| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 8(a) | Multiply out and differentiate $w r t$ to time (or use of product rule i.e. must have two terms with correct structure) | M1 | 1.1a |
|  | $v=2 t^{3}-3 t^{2}+t$ | A1 | 1.1b |
|  | $2 t^{3}-3 t^{2}+t=0$ and solve: $t(2 t-1)(t-1)=0$ | DM1 | 1.1b |
|  | $t=0$ or $t=\frac{1}{2}$ or $t=1$; any two | A1 | 1.1b |
|  | All three | A1 | 1.1b |
|  |  | (5) |  |
| (b) | Find $x$ when $t=0, \frac{1}{2}, 1$ and $2:\left(0, \frac{1}{32}, 0,2\right)$ | M1 | 2.1 |
|  | Distance $=\frac{1}{32}+\frac{1}{32}+2$ | M1 | 2.1 |
|  | $2 \frac{1}{16}(\mathrm{~m})$ oe or 2.06 or better | A1 | 1.1b |
|  |  | (3) |  |
| (c) | $x=\frac{1}{2} t^{2}(t-1)^{2}$ | M1 | 3.1a |
|  | $\frac{1}{2}$ perfect square so $x \geq 0$ i.e. never negative | A1 cso | 2.4 |
|  |  | (2) |  |
| (10 marks) |  |  |  |
| Notes: |  |  |  |
| (a) <br> M1: Must have 3 terms and at least two powers going down by 1 <br> A1: A correct expression <br> DM1: Dependent on first M, for equating to zero and attempting to solve a cubic <br> A1: Any two of the three values (Two correct answers can imply a correct method) <br> A1: The third value |  |  |  |
| (b) <br> M1: For attempting to find the values of $x$ (at least two) at their $t$ values found in (a) or at $t=2$ or equivalent e.g. they may integrate their $v$ and sub in at least two of their $t$ values <br> M1: Using a correct strategy to combine their distances (must have at least 3 distances) |  |  |  |


| Question | Scheme | Marks | AOs | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 3(a) | $v=12+4 t-t^{2}=0$ and solving | M1 | 3.1a | Equating $v$ to 0 and solving the quadratic If no evidence of solving, and at least one answer wrong, M0 |
|  | $t=6$ (or -2) | A1 | 1.1b | 6 but allow -2 as well at this stage |
|  | Differentiate $v$ wrt $t$ | M1 | 1.1a | For differentiation (both powers decreasing by 1) |
|  | $\left(a=\frac{\mathrm{d} v}{\mathrm{~d} t}=\right) 4-2 t$ | A1 | 1.1b | Cao; only need RHS |
|  | When $t=6, a=-8$; Magnitude is $8\left(\mathrm{~m} \mathrm{~s}^{-2}\right)$ | A1 | 1.1b | Substitute in $t=6$ and get $8\left(\mathrm{~m} \mathrm{~s}^{-2}\right)$ as the answer . Must be positive. <br> (A0 if two answers given) |
|  |  | (5) |  |  |
| (b) | Integrate $v$ wrt $t$ | M1 | 3.1a | For integration (at least two powers increasing by 1) |
|  | $(s=) 12 t+2 t^{2}-\frac{1}{3} t^{3}(+C)$ | A1 | 1.1b | Correct expression (ignore $C$ ) only need RHS Must be used in part (b) |
|  | $t=3 \Rightarrow$ distance $=45(\mathrm{~m})$ | A1 | 1.1b | Correct distance. Ignore units |
|  |  | (3) |  |  |
| (8 marks) |  |  |  |  |


| Question |  | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: | :---: |
| 3(a) |  | $v=3 t-2 t^{2}+14$ and differentiate | M1 | 3.1a |
|  |  | $a=\frac{\mathrm{d} v}{\mathrm{~d} t}=3-4 t \quad$ or $\quad(7-2 t)-2(t+2)$ using product rule | A1 | 1.1b |
|  |  | $3-4 t=0$ and solve for $t$ | M1 | 1.1b |
|  |  | $t=\frac{3}{4}$ oe | A1 | 1.1b |
|  |  |  | (4) |  |
| 3(b) |  | Solve problem using $v=0$ to find a value of $t\left(t=\frac{7}{2}\right)$ | M1 | 3.1a |
|  |  | $v=3 t-2 t^{2}+14$ and integrate | M1 | 1.1b |
|  |  | $s=\frac{3 t^{2}}{2}-\frac{2 t^{3}}{3}+14 t$ | A1 | 1.1b |
|  |  | Substitute $t=\frac{7}{2}$ into their $s$ expression (M0 if using suvat) | M1 | 1.1b |
|  |  | $s=\frac{931}{24}=38 \frac{19}{24}=38.79166 . .(\mathrm{m}) \quad$ Accept 39 or better | A1 | 1.1b |
|  |  |  | (5) |  |
| (9 marks) |  |  |  |  |
| Notes: |  |  |  |  |
| (a) | M1 | Multiply out and attempt to differentiate, with at least one power decreasing |  |  |
|  | A1 | Correct expression |  |  |
|  | M1 | Equate their $a$ to 0 and solve for $t$ |  |  |
|  | A1 | cao |  |  |
| (b) | M1 | Uses $v=0$ to obtain a value of $t$ |  |  |
|  | M1 | Attempt to integrate, with at least one power increasing |  |  |
|  | A1 | Correct expression |  |  |
|  | M1 | Substitute in their value of $t$, which must have come from using $v=0$, into their $s$ (must have integrated) |  |  |
|  | A1 | 39 or better |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 8(a) | Substitution of both $t=0$ and $t=10$ | M1 | 2.1 |
|  | $s=0$ for both $t=0$ and $t=10$ | A1 | 1.1b |
|  | Explanation ( $s>0$ for $0<t<10$ ) since $s=\frac{1}{10} t^{2}(t-10)^{2}$ | A1 | 2.4 |
|  |  | (3) |  |
| (b) | Differentiate displacement $s$ w.r.t. $t$ to give velocity, $v$ | M1 | 1.1a |
|  | $v=\frac{1}{10}\left(4 t^{3}-60 t^{2}+200 t\right)$ | A1 | 1.1 b |
|  | Interpretation of 'rest' to give $v=\frac{1}{10}\left(4 t^{3}-60 t^{2}+200 t\right)=\frac{2}{5} t(t-5)(t-10)=0$ | M1 | 1.1 b |
|  | $t=0,5,10$ | A1 | 1.1b |
|  | Select $t=5$ and substitute their $t=5$ into $s$ | M1 | 1.1a |
|  | Distance $=62.5 \mathrm{~m}$ | A1ft | 1.1 b |
|  |  | (6) |  |
| (9 marks) |  |  |  |
| Notes: |  |  |  |
| (a) <br> M1: For substituting $t=0$ and $t=10$ into $s$ expression <br> A1: For noting that $s=0$ at both times <br> A1: $\quad$ Since $s$ is a perfect square, $s>0$ for all other $t$ - values |  |  |  |
| (b) <br> M1: For differentiating $s$ w.r.t. $t$ to give $v$ (powers of $t$ reducing by <br> A1: For a correct $v$ expression in any form <br> M1: For equating $v$ to 0 and factorising <br> A1: For correct $t$ values <br> M1: For substituting their intermediate $t$ value into $s$ <br> A1: ft following an incorrect $t$-value |  |  |  |

