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Other names

Pearson Edexcel
Level 3 GCE

Centre Number

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Candidate Number

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Further Mathematics

Advanced

Paper 2: Core Pure Mathematics 2

Sample Assessment Material for first teaching September 2017

Time: 1 hour 30 minutes

Paper Reference

9FM0/02

You must have:

Mathematical Formulae and Statistical Tables, calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.
Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 7 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Answer ALL questions. Write your answers in the spaces provided.

1. The roots of the equation

$$x^3 - 8x^2 + 28x - 32 = 0$$

are α , β and γ

Without solving the equation, find the value of

(i) $\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma}$

(ii) $(\alpha + 2)(\beta + 2)(\gamma + 2)$

(iii) $\alpha^2 + \beta^2 + \gamma^2$

(8)

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3. (i)

$$\mathbf{M} = \begin{pmatrix} 2 & a & 4 \\ 1 & -1 & -1 \\ -1 & 2 & -1 \end{pmatrix}$$

where a is a constant.

(a) For which values of a does the matrix \mathbf{M} have an inverse?

(2)

Given that \mathbf{M} is non-singular,

(b) find \mathbf{M}^{-1} in terms of a

(4)

(ii) Prove by induction that for all positive integers n ,

$$\begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^n = \begin{pmatrix} 3^n & 0 \\ 3(3^n - 1) & 1 \end{pmatrix}$$

(6)

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Question 3 continued

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(Total for Question 3 is 12 marks)

4. A complex number z has modulus 1 and argument θ .

(a) Show that

$$z^n + \frac{1}{z^n} = 2\cos n\theta, \quad n \in \mathbb{Z}^+ \quad (2)$$

(b) Hence, show that

$$\cos^4 \theta = \frac{1}{8}(\cos 4\theta + 4\cos 2\theta + 3) \quad (5)$$

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Question 4 continued

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(Total for Question 4 is 7 marks)

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5.

$$y = \sin x \sinh x$$

- (a) Show that $\frac{d^4 y}{dx^4} = -4y$ (4)
- (b) Hence find the first three non-zero terms of the Maclaurin series for y , giving each coefficient in its simplest form. (4)
- (c) Find an expression for the n th non-zero term of the Maclaurin series for y . (2)

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6. (a) (i) Show on an Argand diagram the locus of points given by the values of z satisfying

$$|z - 4 - 3\mathbf{i}| = 5$$

Taking the initial line as the positive real axis with the pole at the origin and given that

$$\theta \in [\alpha, \alpha + \pi], \text{ where } \alpha = -\arctan\left(\frac{4}{3}\right),$$

- (ii) show that this locus of points can be represented by the polar curve with equation

$$r = 8 \cos \theta + 6 \sin \theta \quad (6)$$

The set of points A is defined by

$$A = \left\{ z : 0 \leq \arg z \leq \frac{\pi}{3} \right\} \cap \left\{ z : |z - 4 - 3\mathbf{i}| \leq 5 \right\}$$

- (b) (i) Show, by shading on your Argand diagram, the set of points A .
 (ii) Find the **exact** area of the region defined by A , giving your answer in simplest form. (7)

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Question 6 continued

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(Total for Question 6 is 13 marks)

7. At the start of the year 2000, a survey began of the number of foxes and rabbits on an island.

At time t years after the survey began, the number of foxes, f , and the number of rabbits, r , on the island are modelled by the differential equations

$$\frac{df}{dt} = 0.2f + 0.1r$$

$$\frac{dr}{dt} = -0.2f + 0.4r$$

- (a) Show that $\frac{d^2f}{dt^2} - 0.6\frac{df}{dt} + 0.1f = 0$ (3)
- (b) Find a general solution for the number of foxes on the island at time t years. (4)
- (c) Hence find a general solution for the number of rabbits on the island at time t years. (3)

At the start of the year 2000 there were 6 foxes and 20 rabbits on the island.

- (d) (i) According to this model, in which year are the rabbits predicted to die out?
(ii) According to this model, how many foxes will be on the island when the rabbits die out?
(iii) Use your answers to parts (i) and (ii) to comment on the model. (7)

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 17 marks)

TOTAL FOR PAPER IS 75 MARKS

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