

Qu	Scheme	Marks	AO
2. (a)	From [5,20) fd = 3 <u>or</u> 1 large square = 2.5 passengers o.e.	M1	2.2a
	Correct bar above [0, 5)	A1	1.1b
	Correct bar above [20, 40)	A1	1.1b
			(3)
	(b) For [40, 65) <b>130</b> passengers <u>or</u> for [65, 80) <b>60</b> passengers	M1	2.1
	For attempt to find total number of passengers = <b>331</b>	A1ft	1.1b
	[Median = ] $40 + \frac{\frac{1}{2}("331") - 140}{"130"} \times 25$ <u>or</u> $65 - \frac{270 - \frac{1}{2}("331")}{"130"} \times 25$ (o.e.)	M1	1.1b
	$= 44.9038\dots = \text{awrt } \underline{\underline{44.9}}$	A1	1.1b
			(4)
	(c) Upper outlier limit = $58.9 + 1.5 \times (58.9 - 27.3) = 106 (.3) > 90$ So oldest passenger is <u>not</u> an outlier	M1 A1	2.4 2.2a
		(2)	
		<b>(9 marks)</b>	
<b>Notes</b>			
(a)	M1 for attempt at fd or a suitable method to deduce the scale for the histogram May be implied by one correct bar. 1 <sup>st</sup> A1 for first bar [0, 5) with fd = 1 <u>or</u> 2 large squares high 2 <sup>nd</sup> A1 for third bar with fd = 4.5 <u>or</u> 9 large squares high		
(b)	1 <sup>st</sup> M1 for an attempt using their fd to find the missing frequencies. May be in table 1 <sup>st</sup> A1ft for a clear attempt to find the total number of passengers (ft their 130 and 60) 2 <sup>nd</sup> M1 for any expression/equation leading to correct $Q_2$ Must be using 40-65 class 2 <sup>nd</sup> A1 for awrt 44.9 (allow $(n + 1)$ leading to 45)		
(c)	M1 for finding the upper outlier limit ( expression or awrt 106 ) <u>and</u> stating or implying $> 90$ A1 dep on M1 seen for deducing NOT an outlier		

Qu	Scheme	Marks	AO
4 (a)	$\bar{x} = 10.2$ (2222...) <u>10.2</u>	awrt (1)	B1 1.1b
(b)	$\sigma_x = 3.17$ (20227...) <u>3.17</u> Sight of "knots" <u>or</u> "kn" (condone knots/s etc)	awrt (2)	B1ft 1.1b B1 1.2
(c)	October ..... since it is windier in the autumn <u>or</u> month of the hurricane <u>or</u> latest month in the year	(2) B1 B1	2.2b 2.4
(d)(i)	They represent <u>outliers</u>	(2) B1	1.2
(ii)	$Y$ has low median so expect lowish mean (but outlier so $> 7$ ) <u>and</u> $Y$ has big range/IQR or spread so expect larger st.dev Suggests $B$	M1 A1 (3)	2.4 2.2b
<b>(8 marks)</b>			
<b>Notes</b>			
NB	$\bar{x} = \frac{184}{18}$ and $\sigma_x = \sqrt{\frac{2062}{18} - \bar{x}^2}$		
(a)	B1 for $\bar{x} = 10.2$ (allow exact fraction)		
(b)	1 <sup>st</sup> B1ft allow 3.2 from a correct expr' accept $s = 3.26(3984...)$ [ft use of n/a] <u>Treating n/a as 0</u> May see $n = 31$ or $\bar{x} = 5.9354...$ which is B0 in (a) but here in (b) it gives $\sigma_x = 5.59(34...)$ or $s = 5.6858...$ (awrt 5.69) and scores 1 <sup>st</sup> B1 2 <sup>nd</sup> B1 accept kn accept in (a) or (b) (allow nautical miles/hour)		
(c)	1 <sup>st</sup> B1 choosing October but accept September. 2 <sup>nd</sup> B1 for stating that (Camborne) is windier in autumn/winter months "because it is winter/autumn/windier/colder in "month" " Sep $\leq$ "month" $\leq$ Mar scores B1B1 for "month" = Sep or Oct and B0B1 for other months in range		
(d)(i)	B1 for outlier or the idea of an extreme value allow "anomaly"		
(ii)	M1 for a comment relating to location that mentions both median and mean <u>and</u> a comment relating to <u>spread</u> that mentions both range/IQR and standard deviation and leads to choosing $B, C$ or $D$		

Question	Scheme	Marks	AOs
4 (a)	Tr(ace) (data needs to be converted to numbers before the calculation can be carried out)	B1	2.4
		(1)	
(b)	$[1+] \frac{138-131}{24} \times 4$	M1	2.1
	= 2.1666.... awrt <b>2.17</b>	A1	1.1b
		(2)	
(c)	$\sigma = \sqrt{\frac{7704.1875}{184} - \left(\frac{539.75}{184}\right)^2} = 5.7676... \quad \sigma = \text{awrt } \underline{5.77}$	M1 A1	1.1b 1.1b
		(2)	
(d)(i)	Using class midpoints to estimate the mean assumes that the values are uniformly distributed <b>within the class(es)</b> .	B1	2.4
(ii)& (iii)	This is not the case here as the majority of the data (in the first class) are 0.	B1	2.3
	The actual mean is likely to be <u>smaller</u> than the estimate (since the first group has more values at 0 and close to 0)	dB1	2.2b
		(3)	
<b>(8 marks)</b>			
<b>Notes</b>			
(a)	<b>B1:</b> Identifying tr(ace) data Ignore comments about n/a, missing data, anomalies, etc.		
(b)	<b>M1:</b> Correct fraction $\frac{7}{24} \times 4$ allow working down $[5] - \frac{155-138}{24} \times 4$ allow a correct equation leading to a correct fraction e.g. $\frac{x-1}{5-1} = \frac{138-131}{155-131}$ for M1 Use of $(n + 1)$ with 138.75 allow $\frac{7.75}{24} \times 4$ <b>A1:</b> awrt 2.17 (condone $\frac{13}{6}$ ) awrt 2.29 from $(n + 1)$ (condone $\frac{55}{24}$ )		
(c)	<b>M1:</b> Correct expression for standard deviation (allow mean = awrt 2.93) <b>A1:</b> awrt 5.77 correct answer only scores M1A1 (allow $s = 5.78$ ) <b>SC:</b> 5.76 with no working scores M1A0		
(d)(i)	<b>B1:</b> Explaining that data assumed to be spread evenly across each class (o.e.) e.g. The midpoint of each class is the <u>mean</u> of each class or all the values in the class are located at the midpoint condone normally distributed within each class		
<b>Mark together (ii)&amp;(iii)</b>	<b>B1:</b> Demonstrating an understanding of the LDS that the majority of data values (in the first class) are at 0 or close to 0 (trace). <b>dB1:</b> (dependent upon 2 <sup>nd</sup> B1) Correct inference based on knowledge of the LDS <b>SC:</b> If B1 is scored in (i) for ‘The data are spread evenly across each class,’ then in (ii) ‘The data are not evenly distributed in the classes’ scores B1 but in (iii) ‘the actual mean is smaller’ with no further justification scores B0		

Question	Scheme	Marks	AOs
<b>1</b>	1 square is $\frac{78}{12 \times 3 + 3 \times 4 + 2 \times 2} = \left[ \frac{78}{52} = 1.5 \right]$ and $(8 \times 1 + 1 \times 8) \times "1.5"$	M1	3.1a
	<b>24</b> students took less than 11 minutes	A1	1.1b
	Percentage of students = $\frac{"24"}{78 + "24" + 1 \times 8 \times "1.5" + 3 \times 4 \times "1.5"} \times 100$	M1	3.1b
	= 18.18... awrt 18%	A1	1.1b
		(4)	
<b>Total 4</b>			
Notes			
<b>1</b>	<b>M1:</b>	For clear use of frequency density to establish the fd scale and then use the area to find frequency of <11 minutes. Allow maximum of 3 errors in either the heights or widths in total if working shown. They may calculate the area using other size squares. Allow for realising they need to find the total number of squares (88) maximum of 4 errors in either the heights or widths and number < 11 minutes(16) - must have a maximum of 1 error in either the heights or widths (and not use the 78 as part of calculation)	
	<b>A1:</b>	For correct values seen. Allow for 88 and 16	
	<b>M1:</b>	For realising the need to find the total and calculating a percentage. ( with "their 24" as the numerator). Allow $(8 \times 1 + 2 \times 8) \times "1.5"$ instead of $"24" + 1 \times 8 \times "1.5"$ If working shown can allow maximum of 2 errors in either the heights or widths in the calculation of the total. Allow "their 24" / 132 oe	
	<b>A1:</b>	awrt 18	

Question	Scheme	Marks	AOs
4(a)	It is not possible to have a sampling frame	B1	2.3
		(1)	
(b)	Quota sampling <b>and</b> (catch 85 common carp, 45 mirror carp and 30 leather carp) <b>or</b> (ignore any fish caught of a type where the quota is full)	M1	1.1a
	Quota sampling <b>and</b> catch 85 common carp, 45 mirror carp and 30 leather carp <b>and</b> ignore any fish caught of a type where the quota is full	A1	1.1b
		(2)	
(c)	$\sigma = \sqrt{\frac{3053}{160} - \left(\frac{692}{160}\right)^2}$	M1	1.1b
	= 0.6129... awrt 0.613	A1	1.1b
		(2)	
(d)(i)	This would have no effect as the piece of data would remain in the same class	B1	2.2a
(ii)	This would increase the standard deviation as change in mean is small and $6.4 - 4.6 \approx 3\sigma$ therefore estimate of standard deviation will increase	B1	2.2a
		(2)	
<b>(7 marks)</b>			
<b>Notes</b>			
(a)	<b>B1:</b>	For the idea there cannot be a sampling frame/list	
(b)	<b>M1:</b>	Quota sampling <b>and</b> either for the correct numbers of each type <b>or</b> for the idea that if quota full ignore the fish.	
	<b>A1:</b>	Quota sampling <b>and</b> both the correct numbers of each type <b>and</b> for the idea that if quota full ignore the fish or sample until all quotas are full	
(c)	<b>M1:</b>	A correct expression for $\sigma$	
	<b>A1:</b>	Awrt 0.613 allow $s = \text{awrt } 0.615$	
(d)	<b>B1:</b>	Correct deduction with suitable explanation Allow range for class. Do not allow there is no differences	
	<b>B1:</b>	Correct deduction with suitable explanation. so would increase the standard deviation and a suitable reason. Allow the value is bigger than any others in the table <b>oe</b>	

## Paper 2: Statistics and Mechanics Mark Scheme

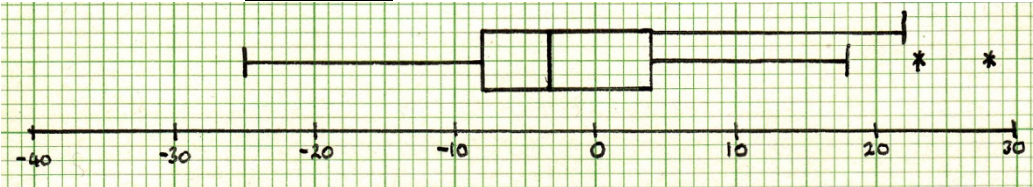
Question	Scheme	Marks	AOs
1(a)	Systematic (sample) cao	B1	1.2
(b)	In LDS some days have gaps because the data was not recorded	B1	2.4
(c)	$\left[ \bar{t} = \frac{374}{20} = 18.7 \right]$ $\sigma_t = \sqrt{\frac{7600}{20} - \bar{t}^2} \quad [ = \sqrt{30.31} ]$	M1	1.1a
	$= 5.5054... \quad \text{awrt } \underline{5.51}$ (Accept use of $s_t = \sqrt{\frac{7600 - 20\bar{t}^2}{19}} = 5.6484...$ )	A1	1.1b
<b>(4 marks)</b>			
<b>Notes:</b>			
(b)	<b>B1:</b> A correct explanation		
(c)	<b>M1:</b> For a correct expression for $\bar{t}$ and $\sigma_t$ or $s_t$ ft an incorrect evaluation of $\bar{t}$		
(c)	<b>A1:</b> For $\sigma_t =$ awrt 5.51 or $s_t =$ awrt 5.65		

Question	Scheme	Marks	AOs
2	$17 + 45 + \frac{1}{3} \times 9 \quad [ = 65 ]$	M1	2.2a
	$(7 - 8) \underline{14} \quad \text{or} \quad (16 - 20) \underline{5}$ [Values may be seen in the table]	M1 A1	3.1a 1.1b
	Percentage of motorists is $\frac{"65"}{6 + "14" + 17 + 45 + 9 + "5"} \times 100$	M1	3.1b
	$= \underline{67.7\%}$	A1	1.1b
<b>(5 marks)</b>			
<b>Notes:</b>			
(c)	<b>M1:</b> For a fully correct expression for the number of motorists in the interval		
(c)	<b>M1:</b> For clear use of frequency density in (4- 6) or (13- 15) cases to establish the fd scale. Then use of area to find frequency in one of the missing cases		
(c)	<b>A1:</b> For both correct values seen		
(c)	<b>M1:</b> For realising that total is required and attempting a correct expression for %		
(c)	<b>A1:</b> For awrt 67.7%		

## Paper 2: Statistics and Mechanics Mark Scheme

Question	Scheme	Marks	AOs
1(a)	Systematic (sample) cao	B1	1.2
(b)	In LDS some days have gaps because the data was not recorded	B1	2.4
(c)	$\left[ \bar{t} = \frac{374}{20} = 18.7 \right]$ $\sigma_t = \sqrt{\frac{7600}{20} - \bar{t}^2} \quad [ = \sqrt{30.31} ]$	M1	1.1a
	$= 5.5054... \quad \text{awrt } \underline{5.51}$ (Accept use of $s_t = \sqrt{\frac{7600 - 20\bar{t}^2}{19}} = 5.6484...$ )	A1	1.1b
<b>(4 marks)</b>			
<b>Notes:</b>			
(b)	<b>B1:</b> A correct explanation		
(c)	<b>M1:</b> For a correct expression for $\bar{t}$ and $\sigma_t$ or $s_t$ ft an incorrect evaluation of $\bar{t}$		
(c)	<b>A1:</b> For $\sigma_t =$ awrt 5.51 or $s_t =$ awrt 5.65		

Question	Scheme	Marks	AOs
2	$17 + 45 + \frac{1}{3} \times 9 \quad [ = 65 ]$	M1	2.2a
	$(7 - 8) \underline{14} \quad \text{or} \quad (16 - 20) \underline{5}$ [Values may be seen in the table]	M1 A1	3.1a 1.1b
	Percentage of motorists is $\frac{"65"}{6 + "14" + 17 + 45 + 9 + "5"} \times 100$	M1	3.1b
	$= \underline{67.7\%}$	A1	1.1b
<b>(5 marks)</b>			
<b>Notes:</b>			
(c)	<b>M1:</b> For a fully correct expression for the number of motorists in the interval		
(c)	<b>M1:</b> For clear use of frequency density in (4- 6) or (13- 15) cases to establish the fd scale. Then use of area to find frequency in one of the missing cases		
(c)	<b>A1:</b> For both correct values seen		
(c)	<b>M1:</b> For realising that total is required and attempting a correct expression for %		
(c)	<b>A1:</b> For awrt 67.7%		

Question Number	Scheme	Marks
<p>1. (a)</p> <p>(b)</p> <p>(c)</p> <p>(d)</p> <p>(e)(i)</p> <p>(ii)</p> <p>(f)</p>	<p>[Range =] <b>63</b></p> <p>[IQR =] <b>18</b></p> <p>[ <math>Q_2</math> = ] <math>(-8) + \frac{20}{33} \times 8</math> or <math>(0) - \frac{13}{33} \times 8</math> [NB <math>(n + 1)</math> will have 20.5 or 12.5]  <math>= -3.1515\dots</math> awrt <b>-3.15</b></p> <p>[<math>Q_3</math> =] mid-point of [0, 8] group so therefore = 4</p> <p>IQR = <math>4 - (-8) = 12</math> so upper limit is <math>4 + 1.5 \times 12 = \mathbf{22}</math>  lower limit is <math>-8 - 1.5 \times 12 = \mathbf{-26}</math></p> <p>So the outliers are <b>23 and 28</b></p>  <p>Interquartile range is smaller (12 compared to 18) or range is smaller (53 v 63)  Median is closer to zero ( - 3.15 is closer than 5)  So they <u>have</u> improved</p>	<p>B1 (1)</p> <p>B1 (1)</p> <p>M1 (2)</p> <p>A1 (2)</p> <p>B1cso (1)</p> <p>M1 (1)</p> <p>A1 (1)</p> <p>A1 (1)</p> <p>M1 (1)</p> <p>A1 (1)</p> <p>A1 (6)</p> <p>B1 (3)</p> <p>B1 (3)</p> <p>dB1 (3)</p> <p><b>[Total 14]</b></p>
<b>Notes</b>		
<p>(c)</p> <p>(d)</p> <p>(e)(i)</p> <p>(ii)</p> <p>(e)(ii)SC</p> <p>(f)</p>	<p>M1 for a correct fraction and <math>\times 8</math> (ignore end point)  A1 for awrt - 3.15 (allow use of <math>n + 1</math> leading to - 3.03 )  Accept <math>-\frac{104}{33}</math> if box plot is OK or 3sf value is quoted in (f)</p> <p>B1cso for a clear argument with no incorrect working seen.  Allow 4.14... from 7.25 for <math>(n + 1)</math> case</p> <p>M1 for at least one correct calculation e.g. <math>4 + 1.5(8 - (-4))</math> ( implied by one correct limit)  1<sup>st</sup> A1 for <u>one</u> correct limit  2<sup>nd</sup> A1 for <u>both</u> correct limits and the two correct outliers identified</p> <p>M1 for a box with 2 whiskers (one at each end)  1<sup>st</sup> A1 for - 8 and 4 and ft <math>Q_2</math> between them <u>and</u> lower whisker ending at - 25 <b>no</b> outliers  2<sup>nd</sup> A1 for upper whisker ending at 18 <b>or</b> 22 <u>and</u> 2 outliers marked at 23 and 28</p> <p>Two incorrect outliers in (e)(i), ft both A1s in (ii) using their outliers provided in [ - 25, 28]</p> <p>1<sup>st</sup> B1 for a statement about <u>range</u> or <u>IQR</u> saying that 2<sup>nd</sup> estimates are better  Allow range or IQR” has decreased” or “is smaller” o.e.  2<sup>nd</sup> B1 for a statement about <u>medians</u> saying that 2<sup>nd</sup> one is <u>closer to zero</u>  <u>Don't</u> allow “decreased” or “smaller” <u>unless</u> clearly using <math> \text{median} </math> or say e.g. <math>3.15 &lt; 5</math>  3<sup>rd</sup> dB1 dep on at least one other B1 for concluding that they <u>have improved</u> based on change in median <u>or</u> range/IQR. Must clearly state “improved” not just “yes”</p>	



Question	Scheme	Marks
<p><b>1. (a)</b></p> <p><b>(b)</b></p> <p><b>(c)</b></p> <p><b>(d)</b></p>	$[Q_2 =] \quad (59.5) + \frac{10}{22} \times 5$ $= 61.7727\dots$ <p style="text-align: right;">awrt <b><u>61.8</u></b></p> $[\bar{x} =] \frac{\sum fx}{50} = \frac{3085}{50}$ $= \mathbf{61.7}$ $[\sigma_x =] \sqrt{\frac{192102.5}{50} - \bar{x}^2} = \sqrt{35.16}$ $= 5.929586\dots$ <p style="text-align: right;">awrt <b><u>5.93</u></b></p> <p>[Interpolation from above]</p> $\frac{4.5}{10} \times 13 \quad (= 5.85)$ <p style="text-align: center;">So probability is <math>\frac{5.85}{50} = \mathbf{0.117}</math></p>	<p>M1</p> <p>A1</p> <p style="text-align: right;">(2)</p> <p>M1</p> <p>A1 cao</p> <p style="text-align: right;">(2)</p> <p>M1</p> <p>A1</p> <p style="text-align: right;">(2)</p> <p>M1</p> <p>A1 cao</p> <p style="text-align: right;">(2)</p> <p style="text-align: right;"><b>(8 marks)</b></p>
<b>Notes</b>		
<p><b>(a)</b></p> <p><b>(b)</b></p> <p><b>(c)</b></p> <p><b>(d)</b></p>	<p>M1 for a correct expression (oe) without endpoint. Allow “n+1” so e.g. <math>(59.5) + \frac{10.5}{22} \times 5</math></p> <p>Allow working down e.g. <math>(64.5) - \frac{12}{22} \times 5</math> Allow <math>\frac{m-59.5}{64.5-59.5} = \frac{25-15}{37-15}</math> oe for M1</p> <p>A1 for awrt 61.8 or, if (n + 1) is used, allow awrt 61.9</p> <p>M1 for a correct expression for the mean <math>\frac{49.5 \times 5 + 57 \times 10 + 62 \times 22 + 69.5 \times 13}{50}</math> <u>or</u></p> <p>an attempt at <math>\frac{\sum fx}{50}</math> with at least 3 correct products <u>or</u> <math>\frac{3000 \leq \sum fx \leq 3200}{50}</math></p> <p>A1 for 61.7 from correct working</p> <p>M1 for a correct expression including square root. Ft their 61.7. Allow use of s</p> <p>A1 for awrt 5.93 Allow <math>s = 5.989787\dots =</math> awrt 5.99</p> <p>M1 for <math>\frac{4.5}{10} \times 13</math> (use of interpolation to find the number of carrots weighing more than 70g) (may be implied by sight of 5.85 may also be implied by 50 – 44.15 (Allow 50 – 44 (=6) or 50 – 45 (=5) coming from 44.15 or 44.2 seen in working to score M1)</p> <p>A1 for an answer of 0.117</p> <p>Note: Use of normal distribution scores M0A0.</p>	

Question Number	Scheme	Marks
2.	$1.5 \times 12 = 18$ 20 people represented by 18 (cm <sup>2</sup> ) or 1 person is represented by 0.9 (cm <sup>2</sup> )  $x = \frac{20 \times 94.5}{18}$ oe $= 105$ (people)	M1  M1  A1cao (3) <b>Total 3</b>
<b>Notes</b>		
	1 <sup>st</sup> M1 for an attempt to relate area to frequency (e.g. $\frac{20}{18}$ or $\frac{18}{20}$ seen) 2 <sup>nd</sup> M1 for a correct expression/equation for total frequency e.g. $\frac{18}{20} = \frac{94.5}{x}$ A1 for 105cao	

Question	Scheme	Marks						
<b>8.(a)</b>	(Time is) <u>continuous</u>	B1 (1)						
<b>(b)</b>	40 people = 8 large squares/200 small squares 200 people = 40 large squares/1000 small squares 40/(21 – 11) or correct scale on f.d. axis $\frac{x}{40} = \frac{180}{200}$ or $\frac{x}{40} = \frac{7.2}{8}$ or $(21 - 18) \times 4 + (25 - 21) \times 6$  36 people (spent between 18 and 25 minutes shopping in the supermarket)	B1  M1  A1 (3)						
<b>(c)</b>	Median = $26 + \frac{[30]}{36} \times 5 =$ awrt <b>30.2</b>	M1A1 (2)						
<b>(d)</b>	$\sum fx = 16 \times 40 + 23.5 \times 30 + 28.5 \times 36 + 33.5 \times 40 + 38.5 \times 14 + 46 \times 20 + 61 \times 20$ $= 6390^{**}$	M1 A1cso (2)						
<b>(e)</b>	i $\bar{x} = \frac{6390}{200} = 31.95$ ii $\sigma = \sqrt{\frac{238430}{200} - 31.95^2} = \sqrt{171.3475} = 13.09$ (or $s = 13.122$ ) awrt <b>13.1</b>	B1  M1A1 (3)						
<b>(f)</b>	0.409... awrt <b>0.4</b>	B1 (1)						
<b>(g)</b>	<table border="1" data-bbox="300 1144 1315 1261"> <tr> <td>Method 1</td> <td>Method 2 (see note)</td> </tr> <tr> <td>(positive) skew or median <math>\neq</math> mean oe</td> <td>(almost) symmetric oe</td> </tr> <tr> <td>not a good decision</td> <td>a good decision</td> </tr> </table>	Method 1	Method 2 (see note)	(positive) skew or median $\neq$ mean oe	(almost) symmetric oe	not a good decision	a good decision	B1 dB1 (2) <b>Total 14</b>
Method 1	Method 2 (see note)							
(positive) skew or median $\neq$ mean oe	(almost) symmetric oe							
not a good decision	a good decision							
<b>Notes</b>								
<b>(a)</b>	Allow not discrete. Condone misspellings if intention of ‘continuous’ is clear.							
<b>(b)</b>	B1 for establishing a ratio (usually 5 or 1/5) between people and area <u>or</u> calculating f.d. (may be implied by M1) M1 for a correct ratio <u>or</u> expression using areas for the people from 18 to 25 A1 36 cao (Answer of 36 scores 3 out of 3).							
<b>(c)</b>	M1 for an attempt at the medians (should have 26, 36 and 5). If working down $31 - \frac{[6]}{36} \times 5$ A1 awrt 30.2 (can come from using $(n+1)$ )							
<b>(d)</b>	M1 for a correct expression for $\sum fx$ condone one incorrect product A1cso for 6390 and all correct							
<b>(e) (i)</b>	B1 31.95 or equivalent fraction							
<b>(ii)</b>	M1 for correct expression for standard deviation including root A1 awrt 13.1 (answer of awrt 13.1 scores 2 out of 2) [NB ( $s = 13.122$ )]							
<b>(g)</b>	1 <sup>st</sup> B1 for comment on skew (may be seen in part (f)). Method 1: skew or median $\neq$ mean Only allow method 2 if $ \text{their}(f)  < 0.45$ . Method 2: $\sim$ symmetric (any mention of correlation is B0) 2 <sup>nd</sup> dB1 for a correct compatible comment about the manager’s decision							

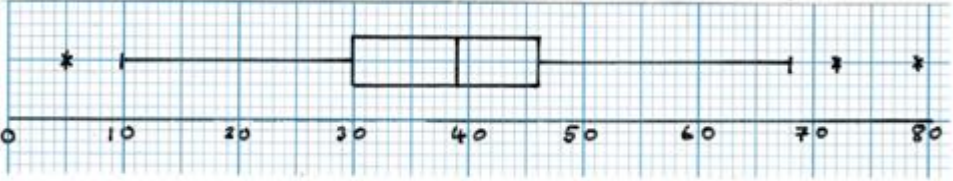
Question	Scheme	Marks
<p><b>2. (a)</b></p> <p><b>(b)</b></p> <p><b>(c)(i)</b></p> <p><b>(ii)</b></p> <p><b>(d)</b></p> <p><b>(e) (i)</b></p> <p><b>(ii)</b></p> <p><b>(iii)</b></p>	<p>Width = <math>\frac{5}{3} \times 1.5 = \underline{2.5 \text{ (cm)}}</math></p> <p>Area = <math>6 \times 1.5 = 9 \text{ cm}^2</math> has frequency = 12 so <math>1.5 \text{ cm}^2 = 2 \text{ people}</math> (o.e.)</p> <p>Frequency of 10 corresponds to area of 7.5 so height = <u><b>3 (cm)</b></u></p> <p><math>Q_2 = [2.5 + ] \frac{(25/25.5 - 16)}{12} \times 3 = 4.75</math> (or 4.875 if use <math>n + 1</math>) awrt <u><b>4.75</b></u></p> <p><math>[\bar{x} = ] \frac{394}{50} = 7.88</math> (*)</p> <p><math>[\sigma_x = ] \sqrt{\frac{6500}{50} - \bar{x}^2} = \sqrt{67.9056}</math></p> <p>= <u><b>awrt 8.24</b></u> (Accept <math>s =</math> awrt 8.32)</p> <p><math>\bar{x} &gt; Q_2</math></p> <p>So <u>positive</u> (skew)</p> <p>There is <u>no effect</u> on the mean</p> <p>The median will <u>increase</u></p> <p>The standard deviation will <u>decrease</u></p>	<p>B1</p> <p>M1</p> <p>A1 (3)</p> <p>M1 A1</p> <p>(2)</p> <p>B1cso</p> <p>M1A1</p> <p>A1 (4)</p> <p>B1ft</p> <p>dB1 (2)</p> <p>B1</p> <p>B1</p> <p>B1 (3)</p> <p><b>[14]</b></p>
<b>Notes</b>		
<p><b>(a)</b></p> <p><b>(b)</b></p> <p><b>(c)(i)</b></p> <p><b>(ii)</b></p> <p><b>(d)</b></p>	<p>M1 for forming a relationship between area and no. of people <u>or</u> “their width” <math>\times</math> “their height” = 7.5</p> <p><u>or</u> for <math>\frac{3h}{10} = \frac{9}{12}</math> oe</p> <p>A1 for height of 3 (cm)</p> <p>NOTE: the common incorrect answer width = 3 and height = 2.5 scores B0M1A0</p> <p>M1 for a correct fraction <math>[\frac{9}{12}</math> or <math>\frac{9.5}{12}] \times 3</math>. Ignore end point but must be +.</p> <p>May be seen in an equivalent expression e.g. <math>\frac{(x - 2.5)}{5.5 - 2.5} = \frac{25 - 16}{28 - 16}</math></p> <p>Allow use of <math>(n + 1)</math> giving 4.875</p> <p>NB May work down so look out for <math>[5.5] - \frac{28 - 25}{12} \times 3</math>, etc.</p> <p>B1 for <math>\frac{394}{50}</math> or for fully correct expression seen <math>\frac{16 \times 1.25 + 12 \times 4 + 10 \times 8 + 8 \times 15.5 + 4 \times 30.5}{50}</math></p> <p>M1 for a correct expression must have 6500, 50 and 7.88. (square root not necessary for M1)</p> <p>1<sup>st</sup> A1 for a correct expression which must have square root</p> <p>2<sup>nd</sup> A1 for awrt 8.24 (use of <math>s =</math> awrt 8.32). Condone incorrect labelling if awrt 8.24 is found.</p> <p>1<sup>st</sup> B1ft for a correct comparison of <math>\bar{x} = 7.88</math> and their <math>Q_2</math> (this may be seen embedded in another formula i.e. <math>3(\text{mean} - \text{median})/s.d.</math>)</p> <p><math>Q_3 - Q_2 &gt; Q_2 - Q_1</math> is B0 unless <math>Q_1</math> and <math>Q_3</math> have been found. (<math>Q_1 = 1.95/1.99</math>, <math>Q_3 = 10.25/10.81</math>)</p> <p>2<sup>nd</sup> dB1 Dependent on the 1<sup>st</sup> B1 and for concluding “positive” skew.</p> <p>Note: if their <math>Q_2 &gt; 7.88</math>, then B0. Positive correlation is B0.</p>	

Question Number	Scheme	Marks
<p><b>1. (a)</b></p> <p><b>(b)</b></p> <p><b>(c)</b></p> <p><b>(d)(i)</b></p> <p><b>(ii)</b></p> <p><b>(e)(i)</b></p> <p><b>(ii)</b></p> <p><b>(iii)</b></p>	<p><math>[61 \times 15 =] \underline{915}</math></p> <p><math>[\text{Var}_A] = \frac{59610}{10} - 77^2 = \underline{32}</math>      <math>[\text{Var}_B] = \frac{58035}{15} - 61^2 = \underline{148}</math></p> <p>Class <i>B</i> since its variance is larger</p> <p><math>\text{Mean}_{AB} = \frac{770 + "915"}{25} = 67.4</math>    or    <math>\frac{10}{25} \times 77 + \frac{15}{25} \times 61 = \underline{67.4}</math></p> <p><math>\text{Var}_{AB} = \frac{59\ 610 + 58\ 035}{25} - "67.4"{}^2 = 163.04</math>      awrt <u>163</u></p> <p>No effect on the variance of class <i>A</i> since addition does not change variance (<math>\text{Var}(X + b) = \text{Var}(X)</math>)</p> <p>The mean will increase since the <u>total score</u> has increased or mean of <i>A</i> increased but mean of <i>B</i> stayed the same</p> <p>The variance of the entire group will increase since the <u>mean of class <i>A</i></u> is now <u>further away from the mean of class <i>B</i></u></p>	<p><b>B1</b></p> <p><b>(1)</b></p> <p><b>M1</b></p> <p><b>A1 A1</b></p> <p><b>(3)</b></p> <p><b>B1ft</b></p> <p><b>(1)</b></p> <p><b>M1 A1</b></p> <p><b>M1 A1</b></p> <p><b>(4)</b></p> <p><b>B1</b></p> <p><b>B1</b></p> <p><b>B1</b></p> <p><b>(3)</b></p> <p><b>[12 marks]</b></p>
<b>Notes</b>		
<p><b>(b)</b></p> <p><b>(c)</b></p> <p><b>(d)(i)</b></p> <p><b>(ii)</b></p> <p><b>(e)(i)</b></p> <p><b>(ii)</b></p> <p><b>(iii)</b></p> <p><b>NB</b></p>	<p>M1 for a correct method for variance for either class. Accept <math>s^2</math> and allow inside <math>\sqrt{\dots}</math> 1<sup>st</sup> A1 for 1 correct answer. NB <math>s_A^2 = 35.5</math> or awrt 35.6 and <math>s_B^2 = 158.57\dots</math> or awrt 159 2<sup>nd</sup> A1 for both correct. [ISW standard deviations following correct variances.]</p> <p>B1ft for Class <i>B</i> <b>and</b> it has a larger variance/standard deviation (do not allow spread) If <math>\text{Var}_A &gt; \text{Var}_B</math> then allow choice of <i>A</i> since variance is larger. Ft their values if <math>&gt; 0</math></p> <p>M1 for a correct calculation for the mean (or weighted mean), ft their 915 from (a) A1 for 67.4 o.e.</p> <p>M1 for use of correct formula (no <math>\sqrt{\dots}</math>) with total <math>\sum x^2 = 117\ 645</math> and their mean. NB <math>\frac{S_{xx}}{25} = \frac{4076}{25}</math> A1 for awrt 163 [Don't ISW standard deviation]</p> <p>B1 for no effect/does not change <b>and</b> correct supporting reason that mentions addition or subtraction doesn't affect or only affected by multiplication/division. Comment that <math>(x - \bar{x})</math> doesn't change is fine. Just "coding" is not sufficient.</p> <p>B1 for stating the mean will increase <b>and</b> correct supporting reason that states or implies that total (of scores) has increased. Allow new mean = <math>\frac{1715}{25} = 68.6</math></p> <p>B1 for increase <b>and</b> correct supporting reason that mentions <u><i>A</i> marks</u> and <u><i>B</i> marks</u> and that they are <u>more spread</u> out. Just saying: "marks are more varied" or "only added 3 to one class" is <b>not</b> sufficient</p> <p>Calc for (iii) gives new <math>\Sigma x^2 = 64\ 320</math> and <math>\text{Var}_{AB} = 188.24</math> but no mark</p>	

## January 2017 WST01 Mark Scheme

Question Number	Scheme	Marks
1. (a)	25 small sq' = 5 tomatoes <u>or</u> 1 large square = 5 tomatoes <u>or</u> fd=5 for 2~3 <u>or</u> $\frac{5}{25} \times 20$ <u>or</u> $5 \times 0.8$ <u>or</u> $2 \times 2$ $= \underline{4}$	M1 A1 (2)
(b)	$100 - (5 + '4')$ <u>or</u> $16 + 32 + 25 + 10 + 8$ , so probability = $\frac{91}{100}$ (condone 91%)	M1, A1 (2)
(c)	$\frac{(7 - 6.25) \times 16 + 25 + 10 + 8}{100}$ <u>or</u> $1 - \frac{(a) + 5 + 16 + (6.25 - 5) \times 16}{100} = \frac{55}{100}$	M1, A1 (2)
(d)	Since '0.55' > 0.5 (or equivalent reason) <u>and</u> state median > 6.25	B1 (1)
(e)	Median > mean, so negative skew	B1 (1)
(f)	Freq. for $(5.5 < \text{weight} < 7) = (7 - 5.5) \times '16'$ or $\frac{3}{4} \times '32'$ , probability = $\frac{24}{100}$ P (both weigh between 5.5 and 7) = $\frac{24}{100} \times \frac{23}{99} = \frac{46}{825}$ (o.e.) <u>or</u> awrt <b>0.056</b>	M1, A1 M1 A1 (4)
<b>Notes</b>		
<b>A correct answer with no working scores M1A1 in parts (a)~(c)</b>		
(a)	M1 for a correct: statement linking area with frequency <u>or</u> calculation <u>or</u> at least 2 values on the fd scale on axis <u>or</u> at least 2 frequencies on/in histogram bars. A1 for an answer of 4 (if not in script, can be awarded if 4 seen correctly on histogram). If answers on both diagram and script contradict, the script has preference.	
(b)	M1 for $100 - (5 + '(a)')$ ft $0 < \text{'their (a)'} < 10$ <u>or</u> for a correct method for finding the sum of the areas of all the bars above 3 (condone one slip if 5 terms seen)	
(c)	M1 fully correct expression (possibly ft their (a)) and need division by 100 (o.e.) A1 for $\frac{11}{20}$ or 0.55 (o.e.) [Allow 55% or ratio 55:100]	
(d)	B1 for $Q_2 > 6.25$ with reason based on (c) where $0.5 < \text{'their (c)'} < 1$ [comparison of "55" & 50]	
(e)	B1 for stating "median > mean" <u>and</u> "negative skew" (independent of (d))	
(f)	1 <sup>st</sup> M1 for method to find the frequency between 5.5 and 7 (Implied by the 24 used) e.g. $(4 + 5 + 16 + 16 \times 2) - (4 + 5 + 16 + 16 \times 0.5) = 57 - 33$ based on $(\leq 7) - (\leq 5.5)$ 1 <sup>st</sup> A1 for $\frac{24}{100}$ (o.e.) 2 <sup>nd</sup> M1 for $\frac{'24'}{100} \times \frac{'24'-1}{99}$ ft their 24 but must have numerator < denominator of $100 \times 99$ 2 <sup>nd</sup> A1 for $\frac{46}{825}$ (o.e.) or awrt 0.056 NB $\frac{24}{100} \times \frac{24}{100}$ scores M1A1M0A0 [0.0576 alone 0/4]	

[12 marks]

Question Number	Scheme	Marks
2.(a)	[pass for] <b>30</b> (labelled or 1 <sup>st</sup> answer)	B1 (1)
(b)	[merit for] <b>46</b> (labelled or 2 <sup>nd</sup> answer)	B1 (1)
(c)	$[1.5(Q_3 - Q_1) = 1.5 \times 16 = 24]$ so $c = \underline{70}$ and $d = \underline{6}$	B1, B1 (2)
(d)	<b>68, 72, 79</b>	B2/1/0 (2)
(e)	$5 < d$ therefore 5 is an outlier	M1
		A1
		A1
		(3)
(f)	$\frac{1}{2} \times \left(\frac{1}{4}\right)^2 \times 3$ $= \underline{\underline{\frac{3}{32}}}$	M1M1
		A1
		(3)
		<b>[12 marks]</b>

**Notes**

(c)	<b>In (a), (b), (c) and (d) condone correct numbers with % e.g. 30% for (a)</b> 1 <sup>st</sup> B1 for $c = 70$ 2 <sup>nd</sup> B1 for $d = 6$ (Allow B1B1 for unlabelled 70 followed by 6) Award B1B0 for $c = 6$ and $d = 70$ or 6 and 70 in the wrong order	SC
(d)	B2 for all 3 correct values (and no extra value) (B1 for two correct)	
(e)	<b>Fully correct box plot scores M1A1A1</b> M1 for identifying or stating( e.g. on the grid) that 5 is the only outlier <u>or</u> lower whisker ending at 6 or 10 (May be implied by a correct diagram) 1 <sup>st</sup> A1 for only <u>one</u> outlier correctly marked at 5 (whisker(s) must stop <u>above</u> 5) 2 <sup>nd</sup> A1 for a <u>single</u> lower whisker stopping at 10 (2 whiskers is A0 here) Condone 15 marked (e.g. dash or cross) on an otherwise correct whisker If the outlier is at 5 and lower whisker ends at 6 award M1A1A0	
(f)	1 <sup>st</sup> M1 for $\frac{1}{2} \times \left(\frac{1}{4}\right)^2$ 2 <sup>nd</sup> M1 for an expression of the form $pq^2 \times 3$ where $p$ and $q$ are probabilities ( $p \neq q$ ) NB $\frac{3}{4} \times \left(\frac{1}{4}\right)^2 \times 3 = \frac{9}{64} = 0.140625$ is a common incorrect answer and scores M0M1A0	
	Can award M0M1A0 if <u>just</u> $\frac{9}{64}$ (o.e.) is seen.	SC
	A1 for $\frac{3}{32}$ or exact equivalent. Allow 0.0937 or 0.0938 following a correct expression.	
<b>Warning</b>	$2 \times (0.25)^2 \times (0.75)$ or $2 \times \left(\frac{1}{4}\right)^2 \times \frac{3}{4}$ gives the correct answer but is M0M0A0	

Question Number	Scheme	Marks
8. (a)	Total area of bars = 400 small squares Area required = $40 \times 4 + 20 \times 6 + 6 \times 10 = 340$ small squares No of staff = $340 \times \frac{40}{400} = 34$	B1 B1 M1, A1 (4)
(b)	Median is $(2+) \frac{4}{12} \times 3 = 3$ or $(5-) \frac{8}{12} \times 3 = 3$	M1A1 (2)
(c)	Mean is $\frac{\sum fx}{40} = \frac{1 \times 16 + 3.5 \times 12 + 7.5 \times 6 + 15 \times 4 + 25 \times 2}{40} = \frac{213}{40} = 5.325$	M1,A1 (2)
(d)	(Positive) skew but not negative or there are outliers (which affect mean) Median	B1 dB1 (2)
<b>Total 10</b>		
<b>Notes</b>		
(a)	<p>1<sup>st</sup> B1 for a correct attempt to calculate the whole area (400 small squares o.e.)            Accept <math>160+120+60+40+20</math> or <math>80+60+30+20+10=200</math> or frequencies: <math>16 + 12 + 6 + 4 + 2</math>            or <math>\text{cm}^2</math> <math>6.4 + 4.8 + 2.4 + 1.6 + 0.8 = 16</math> or key: 10 small squares = 1 person (o.e.)            2<sup>nd</sup> B1 for a correct attempt to calculate required area (Accept <math>160 + 120 + 60</math>)            or frequencies: <math>16 + 12 + 6</math> or <math>\text{cm}^2</math> <math>6.4 + 4.8 + 2.4 = 13.6</math>            M1 for a correct expression using their 400 and their 340            A1 for 34            If using frequencies they get M1A1 together when 34 is seen.            An answer of 34 will usually score 4/4 unless there is incorrect working seen</p> <p><b>NB frequencies are: 16, 12, 6, 4, 2 and mid-points are: 1, 3.5, 7.5, 15, 25</b></p>	
(b)	<p>M1 for <math>\frac{20-16}{12} \times (5-2)</math> or <math>\frac{20.5-16}{12} \times (5-2)</math> or similar expressions working down            Look out for methods based on areas should have <math>1^{\text{st}}</math> bar + <math>\frac{1}{3}(2^{\text{nd}}</math> bar) if working up or  <math>(5^{\text{th}} + 4^{\text{th}} + 3^{\text{rd}}</math> bars) + <math>\frac{2}{3}(2^{\text{nd}}</math> bar) if working down. E.g. <math>16 + 4(x-2) = 20</math>            A1 for 3 or (if using <math>n + 1</math> accept 3.125 or awrt 3.13)</p>	
(c)	<p>M1 for an attempt at <math>\frac{\sum fx}{40}</math> where at least 3 correct products of <math>\sum fx</math> are seen            or <math>\sum fx = \text{awrt } 200</math> (1 sf)            A1 for 5.325 or any exact equivalent e.g. <math>\frac{213}{40}</math> and accept 5.33            Accept 5 h 19 mins or 5h 20 mins</p>	
(d)	<p>1<sup>st</sup> B1 for a reason e.g. that the data is skewed            Allow mention of "extreme values" or "outliers"            Do not allow for <u>negative</u> skew or "anomalies"            2<sup>nd</sup> dB1 dependent on mentioning skew for choosing <u>median</u>            SC Allow B0B1 for "Choose median since the data has negative skew" o.e.</p>	