

1. A van of mass 600 kg is moving up a straight road inclined at an angle θ to the horizontal, where $\sin \theta = \frac{1}{16}$. The resistance to motion of the van from non-gravitational forces has constant magnitude R newtons. When the van is moving at a constant speed of 20 m s^{-1} , the van's engine is working at a constant rate of 25 kW.

(a) Find the value of R .

(4)

The power developed by the van's engine is now increased to 30 kW. The resistance to motion from non-gravitational forces is unchanged. At the instant when the van is moving up the road at 20 m s^{-1} , the acceleration of the van is $a \text{ m s}^{-2}$.

(b) Find the value of a .

(4)



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Q1

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2. A ball of mass 0.4 kg is moving in a horizontal plane when it is struck by a bat. The bat exerts an impulse $(-5\mathbf{i} + 3\mathbf{j})$ N s on the ball. Immediately after receiving the impulse the ball has velocity $(12\mathbf{i} + 15\mathbf{j})$ m s $^{-1}$.

Find

- (a) the speed of the ball immediately before the impact,

(4)

- (b) the size of the angle through which the direction of motion of the ball is deflected by the impact.

(3)



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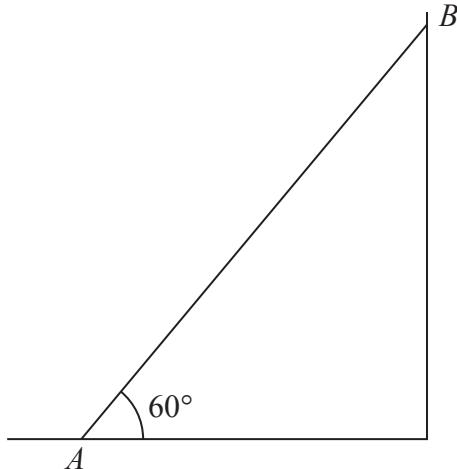


Figure 1

A non-uniform rod, AB , of mass m and length $2l$, rests in equilibrium with one end A on a rough horizontal floor and the other end B against a rough vertical wall. The rod is in a vertical plane perpendicular to the wall and makes an angle of 60° with the floor as

shown in Figure 1. The coefficient of friction between the rod and the floor is $\frac{1}{4}$ and the coefficient of friction between the rod and the wall is $\frac{2}{3}$. The rod is on the point of slipping at both ends.

- (a) Find the magnitude of the vertical component of the force exerted on the rod by the floor. (5)

The centre of mass of the rod is at G .

- (b) Find the distance AG . (5)



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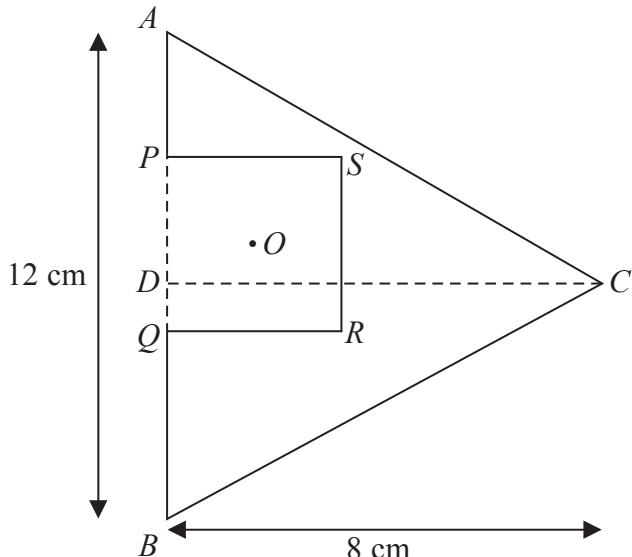


Figure 2

Figure 2 shows a lamina L . It is formed by removing a square $PQRS$ from a uniform triangle ABC . The triangle ABC is isosceles with $AC = BC$ and $AB = 12 \text{ cm}$. The midpoint of AB is D and $DC = 8 \text{ cm}$. The vertices P and Q of the square lie on AB and $PQ = 4 \text{ cm}$. The centre of the square is O . The centre of mass of L is at G .

- (a) Find the distance of G from AB .

(4)

When L is freely suspended from A and hangs in equilibrium, the line AB is inclined at 25° to the vertical.

- (b) Find the distance of O from DC .

(6)



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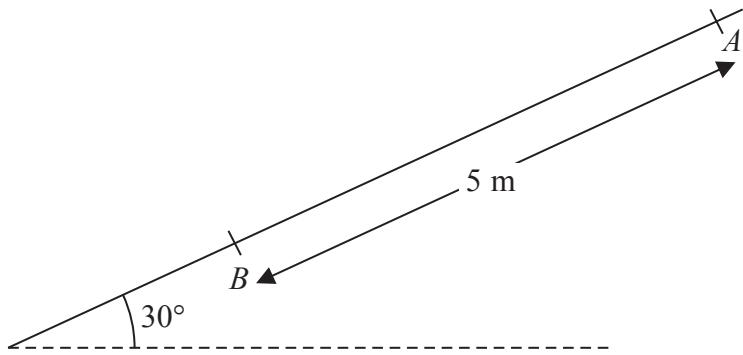


Figure 3

A particle P of mass 2 kg is released from rest at a point A on a rough inclined plane and slides down a line of greatest slope. The plane is inclined at 30° to the horizontal. The point B is 5 m from A on the line of greatest slope through A , as shown in Figure 3.

- (a) Find the potential energy lost by P as it moves from A to B .

(2)

The speed of P as it reaches B is 4 m s^{-1} .

- (b) (i) Use the work-energy principle to find the magnitude of the constant frictional force acting on P as it moves from A to B .

(ii) Find the coefficient of friction between P and the plane.

(7)

The particle P is now placed at A and projected down the plane towards B with speed 3 m s^{-1} . Given that the frictional force remains constant,

- (c) find the speed of P as it reaches B .

(4)



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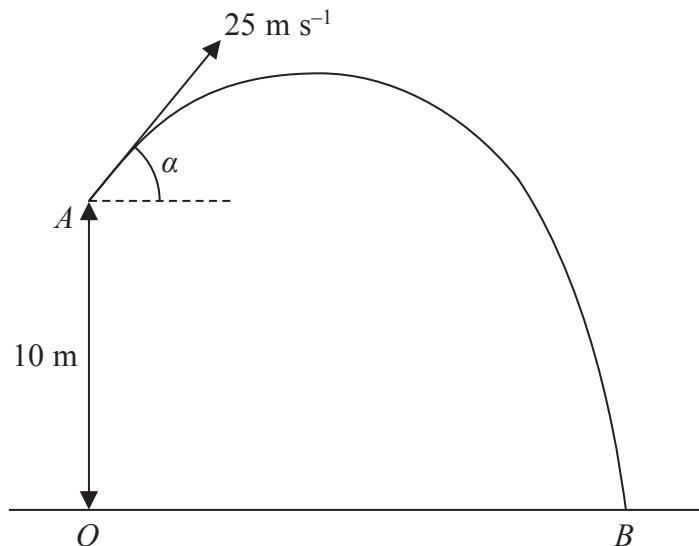
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6.

**Figure 4**

A particle P is projected from a point A with speed 25 m s^{-1} at an angle of elevation α , where $\sin \alpha = \frac{4}{5}$. The point A is 10 m vertically above the point O which is on horizontal ground, as shown in Figure 4. The particle P moves freely under gravity and reaches the ground at the point B .

Calculate

- (a) the greatest height above the ground of P , as it moves from A to B , (3)

- (b) the distance OB . (6)

The point C lies on the path of P . The direction of motion of P at C is perpendicular to the direction of motion of P at A .

- (c) Find the time taken by P to move from A to C . (4)
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7. A particle P of mass $2m$ is moving in a straight line with speed $3u$ on a smooth horizontal table. A second particle Q of mass $3m$ is moving in the opposite direction to P along the same straight line with speed u . The particle P collides directly with Q . The direction of motion of P is reversed by the collision. The coefficient of restitution between P and Q is e .

(a) Show that the speed of Q immediately after the collision is $\frac{u}{5}(8e + 3)$ (6)

(b) Find the range of possible values of e . (4)

The total kinetic energy of the particles before the collision is T . The total kinetic energy of the particles after the collision is kT . Given that $e = \frac{1}{2}$

(c) find the value of k . (4)



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