

GCE

Mathematics B (MEI)

Unit H640/01: Pure Mathematics and Mechanics

Advanced GCE

Mark Scheme for June 2018

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, Cambridge Nationals, Cambridge Technicals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

© OCR 2018

Annotations and abbreviations

Annotation in scoris	Meaning
√and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations	Meaning
in mark scheme	
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
сао	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction In this question you must show detailed reasoning appears in the
	question.

Subject-specific Marking Instructions for A Level Mathematics B (MEI)

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Е

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results.
 Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
 Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

www.yesterdaysmathsexam.com Mark Scheme

i If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question	Answer	Marks	AOs		Guidance
1	EITHER $f(2) = 3 \times 2^3 - 8 \times 2^2 + 3 \times 2 + 2 = 24 - 32 + 6 + 2 = 0$ Therefore by the factor theorem $(x - 2)$ is a factor	M1 A1 E1 [3]	1.1a 1.1b 2.2a	AG Function notation need not be used Zero must be seen Reason required	
	OR $f(x) = (x-2)(3x^2 - 2x - 1)$ No remainder so $(x-2)$ is a factor	[5] M1 A1 E1 [3]		Using algebraic division as far as $3x^2$ Correct quotient Reason required	
2	When $x=0$ $e^0 - 5 \times 0^3 = 1 > 0$ When $x=1$ $e^1 - 5 \times 1^3 = e - 5 < 0$ So [as the function is continuous and there is a change of sign] there is a root between 0 and 1	M1 E1 [2]	1.1a 2.2a	Attempting to evaluate the function at both values Conclusion from correct values	
3	$(1 + \tan^2 \theta) + 2 \tan \theta = 4$ $\tan^2 \theta + 2 \tan \theta - 3 = 0$ $(\tan \theta - 1)(\tan \theta + 3) = 0$ When $\tan \theta = 1$, $\theta = 45^\circ$, 225° When $\tan \theta = -3$, $\theta = 108.4^\circ$, 288.4°	M1 M1 A1 A1 [4]	3.1a 1.1a 1.1b 1.1b	DR Using appropriate trig identity Showing algebraic method for solving their quadratic Any two correct values for θ All correct values for θ and no extras in the interval. Ignore values outside the required interval.	Must attempt to reach an equation with only one trig function eg $20\cos^4 \theta - 12\cos^2 \theta + 1 = 0$ Or $\sqrt{5}\sin(2\theta - 63.4^\circ) = 1$
4 (i)	$v^{2} = u^{2} + 2as$ $1.2^{2} = 2 \times a \times 1.8$ $a = 0.4 \text{ m s}^{-2}$	M1 A1 [2]	3.3 1.1b	Using suitable suvat equation(s) leading to value for <i>a</i>	

(Question	Answer	Marks	AOs		Guidance
	(ii)	F - 19 = 2.8a	M1	3.3	Using Newton's second law. All	
		F = 20.12 (20.1 N to 3sf)			terms present.	
			A1	1.1b	Allow 20 N FT their a	
			[2]			
5	(i)	$d\mathbf{r}$ (12, 2, 2)), (2, c).	M1	1.1a	Attempt to differentiate at least one	
	~ /	$\mathbf{v} = \frac{d\mathbf{r}}{dt} = (12 - 2 \times 2t)\mathbf{i} + (2t - 6)\mathbf{j}$			coefficient	
		ui	A1	2.5	Must use vector notation	
			[2]			
	(ii)	When $t = 3$ both components of velocity are zero,	M1	3.1a	Equating at least one component of	Do not allow M1 for solving
					their vector velocity to zero	12 - 4t = 2t - 6 unless at
						least one zero subsequently
		so the particle is stationary at $t = 3$.	E1	2.2a	Must be argued from two zero	established
		× 2	[2]		components	

(Question	Answer	Marks	AOs		Guidance
6	(i)	Arithmetic sequence with $a = 50$, $d = 20$ $S_{24} = \frac{24}{2} (2 \times 50 + (24 - 1)20)$ $= \pounds 6720$	M1	1.1 a	Using appropriate formula for sum of an arithmetic sequence with a = 50, d = 20	Allow for total written out in full
		$= \pm 0720$	A1 [2]	1.1b	Allow full credit for any correct method	
	(ii)	Each month is 12% more than the previous, so multiplied by 1.12 giving a geometric sequence with $a = 50$, $r = 1.12$	E1 [1]	2.4	Clear argument must include the value 1.12	
	(iii)	Geometric sequence with $a = 50$, $r = 1.12$ $S_{24} = \frac{50(1.12^{24} - 1)}{0.12}$	M1	3.1 a	Using appropriate formula for sum of a geometric sequence with a = 50, r = 1.12	Allow for total written out in full
		= £5907.76 which is less than Aleela	A1 E1 [3]	1.1b 2.1	Allow any suitable rounding FT their values (dep on earning the M marks in part (i) and (iii))	
7	(i)	F = 30 + 50 = 80 N	B1 [1]	1.1a	Сао	
	(ii)	Taking moments about the top of the rod $Fx = 50 \times 2$ x = 1.25 m	M1 A1 [2]	3.3 1.1b	Or any other suitable point Cao	All necessary terms must be present. Each term must be a product of a force and a length.

	Question	Answer	Marks	AOs		Guidance
8	(i)	EITHER $8\sin^2 x \cos^2 x = 2(1 - \cos 2x)(1 + \cos 2x)$	M1	3.1a	AG Using a double angle formula	
		$= 2(1 - \cos^2 2x) = 2 - (1 + \cos 4x)$	M1	3.1 a	Second use of a double angle formula	
		$=1-\cos 4x$	E1 [3]	2.1	Clearly shown	
	(i)	$OR 8 \sin^2 x \cos^2 x = 2(2\sin x \cos x)^2$	M1		Using a double angle formula	Allow any other valid sequence of identities used.
		$= 2\sin^2 2x [= 1 - \cos 2(2x)] = 1 - \cos 4x$	M1		Another use of a double angle formula	
			E1 [3]		Clearly shown	
	(i)	$OR 1 - \cos 4x = 1 - \left(1 - 2\sin^2 2x\right)$	M1		Using a double angle formula	
		$= 2\sin^2 2x$ $= 2(2\sin x \cos x)^2$	M1		Another use of a double angle formula	
		$=8\sin^2 x \cos^2 x$	E1 [3]		Clearly shown	
	(ii)	$\int \sin^2 x \cos^2 x dx = \frac{1}{8} \int 1 - \cos 4x dx$	M1	1.1a	Attempt to integrate both terms	
			A1	1.1b	$\frac{1}{4}\sin 4x$ seen or implied	
		$=\frac{1}{8}x - \frac{1}{32}\sin 4x + c$	A1 [3]	1.1b	All correct. Must include $+c$	

	Question	Answer	Marks	AOs		Guidance
9	(i)	Vertical motion $u = 0$ $s = ut + \frac{1}{2}at^2$	B1	3.3	Using $u = 0$ in the vertical direction to model horizontal motion soi	
		$-5 = 0 - \frac{9.8}{2}t^2$	M1	3.4	Using suvat equation(s) to find <i>t</i> . Allow sign errors and incorrect value for <i>u</i> .	
		$t = \sqrt{\frac{10}{9.8}} = 1.01 \text{ s}$	A1 [3]	1.1b	Must follow from working where the signs are consistent.	
	(ii)	x = 14t $y = 5 - 4.9t^{2}$	B1 B1	3.3 3.3	May be implied May be implied	
		So cartesian equation is $y = 5 - 4.9 \left(\frac{x}{14}\right)^2 \left[=5 - \frac{x^2}{40}\right]$	M1 A1 [4]	1.1a 1.1b	Attempt to eliminate <i>t</i> Any form	
	(iii)	EITHER When $y = 2$ $y = 5 - \frac{x^2}{40} = 2$ m $\frac{x^2}{40} = 3$	M1	3.4	Using their equation of trajectory and $y = 2$	SC2 for $d < \sqrt{80}$ [= 8.94] SC1 for $d = \sqrt{80}$ [= 8.94]
		$x = \sqrt{120} = 10.9544$ [0<] $d < 11.0$ m	A1 E1 [3]	1.1b 3.2a	Must be 11.0 or better Allow "Fence must be less than 10.95 m from the origin." FT their value	
	(iii)	OR When $y = 2 \ 2 = 5 - 4.9t^2$ t = 0.782 When $t = 0.782 \ x = 14 \times 0.782 = 10.95$ [0 <]d < 11.0 m	M1 A1 A1 [3]		Both steps required for M1 Must be 11.0 or better Allow "Fence must be less than 10.95 m from the origin."	Allow if the origin is taken to be at window height and the top of the wall is 3m below the window. Signs must be consistent for A1

www.yesterdaysmathsexam.com Mark Scheme

Question	Answer	Marks	AOs		Guidance
10	Curve crosses the x-axis when $y=0$ $y = (k - x) \ln x = 0$	M1	3.1 a	Attempt to solve $y = 0$	
	Either $k - x = 0$ or $\ln x = 0$ x = k or 1 EITHER	A1	1.1b	Both roots required	
	Area = $\int_{1}^{k} (k-x) \ln x dx$ Let $u = \ln x$, $\frac{dv}{dx} = k - x$, $\frac{du}{dx} = \frac{1}{x}$, $v = kx - \frac{1}{2}x^{2}$	M1	2.1	Using integration by parts with $u = \ln x$, $\frac{dv}{dx} = k - x$ clearly argued	
	Area = $\left[\left(kx - \frac{1}{2}x^2 \right) \ln x \right]_1^k - \int_1^k \frac{1}{x} \left(kx - \frac{1}{2}x^2 \right) dx$	A1	1.1b	Allow without limits	
	$\left[\left(kx - \frac{1}{2}x^2\right)\ln x\right]_1^k - \int_1^k \left(k - \frac{1}{2}x\right) dx$	M1	3.1 a	Simplifying the integrand	
	$\left[\left(kx - \frac{1}{2}x^2\right)\ln x - \left(kx - \frac{1}{4}x^2\right)\right]_1^k$	A1	1.1b	Second part correct	
	$\left(\left(k^{2} - \frac{1}{2}k^{2}\right)\ln k - \left(k^{2} - \frac{1}{4}k^{2}\right)\right) - \left(\left(k - \frac{1}{2}\right)\ln 1 - \left(k - \frac{1}{4}\right)\right)$	M1dep	1.1a	Using limits. Dependendent on M mark for integration by parts	
	$=\frac{1}{2}k^{2}\ln k - \frac{3}{4}k^{2} + k - \frac{1}{4}$	A1 [8]	1.1b	Cao	

www.yesterdaysmathsexam.com Mark Scheme

Question	Answer	Marks	AOs		Guidance
10	OR Integral split into two separate integrals $\int_{1}^{k} k \ln x dx$				
	Let $u = \ln x$, $\frac{dv}{dx} = k$, $\frac{du}{dx} = \frac{1}{x}$, $v = kx$	M1		Using integration by parts with $u = \ln x, \frac{dv}{dx} = k$	
	$= \left[kx\ln x\right]_{1}^{k} - \int_{1}^{k} \frac{1}{x}kx \mathrm{d}x$	M1		or $u = \ln x$, $\frac{dv}{dx} = \pm x$ clearly argued Simplifying the integrand	
	$\begin{bmatrix} kx \ln x \end{bmatrix}_{1}^{k} - \int_{1}^{k} k dx = \begin{bmatrix} kx \ln x - kx \end{bmatrix}_{1}^{k} \left(k^{2} \ln k - k^{2} \right) - \left(k \ln 1 - k \right) = k^{2} \ln k - k^{2} + k$	M1dep		Substituition of limits seen in at least one integral. Dependendent on M mark for integration by parts	
	And Area = $\int_{1}^{k} x \ln x dx$			mark for megration by parts	
	Let $u = \ln x$, $\frac{dv}{dx} = x$, $\frac{du}{dx} = \frac{1}{x}$, $v = \frac{1}{2}x^2$				
	$= \left[\frac{1}{2}x^{2}\ln x\right]_{1}^{k} - \int_{1}^{k}\frac{1}{x} \times \frac{1}{2}x^{2}dx$ $\left[\frac{1}{2}x^{2}\ln x\right]_{1}^{k} - \int_{1}^{k}\frac{1}{2}x dx$	A1		Both integrals correct at this stage Allow without limits	
	$\left[\frac{1}{2}x^{2}\ln x - \frac{1}{4}x^{2}\right]_{1}^{k}$	A1		Both integrals fully correct Allow without limits	
	$\begin{pmatrix} \frac{1}{2}k^2\ln k - \frac{1}{4}k^2 \end{pmatrix} - \left(\frac{1}{2}\ln 1 - \frac{1}{4}\right) = \frac{1}{2}k^2\ln k - \frac{1}{4}k^2 + \frac{1}{4}$ Area = $\left(k^2\ln k - k^2 + k\right) - \left(\frac{1}{2}k^2\ln k - \frac{1}{4}k^2 + \frac{1}{4}\right)$				
	$=\frac{1}{2}k^{2}\ln k - \frac{3}{4}k^{2} + k - \frac{1}{4}$	A1		Сао	

(Question	Answer	Marks	AOs		Guidance
11	(i)	Component of weight down the plane $4.7g \sin 60^{\circ}$ Equilibrium equation $T = 4.7g \sin 60^{\circ}$ = 39.889 so $T = 39.9$ to 3 sf	B1 E1 [2]	2.1 3.3	AG Award if seen Must be clear that 39.9 N is the tension and not just component of weight	
	(ii)	Resolve perpendicular to the slope <i>N</i> is the normal reaction between plane and block B $N = 4g \cos 25^{\circ}$ Resolve up the slope $T - F - 4g \sin 25^{\circ} = 0$	B1 M1 A1	1.1a 3.3 1.1b	Need not be evaluated here [≈ 35.5] Allow only sign errors <i>F</i> need not be evaluated here [≈ 23.3]	If only values are seen used,
		On the point of sliding so $F = \mu N = \mu \times 4g \cos 25^{\circ}$ $\mu = \frac{4.7g \sin 60^{\circ} - 4g \sin 25^{\circ}}{4g \cos 25^{\circ}} = 0.656 \text{ to } 3\text{sf}$	M1 A1 [5]	3.1b 1.1b	Do not allow for $F \le \mu N$ unless = used subsequently. FT their values. FT (notice this answer is 0.657 if 39.9 used for <i>T</i>)	it must be clear that the values used are friction and normal reaction.

Q	uestion		Answer	Marks	AOs		Guidance
12	(i)		C is (1, -1)	B1 [1]	1.1a	Cao	
	(ii)	A	EITHER Substitute $y = \frac{3}{4}x - 8$ into the equation of the circle	M1	3.1 a	AG Attempt to eliminate one variable	
			$(x-1)^{2} + \left(\frac{3}{4}x - 8 + 1\right)^{2} = 25$ x ² - 8x + 16 = 0 EITHER (x-4) ² = 0	M1 A1	1.1a 1.1b	Attempt to expand and collect terms to obtain 3 term quadratic expression A correct 3 term quadratic	
			OR Discriminant = $(-8)^2 - 4 \times 1 \times 16 = 0$ So the equation has a repeated root so the line is a tangent	A1 [4]	2.2a	Clearly argued	
	(ii)	А	OR Substitute $x = \frac{4}{3}y - \frac{32}{3}$ into the equation of the circle	M1	3.1 a	AG Attempt to eliminate one variable	
			$\left(\frac{4}{3}y - \frac{32}{3} - 1\right)^2 + (y+1)^2 = 25$ y ² + 10y + 25 = 0 EITHER (y+5) ² = 0	M1 A1	1.1a 1.1b	Attempt to expand and collect terms to obtain 3 term quadratic expression A correct 3 term quadratic	
			OR Discriminant = $10^2 - 4 \times 1 \times 25 = 0$ So the equation has a repeated root so the line is a tangent	A1 [4]	2.2a	Clearly argued	
		В	x = 4 and $y = -5$ so B is (4, -5)	B1 [1]	1.1a	Сао	

www.yesterdaysmathsexam.com Mark Scheme

Question	Answer	Marks	AOs		Guidance
(iii)	$\angle CAD = \angle CBD = 90^\circ$ (radius is perpendicular to	B1	2.1	Allow for one or other of these	Allow up to B1, B1 for any
	the tangent)			angles	two of these three pieces of
	Gradient of AC = $\frac{2 - (-1)}{5 - 1} = \frac{3}{4}$				evidence. Allow the final B1
	Gradient of AC = $\frac{-1}{5-1} = \frac{-1}{4}$				only when the proof is
	(-1)-(-5) 4				complete and clearly argued.
	Gradient of BC = $\frac{(-1)-(-5)}{1-4} = -\frac{4}{3}$	B1	3.1 a		
	So AC is perpendicular to BC so $\angle ACB = 90^{\circ}$	DI	J.1a		
	So ADBC is a rectangle				
	Either $AC = BC$ radius [=5]				
	Or AD = BD equal tangents	B1	2.1	Complete proof	
	so ADBC is a square.	[3]		AG	
	$\angle CAD = \angle CBD = 90^{\circ}$ (radius is perpendicular to	B1		Allow for one or other of these	
	the tangent)			angles	
	Gradient of AC = $\frac{2 - (-1)}{5 - 1} = \frac{3}{4}$				
	Gradient of BD is $\frac{3}{4}$				
	So AC is parallel to BD So ADBC is a rectangle	B1			
	AC = BC = radius	B1		Complete proof	
	so ADBC is a square.			AG	
	$\angle CAD = 90^{\circ}$ (radius is perpendicular to the	B1			
	tangent)	D.			
	AC = BC radius [=5]	B1			
	Gradient of AC = $\frac{2 - (-1)}{5 - 1} = \frac{3}{4}$				
	Equation of AD is $y-2 = -\frac{4}{3}(x-5)$			Gradient of AD must be found from	
	5			the coordintes of A and C	
	So coordinates of D are (8, -2)				
	Hence $BD = 5$ and $AD = 5$	B1		Complete proof	
	So ABCD is a rhombus				

www.yesterdaysmathsexam.com

Mark Scheme

Question	Answer	Marks	AOs		Guidance
(iv)	E is the point (1, -6) EITHER C (1, -1) 0	B1	2.1	May be implied	
	B (4, -5)	M1	3.1 a	Right-angled triangle formed and use of arctan	
	$\theta = \arctan\left(\frac{3}{4}\right) = 0.6435$	A1	3.1 a	oe	
	OR $BE = \sqrt{(4-1)^2 + (-5-(-6))^2} = \sqrt{10}$ Cosine rule in triangle BCE $\cos BCE = \frac{5^2 + 5^2 - 10}{2 \times 5 \times 5} \left[= \frac{40}{50} \right]$ $\angle BCE = 0.6435$ OR M is the midpoint of BE M is (2.5, -5.5) $BM = \sqrt{(4-2.5)^2 + (-5-(-5.5))^2} = \frac{1}{2}\sqrt{10}$ $(\frac{1}{2}\sqrt{10})$	(M1) (A1)		Using distance BC and the cosine rule oe	
	$\angle BCM = \arcsin\left(\frac{\frac{1}{2}\sqrt{10}}{5}\right) = 0.32175$	(M1)		Using trig in triangle BCM or ECM Allow for $\angle BCM$	
	$\angle BCE = 0.6435$	(A1)		Oe. Must be $\angle BCE$	
	Area sector = $\frac{1}{2}r^2\theta = \frac{1}{2} \times 25 \times 2 \times 0.32175$	M1dep	1.1 a	Using the sector area formula	
	= 8.04376	A1 [5]	1.1b	FT their $\angle BCM$	

www.yesterdaysmathsexam.com Mark Scheme

Q	uestion	Answer	Marks	AOs		Guidance
13	(i)	$f'(x) = \frac{1}{3} (27 - 8x^3)^{-\frac{2}{3}} \times (-24x^2)$ $\left[= \frac{-8x^2}{(27 - 8x^3)^{\frac{2}{3}}} \right]$	M1 A1	1.1a 1.1	Using the chain rule Allow unsimplified	
		$f'(1.5) = -\frac{8 \times 1.5^2}{0}$ and dividing by zero zgives the error.	E1 [3]	2.4	Sufficient to say "can't divide by zero" oe	
	(ii)	$(27-8x^3)^{\frac{1}{3}} = 27^{\frac{1}{3}} \left(1-\frac{8}{27}x^3\right)^{\frac{1}{3}}$	B1	3.1a	Dealing with the 27 correctly	
		$= 3 \left(1 + \left(\frac{1}{3}\right) \left(-\frac{8x^3}{27}\right) + \frac{\left(\frac{1}{3}\right) \left(-\frac{2}{3}\right)}{2!} \left(-\frac{8x^3}{27}\right)^2 + \dots \right)$	M1	1.1a	Using the Binomial expansion substantially correctly	
		$=3-\frac{8x^3}{27}-\frac{64x^6}{2187}+\dots$	A1 [3]	1.1b	Cao	
	(iii)	The binomial expansion is valid for $\left -8\frac{x^3}{27}\right < 1$ x < 1.5 and the limits of the integral are completely in this interval.	B1 E1 [2]	2.4 2.3	Allow unsimplified but must use correct modulus notation or equivalent Must indicate that the limits of the integral lie in their interval for which the expansion is valid.	
	(iv)	$\frac{0.25}{2} (3 + 2.6684 + 2(2.9954 + 2.9625 + 2.8694))$	B1 M1	1.1a 1.1b	h = 0.25 used For sum in the bracket – condone one slip.	Values from candidates own calculators may differ in the last decimal place.
		$=\frac{0.25}{2} \times 23.3224 = 2.9153$	A1 [3]	1.1b	Allow for 2.92 or better	
	(v)	There is area between the curve and the top of the trapezia, so some area is missing from the estimate.	E1 [1]	2.4	Allow for any sensible explanation eg the trapezia are under the curve	"The curve is concave downwards" on its own is not quite enough

Question		Answer	Marks	AOs		Guidance
14	(i)	u = 5, v = 11.4, t = 4				
		$a = \frac{v - u}{t} = \frac{11.4 - 5}{4} = 1.6$	M1	3.1b	Using <i>suvat</i> equation(s) leading to value for <i>a</i>	
		i +	A1	1.1b	Any form	
		v = 5 + 1.6t	A1	3.3	FT their a	
	(::)	The converse due to able to concluste in definitely.	[3] E1	3.5b		
	(ii)	The car would not be able to accelerate indefinitely – the velocity would become too large	[1]	3.50		
	(iii)	$\frac{1}{2} = 17.8$				
	(III)		B1	1.1a	Calculation or point on graph	
		$t = \frac{17.8 - 5}{1.6} = 8$	DI	1.1a	labelled at $t = 8$	
		20 velocity (ms-1)	G1	1.1a	Two line segments with one	
		15			horizontal	
		10	G1	3.5c	Axes labelled.	Mark intent for 17.8 – allow
					(0, 5) and constant speed 17.8 clear	for a linear scale beyond 17.8
		5	[2]		on vertical scale	
		time (s) 5 10 15 20	[3]			
	(iv)	Dividing area into sections	M1	3.1b		FT their graph if linear for
						M1 A0 for a triangle or
		Area under trapezium = $\frac{1}{2}(5+17.8) \times 8 = 91.2$	A1	1.1a	May be found as sum of areas. May	trapezium area
		Area rectangle $12 \times 17.8 = 213.6$			be implied by correct total	
		Total displacement = 304.8 m	A1	1.1b	FT their distance found for first 8s	213.6 must be added to
			[3]			another distance
	(v)	When $t = 4$ $v = 5 + 0.3 \times 4^2 - 0.05 \times 4^3 = 11.4$ m s ⁻¹	B1	3.4	Allow without comment	
		Which matches the given value	[1]			
	(vi)	$\frac{\mathrm{d}v}{\mathrm{d}t} = 0.6 \times 2t - 0.05 \times 3t^2 \left[= 1.2t - 0.15t^2 \right]$				Final mark can be awarded
		$\begin{bmatrix} \frac{1}{dt} & -0.05 \times 3t & \begin{bmatrix} -1.2t & -0.15t \end{bmatrix}$	M1	1.1a	Need not be simplified	independently for a statement
		When $t = 8$ $v = 1.2 \times 8 - 0.15 \times 64 = 0$	4.1	2.2		about change in acceleration
		Acceleration is zero at $t = 8$	A1	3.2a	Must mention acceleration	as long as supported by some
		which means that the car reaches its maximum	E1	2.2-	Must compare with model A	numerical evidence
		speed without the sudden change in acceleration in		3.2a	Must compare with model A	
		model A.	[3]			

www.yesterdaysmathsexam.com Mark Scheme

Question	Answer	Marks	AOs		Guidance
(vii)	EITHER	M1	2.1		Allow for correct definite
	$\int_{0}^{8} (5+0.6t^{2}-0.05t^{3}) dt = \left[5t+0.2t^{3}-0.0125t^{4}\right]_{0}^{8}$ =91.2 m	A1	1.1b	вс	integral stated and calculator used. Also allow M1A1 for
	which is same as model A for the first 8 s Distance is the same for the remainder of the time So this is the same as model A at $t = 20$	E1 [3]	2.1	Must consider to $t = 20$	$5 \times 8 - 0.2 \times 8^3 - 0.0125 \times 8^4$ seen
	OR $\int_{0}^{8} (5+0.6t^{2}-0.05t^{3}) dt = [5t+0.2t^{3}-0.0125t^{4}]_{0}^{8}$ =91.2 m	M1 A1		BC	Allow for correct definite integral stated and calculator used.
	Distance at 17.8 ms ⁻¹ 213.6 Total distance 304.8m [which is the same as model A]	Al		Must consider to $t = 20$	

OCR (Oxford Cambridge and RSA Examinations) The Triangle Building Shaftesbury Road Cambridge CB2 8EA

OCR Customer Contact Centre

Education and Learning

Telephone: 01223 553998 Facsimile: 01223 552627 Email: <u>general.qualifications@ocr.org.uk</u>

www.ocr.org.uk

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored

Oxford Cambridge and RSA Examinations is a Company Limited by Guarantee Registered in England Registered Office; The Triangle Building, Shaftesbury Road, Cambridge, CB2 8EA Registered Company Number: 3484466 OCR is an exempt Charity



OCR (Oxford Cambridge and RSA Examinations) Head office Telephone: 01223 552552 Facsimile: 01223 552553 UKAS UKAS USSTERSODOT

© OCR 2018