

1. Three particles of mass $3m$, $2m$ and km are placed at the points whose coordinates are $(1, 5)$, $(6, 4)$ and $(a, 1)$ respectively. The centre of mass of the three particles is at the point with coordinates $(3, 3)$.

Find

(a) the value of k , **(3)**

(b) the value of a . **(3)**



3.

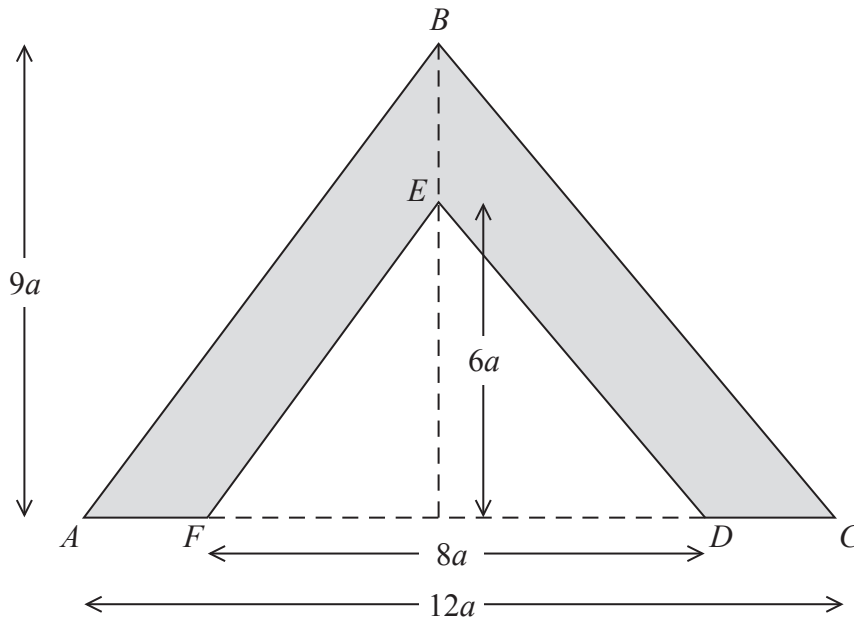


Figure 1

The uniform lamina $ABCDEF$, shown shaded in Figure 1, is symmetrical about the line through B and E . It is formed by removing the isosceles triangle FED , of height $6a$ and base $8a$, from the isosceles triangle ABC of height $9a$ and base $12a$.

(a) Find, in terms of a , the distance of the centre of mass of the lamina from AC . (5)

The lamina is freely suspended from A and hangs in equilibrium.

(b) Find, to the nearest degree, the size of the angle between AB and the downward vertical. (4)



6.

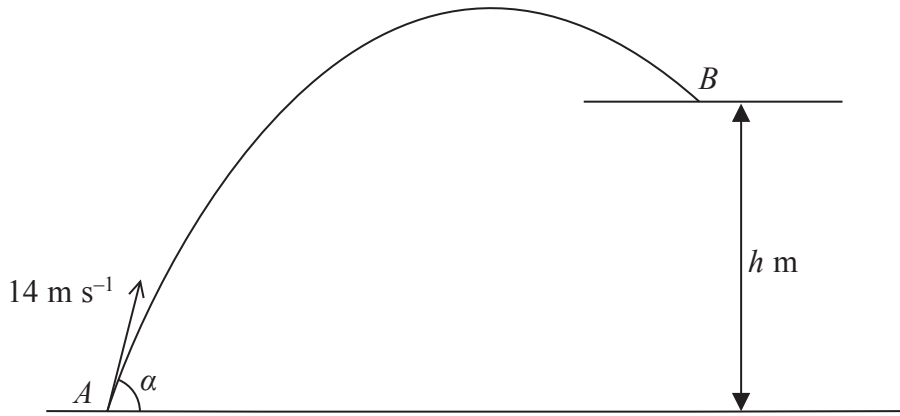


Figure 2

A small ball is projected with speed 14 m s^{-1} from a point A on horizontal ground. The angle of projection is α above the horizontal. A horizontal platform is at height h metres above the ground. The ball moves freely under gravity until it hits the platform at the point B , as shown in Figure 2. The speed of the ball immediately before it hits the platform at B is 10 m s^{-1} .

(a) Find the value of h . (4)

Given that $\sin \alpha = 0.85$,

(b) find the horizontal distance from A to B . (8)



7.

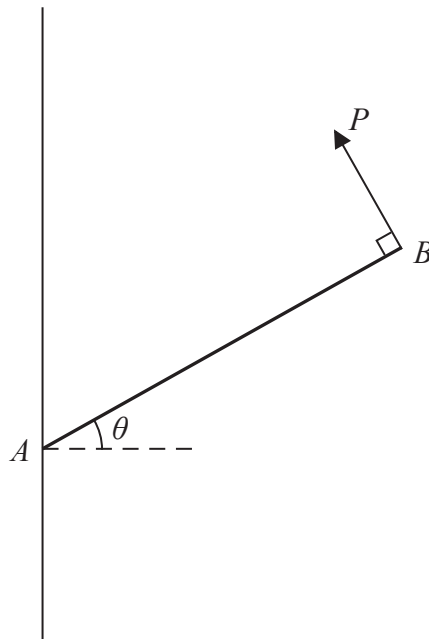


Figure 3

A uniform rod AB of weight W has its end A freely hinged to a point on a fixed vertical wall. The rod is held in equilibrium, at angle θ to the horizontal, by a force of magnitude P . The force acts perpendicular to the rod at B and in the same vertical plane as the rod, as shown in Figure 3. The rod is in a vertical plane perpendicular to the wall. The magnitude of the vertical component of the force exerted on the rod by the wall at A is Y .

(a) Show that $Y = \frac{W}{2}(2 - \cos^2 \theta)$. (6)

Given that $\theta = 45^\circ$

(b) find the magnitude of the force exerted on the rod by the wall at A , giving your answer in terms of W . (6)



8. The points A and B are 10 m apart on a line of greatest slope of a fixed rough inclined plane, with A above B . The plane is inclined at 25° to the horizontal. A particle P of mass 5 kg is released from rest at A and slides down the slope. As P passes B , it is moving with speed 7 m s^{-1} .

(a) Find, using the work-energy principle, the work done against friction as P moves from A to B . (4)

(b) Find the coefficient of friction between the particle and the plane. (5)



