| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 9(a) | Equation of motion for $P$ | M1 | 3.3 |
|  | $2 m g-T=2 m^{\prime} \frac{5 g}{7}$ | A1 | 1.1b |
|  | $T=\frac{4 m g}{7}$ | A1 | 1.1b |
|  |  | (3) |  |
| (b) | Since the string is modelled as being inextensible | B1 | 3.4 |
|  |  | (1) |  |
| (c) | Equation of motion for $Q$ OR for whole system | M1 | 3.3 |
|  | $T-k m g=k m^{\prime} \frac{5 g}{7} \quad$ OR $\quad 2 m g-k m g=(k m+2 m) \frac{5 g}{7}$ | A1 | 1.1b |
|  | $\frac{4 m g}{7}-k m g=k m^{\prime} \frac{5 g}{7}$ oe and solve for $k$ | DM1 | 1.1b |
|  | $k=\frac{1}{3}$ or 0.333 or better | A1 | 1.1b |
|  |  | (4) |  |
| (d) | e.g The model does not take account of the mass of the string (see notes below for alternatives) | B1 | 3.5b |
|  |  | (1) |  |
| (9 marks) |  |  |  |

## Notes: Condone both equations of motion appearing in (a) if used in (c)

(a)

M1: Resolving vertically for $P$ with usual rules, correct no. of terms but condone sign errors and $a$ does not need to be substituted (N.B. inconsistent omission of $m$ is M0). Allow $m a$ on RHS for M1
A1: A correct equation (allow if they use 7 instead of $\frac{5 g}{7}$ )
A1: A correct answer of form $c m g$, where $c=\frac{4}{7}$ oe or 0.57 or better
(b)

B1: String is inextensible. N.B. B0 if any extras (wrong or irrelevant) given

## (c)

M1: Resolving vertically for $Q$ or for a whole system equation, with usual rules, correct no. of terms but condone sign errors and neither $T$ nor $a$ does need to be substituted
N.B. Omission or extra $g$ in a resolution is an accuracy error not a method error

In 2(a), use the mass which appears in the ' $m a$ ' term of an equation of motion, to identify which particle that equation of motion applies to.

| Question | Scheme | Marks | AOs | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 2(a) | Equation of motion for $Q$ | M1 | 3.3 | Equation of motion for $Q$ with correct no. of terms, condone sign errors. |
|  | $0.6 \mathrm{~g}-\mathrm{T}=0.6 a$ | A1 | 1.1b | A correct equation |
|  | Equation of motion for $P$ | M1 | 3.3 | Equation of motion for $Q$ with correct no. of terms, condone sign errors. |
|  | $T=0.8 a$ | A1 | 1.1b | A correct equation |
|  | $a=4.2\left(\mathrm{~m} \mathrm{~s}^{-2}\right)$ * | A1* | 2.2a | Given acceleration obtained correctly. <br> You must see an equation in $a$ only before reaching $a=4.2$ |
|  |  | (5) |  | N.B. if they just use the whole system equation: $0.6 g=1.4 a$, can only score max M1A1M0A0A0 <br> N.B. Use of $g=9.81$ or 10 loses final A mark only. <br> N.B. Complete verification, using both equations, can score full marks. |


| (b) | $0.4=\frac{1}{2} \times 4.2 \times t_{1}^{2} \quad$ or e.g. they may find $v$ first and then use $v=4.2 t_{1}$ | M1 | 2.1 | Complete method (they may use more than one suvat equation) to find time for $Q$ to hit the floor <br> (M0 if 0.4 not used as distance moved and/or if 4.2 is not used as acceleration and this applies to finding $v$ as well if they use $v$ to find $t_{1}$ ) |
| :---: | :---: | :---: | :---: | :---: |
|  | $t_{1}=0.436(4357 \ldots .$.$) Allow 0.43,0.44,0.436$, or better, or any surd form e.g. $\frac{2}{\sqrt{21}}$ | A1 | 1.1b | See alternatives |
|  | $\begin{aligned} & v=4.2 \times t_{1} \quad \text { or } \quad v=\sqrt{2 \times 4.2 \times 0.4} \quad \text { or } \quad 0.4=\frac{(0+v)}{2} \times t_{1} \\ & (v=1.8330 \ldots) \end{aligned}$ | M1 | 3.4 | Complete method to find speed of $Q$ as it hits the floor (M0 if 0.4 not used as distance moved and/or if 4.2 is not used as acceleration and this applies to finding $t_{1}$ as well if they use $t_{1}$ to find $v$ ) |
|  | $t_{2}=\frac{1.5-0.4}{v}$ | M1 | 1.1b | Uses distance/speed to find time for $P$ to hit the pulley after $Q$ has hit the floor. <br> N.B. This is independent of previous M mark. |
|  | Complete strategy to solve the problem by finding the sum of the two times $t_{1}+t_{2}$ | DM1 | 3.1b | Complete method to solve the problem by finding and adding the two required times, dependent on previous three M marks |
|  | 1.0 (s) or 1.04 (s) | A1 | 1.1b |  |
|  |  | (6) |  |  |
| (c) | e.g. rope being light; rope being inextensible; pulley being smooth; pulley being small; balls being particles | B1 | 3.5b | Clear statement. Allow negatives of these i.e. the rope may not be light, the rope may not be inextensible etc Must be a limitation of the model stated in the question Penalise incorrect or irrelevant extras |
|  |  | (1) |  | B0 for: Air resistance, table being smooth |
| (12 marks) |  |  |  |  |



| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 9(a)(i) | Equation of motion for $A$ | M1 | 3.3 |
|  | $T-12.7=2.5 a$ | A1 | 1.1b |
| (ii) | Equation of motion for $B$ | M1 | 3.3 |
|  | $1.5 g-T=1.5 a$ | A1 | 1.1b |
|  |  | (4) |  |
| (b) | Solving two equations for $a$ | M1 | 1.1b |
|  | $a=0.5$ | A1 | 1.1b |
|  |  | (2) |  |
| (c) | $1=\frac{1}{2} \leftarrow 0.5 t^{2}$ | M1 | 3.4 |
|  | $t=2$ seconds | A1ft | 1.1b |
|  |  | (2) |  |
| (d) | Valid improvement, see below in notes | B1 | 3.5c |
|  | Valid improvement, see below in notes | B1 | 3.5c |
|  |  | (2) |  |
| (10 marks) |  |  |  |


| Question <br> Number | Scheme | Marks |
| :---: | :---: | :---: |
|  | $\begin{gathered} (-10 \mathbf{i}+a \mathbf{j})+(b \mathbf{i}-5 \mathbf{j})+(2 a \mathbf{i}+7 \mathbf{j})=3(3 \mathbf{i}+4 \mathbf{j}) \\ a-5+7=12 \Rightarrow a=10 \\ -10+b+2 a=9 \Rightarrow b=-1 \end{gathered}$ | M1 <br> M1 A1 <br> M1 A1 (5) |
| (b) | $\begin{aligned} 20 \mathbf{i}+20 \mathbf{j} & =\mathbf{u}+4(3 \mathbf{i}+4 \mathbf{j}) \\ \mathbf{u} & =(8 \mathbf{i}+4 \mathbf{j}) \\ u & =\sqrt{8^{2}+4^{2}}=\sqrt{80}=8.9 \text { (or better) } \end{aligned}$ | $$ |
|  | Notes | 9 |
| 2(a) | First M1 for applying $\mathbf{F}=m \mathbf{a}$; need all terms but allow slips and allow $m$ instead of 3 Second M1 (independent but M0 if they have $\mathbf{0}$ instead of ma) for equating coefficients of j <br> First A1 for $a=10$ <br> Third M1 (independent but M0 if they have $\mathbf{0}$ instead of ma) for equating coefficients of $\mathbf{i}$ Second A1 for $b=-1$ |  |
| (b) | First M1 for applying $\mathbf{v}=\mathbf{u}+t \mathbf{a}$; need all terms and must be vector $\mathbf{u}$ First A1 for $8 \mathbf{i}+4 \mathbf{j}$ <br> Second M1 (independent) for finding magnitude of their vector $\mathbf{u}$ Second A1 for $\sqrt{ } 80$ or 8.9 or better |  |

## WME01 Mechanics M1

## Mark Scheme

| Question | Scheme | Marks | Notes |
| :---: | :---: | :---: | :---: |
| 1. | Vertically: $T \cos 40+F \cos 60=5$ | M1 | First equation seen for resolution of forces. No missing/additional terms Condone sin/cos confusion and sign error(s) 5 g in place of 5 is an accuracy error $T$ must link with 40 or 50 and $F$ with 60 or 30 |
|  |  | A1 | Correct equation |
|  | Horizontally: $T \cos 50=F \cos 30$ | M1 | Second equation seen for resolution of forces No missing/additional terms <br> Condone sin/cos confusion and sign error(s) <br> 5 g in place of 5 is an accuracy error <br> $T$ must link with 40 or 50 and $F$ with 60 or 30 |
|  |  | A1 | Correct equation |
|  | Perpendicular to line of $F$ : $T \cos 10=5 \cos 30$ |  |  |
|  | Perpendicular to line of $T$ : $F \cos 10=5 \cos 50$ |  |  |
|  | Solve for $T$ or $F$ | dM1 | Dependent on using equation(s) that scored M $\operatorname{mark}(\mathrm{s})$ |
|  | $T=4.3969 . . \mathrm{N}=4.4 \mathrm{~N}$ (or better) | A1 | One correct |
|  | $F=3.263 \ldots . \quad=3.3 \mathrm{~N}($ or better $)$ | A1 | Both correct |
|  |  | [7] |  |
| 1 alt |  |  | Solution using Lami's theorem Or a triangle of forces |
|  | $\frac{5}{\sin 100}=\frac{F}{\sin 140}=\frac{T}{\sin 120}$ | M1 | One pair including $\frac{5}{\sin 100}$ or $\frac{5}{\sin 80}$ Incorrect pairing of forces and angles is M0 |
|  |  | A1 | Two fractions correct |
|  |  | M1 | Second pair of fractions |
|  |  | A1 | All correct |
|  | Solve for $T$ or $F$ | dM1 | Dependent on using equation(s) that scored M mark(s) |
|  | $T=4.3969 . . \mathrm{N}=4.4 \mathrm{~N}$ (or better) | A1 | One correct |
|  | $F=3.263 \ldots . \quad=3.3 \mathrm{~N}($ or better $)$ | A1 | Both correct |


| Question Number | Scheme | Marks | Notes |
| :---: | :---: | :---: | :---: |
| 3.(a) | $7^{2}=2 \times 9.8 h$ | M1 | Use of $v^{2}=u^{2}+2 a s$ with $u=0, v=7$ or alternative complete method to find $h$. |
|  | $h=2.5$ | A1 | Condone $h=-2.5$ in the working but the final answer must be positive. |
|  |  | (2) |  |
| 3.(b) | $9 \times 7=10.5 u$ | M1 | Use CLM to find the speed of the blocks after the impact. Condone additional factor of g throughout. |
|  | $u=6$ | A1 |  |
|  | $0^{2}=6^{2}-2 a \times 0.12$ | M1 | Use of $v^{2}=u^{2}+2 a s$ with $u=6, v=0$ <br> Allow for their $u$ and $v=0$ <br> Allow for $u=7, v=0$ <br> Accept alternative suvat method to form an equation in $a$. <br> Condone use of 12 for 0.12 |
|  |  | A1 | Correctly substituted equation in $a$ with $u=6, s=0.12$ (implied by $a=150$ ) |
|  | $(\downarrow) 10.5 g-R=10.5 \times(-\mathrm{a})$ | M1 | Use of $F=m a$ with their $a \neq \pm \mathrm{g}$ Must have all 3 terms and 10.5 Condone sign error(s) |
|  | ( $\downarrow$ ) $10.5 g-R=10.5 \times(-150)$ | A1 | Unsimplified equation with $a$ substituted and at most one error <br> (their $a$ with the wrong sign is 1 error) |
|  |  | A1 | Correct unsimplified equation with $a$ substituted |
|  | $R=1680$ or 1700 | A1 |  |
|  |  | (8) |  |
|  | Alternative for the last 6 marks: |  |  |
|  | $\frac{1}{2} \times 10.5 \times 6^{2}+10.5 \times 9.8 \times 0.12=R \times 0.12$ | M2 | Energy equation ( needs all three terms) |
|  |  | A3 | -1 each error <br> A1A1A0 for 1 error, A1A0A0 for 2 errors |
|  | $R=1680$ or 1700 | A1 |  |
|  |  | [10] |  |



| Question Number | Scheme | Marks | Notes |
| :---: | :---: | :---: | :---: |
| (c) | String slack: accel of $P($ up plane $)=-g \cos 60=-\frac{1}{2} g$ | B1 |  |
|  | $0=\frac{2.4 g}{5}-g s$ | M1 | Use of $v^{2}=u^{2}+2 a s$ or equivalent for their acceleration $\neq \frac{2 g}{5}$ |
|  | $s=\frac{2.4 g}{5} \times \frac{1}{g}=\frac{2.4}{5}=0.48$ | A1 |  |
|  | Total dist $=1.08 \mathrm{~m}$ | A1ft <br> (4) | $0.6+\text { their } 0.48$ |
| (d) | $\begin{aligned} & 0=\frac{2}{5} \sqrt{3 g}-\frac{g}{2} t \quad(0=2.17-4.9 t) \\ & t=\frac{4 \sqrt{3 g}}{5 g}=0.4426 \ldots \end{aligned}$ | M1 | Use of $v=u+a t$ or equivalent with their acceleration $\neq \frac{2 g}{5}$ to find $t$. |
|  | $=0.44$ or 0.443 | A1 (2) | only |
|  |  | [16] |  |

January 2018
Mechanics 1 - WME01
Mark Scheme

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 1 |  |  |
|  | N.B. If they assume that the tensions are the same, can score max:M0A0M1A0DM0A0A0. <br> If they use the same angles, can score max: M1A0M1A0DM0A0A0 |  |
|  | Resolve parallel to $A B: \quad T_{A} \cos 30=T_{B} \cos 45$ | M1A1 |
|  | Resolve perpendicular to $A B$ : $W=T_{A} \sin 30+T_{B} \sin 45$ | M1A1 |
|  | Solve for $T_{A}$ or $T_{B}$ | DM1 |
|  | $T_{A}=\frac{2}{1+\sqrt{3}} W(=0.73 \mathrm{~W})$ (or better) | A1 |
|  | $T_{B}=\frac{\sqrt{6}}{1+\sqrt{3}} W(=0.90 W)($ or better $)$ | A1 |
|  |  | (7) |
|  |  |  |
|  | Alternative (triangle of forces): |  |
|  |  |  |
|  | Sine rule for $T_{A}: \frac{T_{A}}{\sin 45}=\frac{W}{\sin 75} \quad$ M1A1 |  |
|  | Sine rule for $T_{B}: \frac{T_{B}}{\sin 60}=\frac{W}{\sin 75} \quad$ M1A1 |  |
|  | Solve for $T_{A}$ or $T_{B}: T_{A}=0.73 W$ (or better ) DM1A1 |  |
|  | $T_{B}=0.90 \mathrm{~W}$ (or better) A1 |  |
|  | (7) |  |
|  |  | [7] |
|  |  |  |
|  |  |  |
|  |  |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 7 a | Motion of $P$ : $\quad T-3 g=3 a$ | M1 |
|  | $33.6-3 g=3 a$ | A1 |
|  | $a=1.4\left(\mathrm{~m} \mathrm{~s}^{-2}\right) \quad *$ Given Answer* | A1 |
|  |  | (3) |
|  |  |  |
| 7b | Motion of $Q: \quad m g-T=m a$ | M1 |
|  | $m g-33.6=1.4 m$ | A1 |
|  | $m=4$ | A1 |
|  |  | (3) |
|  |  |  |
| 7c | Use of $s=(u t+) \frac{1}{2} a t^{2}: \quad 10.5=\frac{1}{2} \times 1.4 \times t^{2}$ | M1A1 |
|  | $T_{1}=\sqrt{15}=3.9$ or better | A1 |
|  |  | (3) |
|  |  |  |
| 7d | Use $v^{2}=\left(u^{2}+\right) 2 a s$ to find speed of particles when $Q$ hits ground: $v=\sqrt{2 \times 1.4 \times 10.5}(=\sqrt{29.4})$ | M1 |
|  | Use $v=u+a t$ to find additional time for $P$ to come to rest: $0=\sqrt{29.4}-g t$ | DM1 |
|  | Total time : $T_{2}=\sqrt{15}+\frac{\sqrt{29.4}}{9.8}=4.4$ or 4.43 | A1 |
|  |  | (3) |
|  |  |  |
| 7 e |  | B1 Shape <br> DB1 ft <br> their values for 5.4, $-5.4$ <br> 3.9, 4.4 (or $\mathrm{T}_{1} \mathrm{~T}_{2}$ ) |
|  |  | [14] |
|  |  |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
|  | Notes |  |
| 7 a | M1 for equation of motion for $P$ with $T$ not substituted, condone sign errors <br> First A1 for a correct equation in $a$ only (allow $\pm a$ ) <br> Second A1 for given answer (units not needed) |  |
| 7b | M1 for equation of motion for $Q$ with neither $T$ nor $a$ substituted, condone sign errors <br> First A1 for a correct equation in $m$ only <br> Second A1 for $m=4$ <br> N.B. Whole system equn: $m g-3 g=\mathrm{a}(m+3)$ may be used |  |
| 7c | M1 for a complete method to find $T_{1}$ (M0 if $g$ used) <br> First A1 for a correct equation (or equations) <br> Second A1 for $\sqrt{ } 15,3.9$ or better $v=\sqrt{ } 29.4$ (5.4) may be found in this part but only gets credit if it appears in part (d) |  |
| 7d | First M1 for a complete method to find the speed of particles when $Q$ hits the ground (M0 if using $g$ ) <br> Second M1 dependent on first M1 for a complete method to find the additional time for $P$ to come to rest (must be using $g$ ) <br> A1 for 4.4 or 4.43 |  |
| 7 e | First B1 (generous) for shape. Graph does not need to go down as far as it goes up and ignore gradients. <br> (B0 if it goes outside the range $0 \leq t \leq T_{3}$ or if a continuous vertical line is included) <br> Second B1, dependent on first B1, ft on their $\sqrt{ } 29.4, T_{1}$ and $T_{2}$ Allow $T_{1}$ and $T_{2}$ entered on the graph (rather than their numerical values) |  |
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| Question | Scheme | Marks |
| :---: | :---: | :---: |
| 1(a) | $\text { For truck: } \begin{aligned} D-600-400 & =2400 \times 0.5 \\ D & =2200 \mathrm{~N} \end{aligned}$ | M1 A1 <br> A1 <br> (3) |
| (b) | For both: $D-600=(M+2400) \times 0.5$ (or trailer: $600-200=\mathrm{M} \times 0.5)$ $M=800 \quad M=800$ | M1 A1 <br> A1 <br> (3) |
| (c) | Truck and trailer have same acceleration. | B1 $(1)$ <br>  7 |
|  | Notes Can mark (a) and (b) 'together' if it helps the candidate, provided no wrong working seen. |  |
| 1(a) | M1 for NL2 for truck only (or for a complete method if they find $M$ first), with correct no. of terms, in $D$ only. (M0 if 600 or 400 is replaced by 200) <br> First A1 for a correct equation . <br> Second A1 for 2200 (N). |  |
| 1(b) | M1 for NL2 for whole system or trailer only, with correct no. of terms. First A1 for a correct equation. (Allow ' $D$ ' or their $D$ ) Second A1 for 800. <br> N.B. In both parts of this question use the mass which is being used in their equation to guide you as to which part of the system is being considered. |  |
| 1(c) | B0 if extras included. E.g if 'tension is same' is included. <br> B1 Must include 'truck and trailer' or 'both particles' or 'accln is same throughout the system' B0 for 'accln is same' |  |
|  |  |  |
|  |  |  |

