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Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

AS MATHEMATICS

Paper 1

Wednesday 15 May 2019

Morning

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
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TOTAL	



J U N 1 9 7 3 5 6 1 0 1

Section AAnswer **all** questions in the spaces provided.

1 State the number of solutions to the equation $\tan 4\theta = 1$ for $0^\circ < \theta < 180^\circ$

Circle your answer.

[1 mark]

1

2

4

8

2 Dan believes that

for every positive integer n , at least one of $2^n - 1$ and $2^n + 1$ is prime.Which value of n shown below is a counter example to Dan's belief?

Circle your answer.

[1 mark] $n = 3$ $n = 4$ $n = 5$ $n = 6$ 

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3 It is given that $(x + 1)$ and $(x - 3)$ are two factors of $f(x)$, where

$$f(x) = px^3 - 3x^2 - 8x + q$$

3 (a) Find the values of p and q .

[3 marks]

3 (b) Fully factorise $f(x)$.

[2 marks]

Turn over ►



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4 Show that $\frac{\sqrt{6}}{\sqrt{3} - \sqrt{2}}$ can be expressed in the form $m\sqrt{n} + n\sqrt{m}$, where m and n are integers.

Fully justify your answer.

[4 marks]



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5 (a) Sketch the curve $y = g(x)$ where

$$g(x) = (x + 2)(x - 1)^2$$

[3 marks]

5 (b) Hence, solve $g(x) \leq 0$

[2 marks]

Turn over ►



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6 (a) (i) Show that $\cos \theta = \frac{1}{2}$ is one solution of the equation

$$6 \sin^2 \theta + 5 \cos \theta = 7$$

[2 marks]

6 (a) (ii) Find all the values of θ that solve the equation

$$6 \sin^2 \theta + 5 \cos \theta = 7$$

for $0^\circ \leq \theta \leq 360^\circ$

Give your answers to the nearest degree.

[2 marks]



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6 (b) Hence, find all the solutions of the equation

$$6 \sin^2 2\theta + 5 \cos 2\theta = 7$$

for $0^\circ \leq \theta \leq 360^\circ$

Give your answers to the nearest degree.

[2 marks]

Turn over for the next question

Turn over ►



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7

Given that $y \in \mathbb{R}$, prove that

$$(2 + 3y)^4 + (2 - 3y)^4 \geq 32$$

Fully justify your answer.

[6 marks]



8 Prove that the curve with equation

$$y = 2x^5 + 5x^4 + 10x^3 - 8$$

has **only one** stationary point, stating its coordinates.

[6 marks]

Turn over for the next question



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9 A curve cuts the x -axis at $(2, 0)$ and has gradient function

$$\frac{dy}{dx} = \frac{24}{x^3}$$

9 (a) Find the equation of the curve.

[4 marks]



- 10** On 18 March 2019 there were 12 hours of daylight in Inverness.
- On 16 June 2019, 90 days later, there will be 18 hours of daylight in Inverness.
- Jude decides to model the number of hours of daylight in Inverness, N , by the formula

$$N = A + B \sin t^\circ$$

where t is the number of days after 18 March 2019.

- 10 (a) (i)** State the value that Jude should use for A . **[1 mark]**

- 10 (a) (ii)** State the value that Jude should use for B . **[1 mark]**

- 10 (a) (iii)** Using Jude's model, calculate the number of hours of daylight in Inverness on 15 May 2019, 58 days after 18 March 2019. **[1 mark]**



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10 (a) (iv) Using Jude’s model, find how many days during 2019 will have at least 17.4 hours of daylight in Inverness.

[4 marks]

10 (a) (v) Explain why Jude’s model will become inaccurate for 2020 and future years.

[1 mark]

10 (b) Anisa decides to model the number of hours of daylight in Inverness with the formula

$$N = A + B \sin\left(\frac{360}{365}t\right)^\circ$$

Explain why Anisa’s model is better than Jude’s model.

[1 mark]

Turn over ►



Section BAnswer **all** questions in the spaces provided.

11 A ball moves in a straight line and passes through two fixed points, *A* and *B*, which are 0.5 m apart.

The ball is moving with a constant acceleration of 0.39 m s^{-2} in the direction *AB*.

The speed of the ball at *A* is 1.9 m s^{-1}

Find the speed of the ball at *B*.

Circle your answer.

[1 mark] 2 m s^{-1} 3.2 m s^{-1} 3.8 m s^{-1} 4 m s^{-1}

12 A particle *P*, of mass *m* kilograms, is attached to one end of a light inextensible string.

The other end of this string is held at a fixed position, *O*.

P hangs freely, in equilibrium, vertically below *O*.

Identify the statement below that correctly describes the tension, *T* newtons, in the string as *m* varies.

Tick (✓) **one** box.

[1 mark]

T varies along the string, with its greatest value at *O*

T varies along the string, with its greatest value at *P*

$T = 0$ because the system is in equilibrium

T is directly proportional to *m*



Turn over for the next question

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13 A car, starting from rest, is driven along a horizontal track.

The velocity of the car, $v \text{ m s}^{-1}$, at time t seconds, is modelled by the equation

$$v = 0.48t^2 - 0.024t^3 \text{ for } 0 \leq t \leq 15$$

13 (a) Find the distance the car travels during the first 10 seconds of its journey.

[3 marks]

13 (b) Find the maximum speed of the car.

Give your answer to three significant figures.

[4 marks]



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13 (c) Deduce the range of values of t for which the car is modelled as decelerating. **[2 marks]**

Turn over for the next question

Turn over ►



14 Two particles, A and B , lie at rest on a smooth horizontal plane.

A has position vector $\mathbf{r}_A = (13\mathbf{i} - 22\mathbf{j})$ metres

B has position vector $\mathbf{r}_B = (3\mathbf{i} + 2\mathbf{j})$ metres

14 (a) Calculate the distance between A and B .

[2 marks]

14 (b) Three forces, \mathbf{F}_1 , \mathbf{F}_2 and \mathbf{F}_3 are applied to particle A , where

$$\mathbf{F}_1 = (-2\mathbf{i} + 4\mathbf{j}) \text{ newtons}$$

$$\mathbf{F}_2 = (6\mathbf{i} - 10\mathbf{j}) \text{ newtons}$$

Given that A remains at rest, explain why $\mathbf{F}_3 = (-4\mathbf{i} + 6\mathbf{j})$ newtons

[1 mark]



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14 (c) A force of $(5i - 12j)$ newtons, is applied to B , so that B moves, from rest, in a straight line towards A .

B has a mass of 0.8 kg

14 (c) (i) Show that the acceleration of B towards A is 16.25 ms^{-2}

[2 marks]

14 (c) (ii) Hence, find the time taken for B to reach A .

Give your answer to two significant figures.

[2 marks]

Turn over ►



15 A tractor and its driver have a combined mass of m kilograms.

The tractor is towing a trailer of mass $4m$ kilograms in a straight line along a horizontal road.

The tractor and trailer are connected by a horizontal tow bar, modelled as a light rigid rod.

A driving force of 11 080 N and a total resistance force of 160 N act on the tractor.

A total resistance force of 600 N acts on the trailer.

The tractor and the trailer have an acceleration of 0.8 m s^{-2}

15 (a) Find m .

[3 marks]

15 (b) Find the tension in the tow bar.

[2 marks]



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