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Other names

Pearson Edexcel
International
Advanced Level

Centre Number

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Candidate Number

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Core Mathematics C34

Advanced

Tuesday 17 January 2017 – Morning
Time: 2 hours 30 minutes

Paper Reference

WMA02/01**You must have:**

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

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Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided – *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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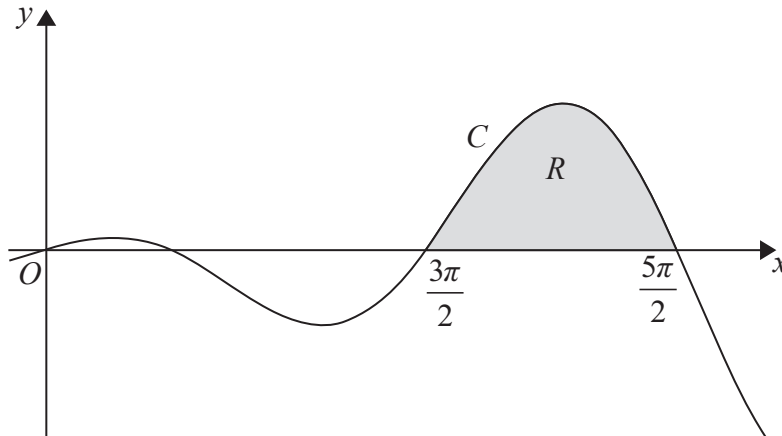


Figure 1

Figure 1 shows a sketch of part of the curve C with equation

$$y = x \cos x, \quad x \in \mathbb{R}$$

The finite region R , shown shaded in Figure 1, is bounded by the curve C and the x -axis for $\frac{3\pi}{2} \leq x \leq \frac{5\pi}{2}$

- (a) Complete the table below with the exact value of y corresponding to $x = \frac{7\pi}{4}$ and with the exact value of y corresponding to $x = \frac{9\pi}{4}$

x	$\frac{3\pi}{2}$	$\frac{7\pi}{4}$	2π	$\frac{9\pi}{4}$	$\frac{5\pi}{2}$
y	0		2π		0

(1)

- (b) Use the trapezium rule, with all five y values in the completed table, to find an approximate value for the area of R , giving your answer to 4 significant figures.

(3)

- (c) Find

$$\int x \cos x \, dx$$

(3)

- (d) Using your answer from part (c), find the exact area of the region R .

(2)



11. (a) Express $35 \sin x - 12 \cos x$ in the form $R \sin(x - \alpha)$, where $R > 0$ and $0 < \alpha < \frac{\pi}{2}$

Give the exact value of R , and give the value of α , in radians, to 4 significant figures. (3)

- (b) Hence solve, for $0 \leq x < 2\pi$,

$$70 \sin x - 24 \cos x = 37$$

(Solutions based entirely on graphical or numerical methods are not acceptable.) (4)

$$y = \frac{7000}{31 + (35 \sin x - 12 \cos x)^2}, \quad x > 0$$

- (c) Use your answer to part (a) to calculate

- (i) the minimum value of y ,
(ii) the smallest value of x , $x > 0$, at which this minimum value occurs. (4)

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Question 11 continued

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(Total 11 marks)

Q11

Grading boxes



12. In freezing temperatures, ice forms on the surface of the water in a barrel. At time t hours after the start of freezing, the thickness of the ice formed is x mm. You may assume that the thickness of the ice is uniform across the surface of the water.

At 4pm there is no ice on the surface, and freezing begins.

At 6pm, after two hours of freezing, the ice is 1.5 mm thick.

In a simple model, the rate of increase of x , in mm per hour, is assumed to be constant for a period of 20 hours.

Using this simple model,

(a) express t in terms of x , (2)

(b) find the value of t when $x = 3$ (1)

In a second model, the rate of increase of x , in mm per hour, is given by the differential equation

$$\frac{dx}{dt} = \frac{\lambda}{(2x + 1)} \text{ where } \lambda \text{ is a constant and } 0 \leq t \leq 20$$

Using this second model,

(c) solve the differential equation and express t in terms of x and λ , (3)

(d) find the exact value for λ , (1)

(e) find at what time the ice is predicted to be 3 mm thick. (2)

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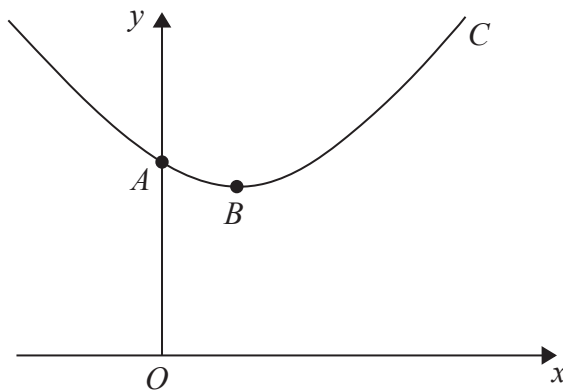


Figure 4

The curve C shown in Figure 4 has parametric equations

$$x = 1 + \sqrt{3} \tan \theta, \quad y = 5 \sec \theta, \quad -\frac{\pi}{2} < \theta < \frac{\pi}{2}$$

The curve C crosses the y -axis at A and has a minimum turning point at B , as shown in Figure 4.

(a) Find the exact coordinates of A . (3)

(b) Show that $\frac{dy}{dx} = \lambda \sin \theta$, giving the exact value of the constant λ . (4)

(c) Find the coordinates of B . (2)

(d) Show that the cartesian equation for the curve C can be written in the form

$$y = k\sqrt{(x^2 - 2x + 4)}$$

where k is a simplified surd to be found. (3)

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14. *ABCD* is a parallelogram with *AB* parallel to *DC* and *AD* parallel to *BC*.
The position vectors of *A*, *B*, *C*, and *D* relative to a fixed origin *O* are ***a***, ***b***, ***c*** and ***d*** respectively.

Given that

$$\mathbf{a} = \mathbf{i} + \mathbf{j} - 2\mathbf{k}, \quad \mathbf{b} = 3\mathbf{i} - \mathbf{j} + 6\mathbf{k}, \quad \mathbf{c} = -\mathbf{i} + 3\mathbf{j} + 6\mathbf{k}$$

- (a) find the position vector ***d***, (3)

- (b) find the angle between the sides *AB* and *BC* of the parallelogram, (4)

- (c) find the area of the parallelogram *ABCD*. (2)

The point *E* lies on the line through the points *C* and *D*, so that *D* is the midpoint of *CE*.

- (d) Use your answer to part (c) to find the area of the trapezium *ABCE*. (2)

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