) + \frac{10 \times 9 \times \left(-\frac{x}{16}\right)^2}{2!} + \dots \right)$

A1 $1024 - 640x + 180x^2$ Accept $1024 + -640x + 180x^2$

Can be listed with commas or appear on separate lines. Accept in reverse order.

(b)

M1 Sets their '1024' $\times a = 256$ A1 $a = \frac{1}{4}$. Accept equivalents such as 0.25.Accept this for both marks (it can be done by substituting $x = 0$ into both sides of the expression) as long as it is not found from an incorrect method

(c)

M1 Sets their '1024' $\times b \pm$ their '640' $a = 352$ A1 $b = \frac{1}{2}$ or 0.5

Question Number	Scheme	Marks	
	Mark (a) and (b) together		
10(a)	$(1+ax)^{20} = 1^{20} + {}^{20}C_1 1^{19} (ax)^1 + {}^{20}C_2 1^{18} (ax)^2$. Note that the notation $\binom{20}{1}$ may be seen for ${}^{20}C_1$ etc.		
	${}^{20}C_1 1^{19} (ax)^1 = 4x \Rightarrow 20a = 4 \Rightarrow a = 0.2$	M1: Uses either ${}^{20}C_1 (1^{19})(ax)^1 = 4x^1$ or $20a = 4$ to obtain a value for a . A1: $a = 0.2$ or equivalent	M1A1
			(2)
(b)	${}^{20}C_2 1^{18} (ax)^2 = px^2$ $\Rightarrow \frac{20 \times 19}{2} \times (0.2)^2 = p$ $\Rightarrow p = \dots$	Uses ${}^{20}C_2 (1^{18})(ax)^2 = px^2$ and their value of a to find a value for p . Condone the use of a rather than a^2 in finding p . Maybe implied by an attempt to find a value for $190a^2$ or $190a$. Note: ${}^{20}C_{18}$ can be used for ${}^{20}C_2$	M1
	$p = 7.6$	Accept equivalents such as $\frac{38}{5}, \frac{190}{25}$	A1
			(2)
(c)	Term is ${}^{20}C_4 1^{16} (ax)^4 \Rightarrow q = \dots$	Identifies the correct term and uses their value of a to find a value for q . Condone the use of a rather than a^4 . Must be an attempt to calculate ${}^{20}C_4 a^4$ or ${}^{20}C_4 a$ or ${}^{20}C_{16} a^4$ or ${}^{20}C_{16} a$	M1
	$q = {}^{20}C_4 \times 0.2^4 = \frac{969}{125} = (7.752)$	$q = \frac{969}{125}$ or exact equivalent e.g. $7.752, 7\frac{94}{125}$. $q = \frac{969}{125} x^4$ scores A0 but $qx^4 = \frac{969}{125} x^4$ scores A1.	A1
			(2)
			(6 marks)

Question	Scheme	Marks
5.	<p>(a) $\left(3 - \frac{ax}{2}\right)^5 = 3^5 + \binom{5}{1}3^4 \cdot \left(-\frac{ax}{2}\right) + \binom{5}{2}3^3 \cdot \left(-\frac{ax}{2}\right)^2 + \binom{5}{3}3^2 \cdot \left(-\frac{ax}{2}\right)^3 \dots$ $= 243, -\frac{405}{2}ax + \frac{135}{2}a^2x^2 - \frac{45}{4}a^3x^3 \dots$</p> <p>(b) $\frac{405}{2}a = \frac{45}{4}a^3$ $a^2 = \frac{810}{45} = 18 \text{ or equivalent}$ $a = 3\sqrt{2}$</p>	<p>M1 B1, A1, A1 [4]</p> <p>M1 A1 A1 [3]</p> <p>7 marks</p>
Notes		

(a)**M1:** The **method** mark is awarded for an attempt at Binomial to get the second and/or third and/or fourth term.You need to see the **correct** binomial coefficient combined with correct power of x . e.g. $\binom{5}{2} \dots x^2$ Condone bracket errors. Accept any notation for 5C_1 , 5C_2 and 5C_3 , e.g. $\binom{5}{1}$, $\binom{5}{2}$ and $\binom{5}{3}$

or 5, 10 and 10 from Pascal's triangle.

The mark can be applied in the same way if 3^5 is taken out as a factor.**B1:** For the first term of 243. (writing just 3^5 is **B0**).**A1:** is cao and is for **two correct and simplified terms** from $-\frac{405}{2}ax$, $+\frac{135}{2}a^2x^2$ and $-\frac{45}{4}a^3x^3 \dots$ Allow two correct from $-\frac{405}{2}(ax)$, $+\frac{135}{2}(ax)^2$ and $-\frac{45}{4}(ax)^3 \dots$ with the brackets.

Allow decimals. Allow lists

A1: is c.a.o and is for **all** of the terms correct and simplified.Allow $+\frac{135}{2}(ax)^2$ and $-\frac{45}{4}(ax)^3 \dots$ (ignore x^4 terms)Allow decimal equivalents $-202.5ax + 67.5a^2x^2 - 11.25a^3x^3 \dots$ Allow listing.**(b)****M1:** Puts their coefficient of x equal to their coefficient of x^3 (There should be no x terms)**A1:** This is cao for obtaining a^2 or a correctly (may be unsimplified)**A1:** This is cao for $a = 3\sqrt{2}$ Condone $a = \pm 3\sqrt{2}$

We will condone all 3 marks to be scored in (b) from a solution in (a) where all signs are +ve

$$= 243 + \frac{405}{2}ax + \frac{135}{2}a^2x^2 + \frac{45}{4}a^3x^3 \dots$$

Question Number	Scheme	Marks
1	$(1 + px)^8 = 1 + 8(px) + \frac{8 \times 7}{2!}(px)^2$	M1
	Compares coefficients in $x \Rightarrow 8p = 12 \Rightarrow p = 1.5$	M1A1
	Compares coefficients in $x^2 \Rightarrow q = 28p^2 \Rightarrow q = 63$	M1A1
		(5) (5 marks)

(a)

M1 Uses the power series expansion/ binomial expansion with the correct form for terms 2 and 3. You may ignore the first term in this question.

Accept the correct coefficient with the correct power of x for terms 2 and 3.

$$(1 + px)^8 = 1 + 8(..x) + \frac{8 \times 7}{2!}(..x)^2$$

Allow missing bracket on x^2 term.

Allow for $(1 + px)^8 = 1 + \binom{8}{1}(..x) + \binom{8}{2}(..x)^2$ or equivalent.

Allow sight of $\binom{8}{1}(..x)$ and $\binom{8}{2}(..x)^2$ separated by commas

M1 Sets their coefficient in x equal to 12 $\Rightarrow 8p = 12 \Rightarrow p = \dots$

It is not dependent on the previous M but it must be of the form $kp = 12 \Rightarrow p = \dots$

A1 $p = 1.5$ or equivalent such as $\frac{12}{8}$

M1 Sets q equal to their coefficient of x^2 (which must include a p or a p^2) then substitutes in their value of p leading to $q =$

A1 $q = 63$

Question Number	Scheme	Marks
7(a)	$(1+kx)^8 = 1 + \binom{8}{1}(kx) + \binom{8}{2}(kx)^2 + \binom{8}{3}(kx)^3 \dots$	M1
	$= 1 + 8kx + 28k^2x^2 + 56k^3x^3 + \dots$	B1, A1, A1
	!	[4]
(b)	Sets "56k ³ " = 1512 and obtains $k^3 = \frac{1512}{56}$	M1 A1
	So $k = 3$	A1
		[3]
		7 marks
	Notes	
(a)	<p>M1: The method mark is awarded for an attempt at the Binomial expansion to get the third and/or fourth term. The correct binomial coefficient needs to be combined with the correct power of x. Ignore bracket errors and omission of or incorrect powers of k. Accept any notation for 8C_2 or 8C_3, e.g. $\binom{8}{2}$ or $\binom{8}{3}$ or 28 or 56 from Pascal's triangle.</p> <p>This mark may be given if no working is shown, but either or both of $28k^2x^2$ and $56k^3x^3$ is found.</p> <p>B1: This is for $1 + 8kx$ and not for just $1 + \binom{8}{1}(kx)$</p> <p>A1: is cao and is for $28k^2x^2$ or for $28(kx)^2$</p> <p>A1: is cao and is for $56k^3x^3$ or for $56(kx)^3$</p> <p>Any extra terms in higher powers of x should be ignored.</p> <p>Allow terms separated by commas or given as a list for all the marks.</p>	
(b)	<p>M1: Sets their coefficient of $x^3 = 1512$ and obtains $k^n = ..$ where n is 1 or 3</p> <p>A1: $k^3 = \frac{1512}{56}$ or equivalent e.g. 27 (May be implied by their final answer)</p> <p>A1: $k = 3$ cao (± 3 is A0)</p> <p>Note (b) can be marked independently of part (a) so part (a) might be incorrect or not attempted but they have $56k^3 = 1512$ etc. in (b)</p>	

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Question Number	Scheme	Marks
6.(a)	$(2+ax)^6 = 2^6 + \binom{6}{1}2^5 \cdot (ax) + \binom{6}{2}2^4 \cdot (ax)^2 + \dots$ $= 64 + 192ax + 240a^2x^2 + \dots$	M1 B1, A1, A1 [4]
(b)	$192a = 240a^2$ $a = \frac{192}{240} = 0.8 \text{ or equivalent}$	M1 A1 [2] 6 marks
Alt 6.(a)	$(2+ax)^6 = 2^6 \left(1 + \frac{a}{2}x\right)^6 = 2^6 \left(1 + 6 \times \frac{a}{2}x + \frac{6 \times 5}{2} \left(\frac{a}{2}x\right)^2 + \dots\right)$ $= 64 + 192ax + 240a^2x^2 + \dots$	M1 B1, A1, A1 [4]

- (a)**
- M1 The method mark is awarded for an attempt at a Binomial expansion to get an unsimplified second or third term – Look for a correct binomial coefficient multiplied by a correct power of x . Eg ${}^6C_1 \dots x$ or ${}^6C_2 \dots x^2$
Condone bracket errors or errors (or omissions) in the powers of 2.
Accept any notation for 6C_1 , 6C_2 , e.g. as on scheme or 6, and 15 from Pascal's triangle.
This mark may be given if no working is shown, if either or both of the terms including x is correct.
If the candidate attempts the expansion in descending powers allow ${}^6C_5 \dots x^5$ or ${}^6C_4 \dots x^4$ oe.
- In the alternative it is for the correct form inside the bracket accepting either $1 + 6 \times \frac{a}{2}x + \frac{6 \times 5}{2} \left(\frac{a}{2}x\right)^2$
or $1 + 6 \times \frac{a}{2}x + \frac{6 \times 5}{2} \frac{a}{2}x^2$
- B1 Must be simplified to 64 (writing just 2^6 is B0).
- A1 Score for either of $192ax$ or $240a^2x^2$ correct. Allow $240a^2x^2$ appearing as $240(ax)^2$ with the bracket
- A1 Score for both of $192ax$ and $240a^2x^2$ correct. Allow $240a^2x^2$ appearing as $240(ax)^2$ with the bracket
Allow listing of terms 64, $192ax$, $240a^2x^2$ for all 4 marks.
- (b)**
- M1 Score for setting the coefficients of their x and x^2 terms equal. They must reach an equation not involving x 's.
A1 This is also for any equivalent fraction or decimal to 0.8. Ignore any reference to $a=0$.